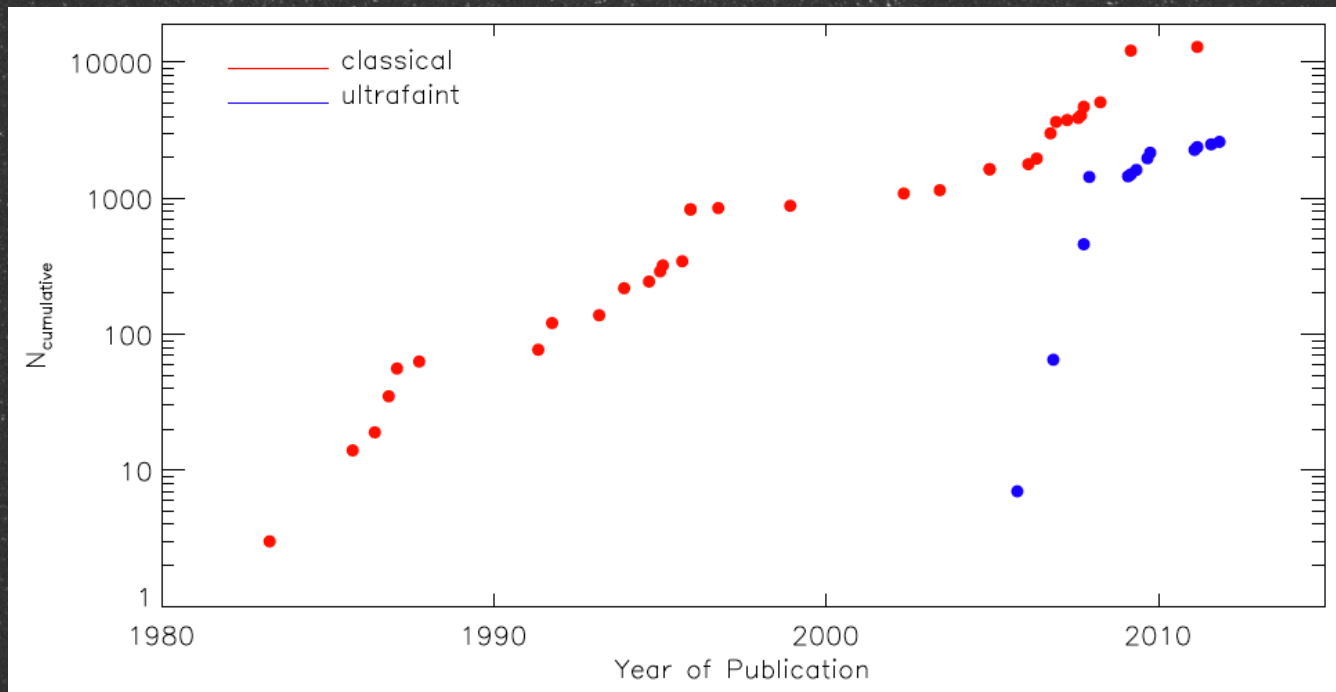


# Radial Velocity Data for Milky Way dSphs

Matthew Walker – CfA/Harvard

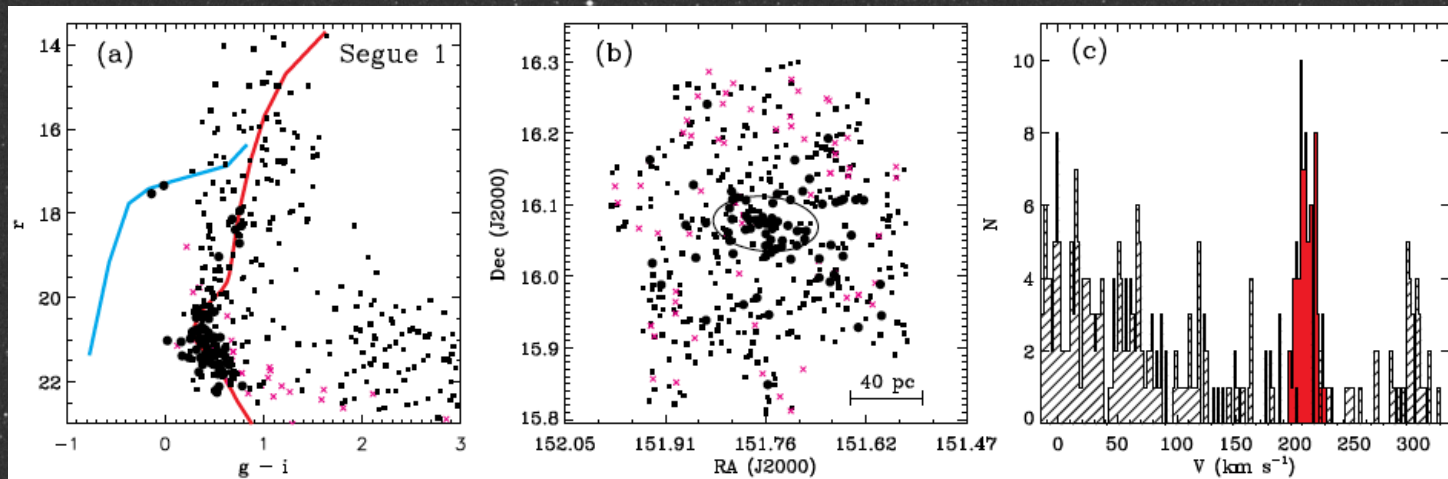


ences: Aaronson (1983); Seitzer & Frogel (1985); Suntzeff et al. (1986); Armandroff & Da Costa (1986); Aaronson & Olszewski (1987b,a); Mateo et al. (1991); Da Costa et al. (1991); Suntzeff et al. (1993); Mateo et al. (1993); Hargreaves et al. (1994b,a); Armandroff et al. (1995); Vogt et al. (1995); Queloz et al. (1995); Olszewski et al. (1995); Hargreaves et al. (1996b); Mateo et al. (1998); Kleyna et al. (2002, 2003); Tolstoy et al. (2004); Kleyna et al. (2005); Muñoz et al. (2006); Muñoz et al. (2006); Battaglia et al. (2006); Westfall et al. (2006); Walker et al. (2006, 2007a); Koch et al. (2007b,a); Martin et al. (2007); Simon & Geha (2007); Sohn et al. (2007); Mateo et al. (2008); Koch et al. (2009); Geha et al. (2009); Walker, Mateo & Olszewski (2009); Walker et al. (2009a); Belokurov et al. (2009); Carlin et al. (2009); Willman et al. (2011); Simon et al. (2011); Adén et al. (2011); Koposov et al. (2011b); Battaglia et al. (2011).

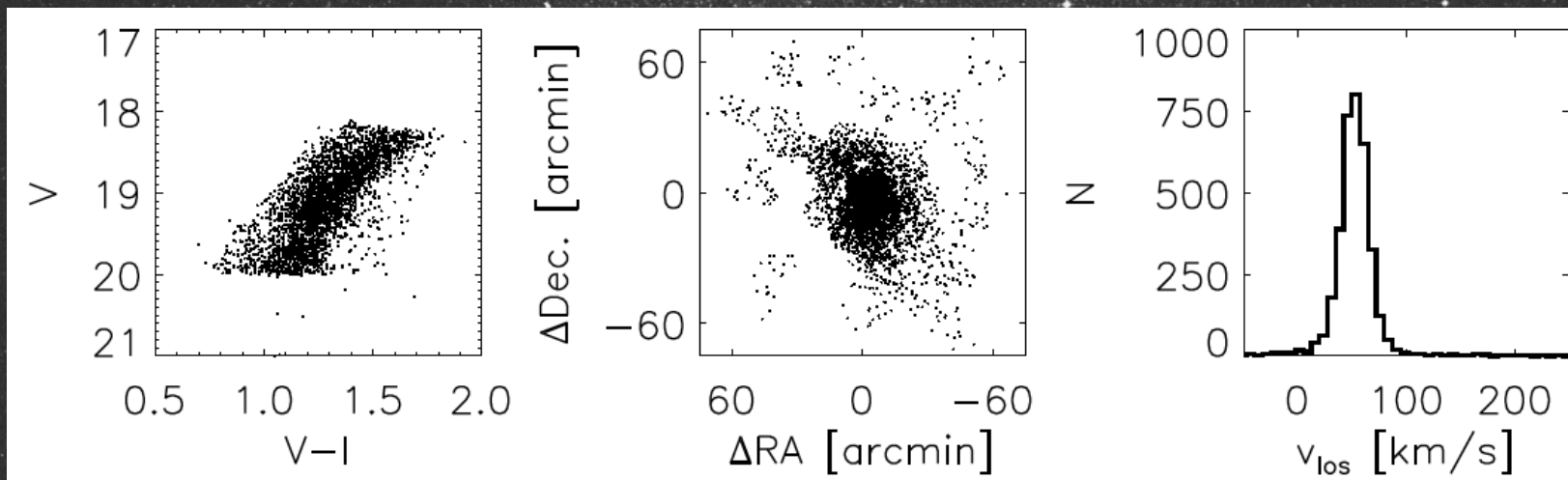
*Dynamics Meets Kinematic Tracers*

Ringberg, 11 April 2012

# 'dynamic' range of known MW dSphs



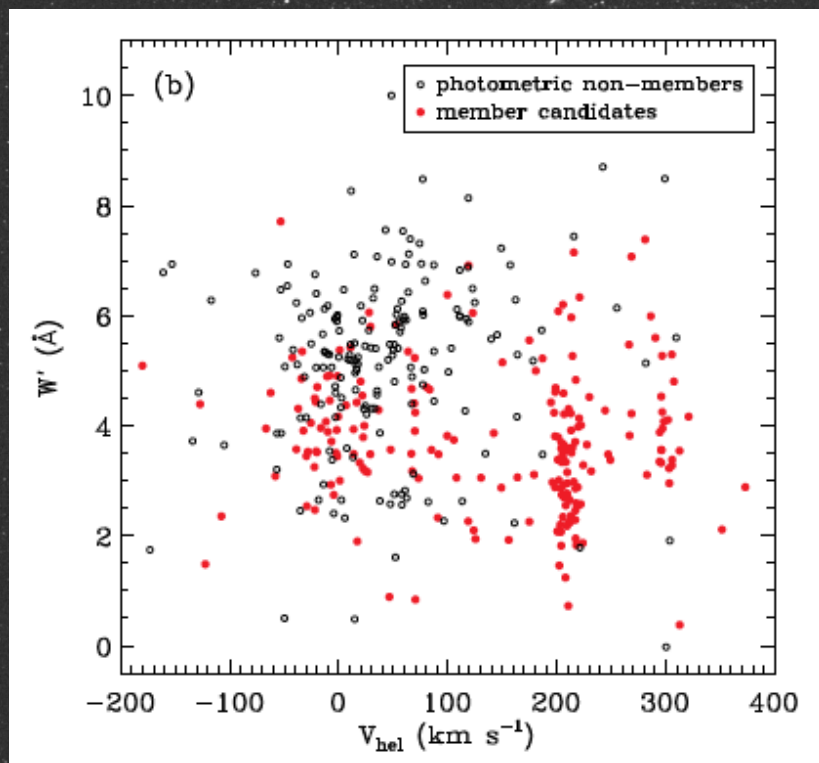
Segue 1 (Simon et al 2011)



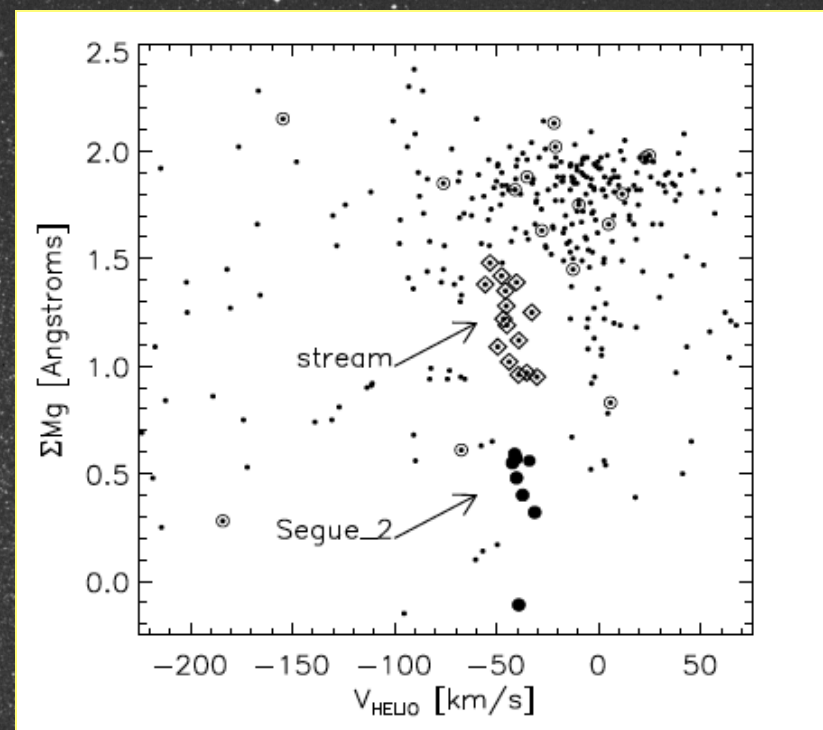
Fornax (Walker, Mateo & Olszewski 2009)



# Streams

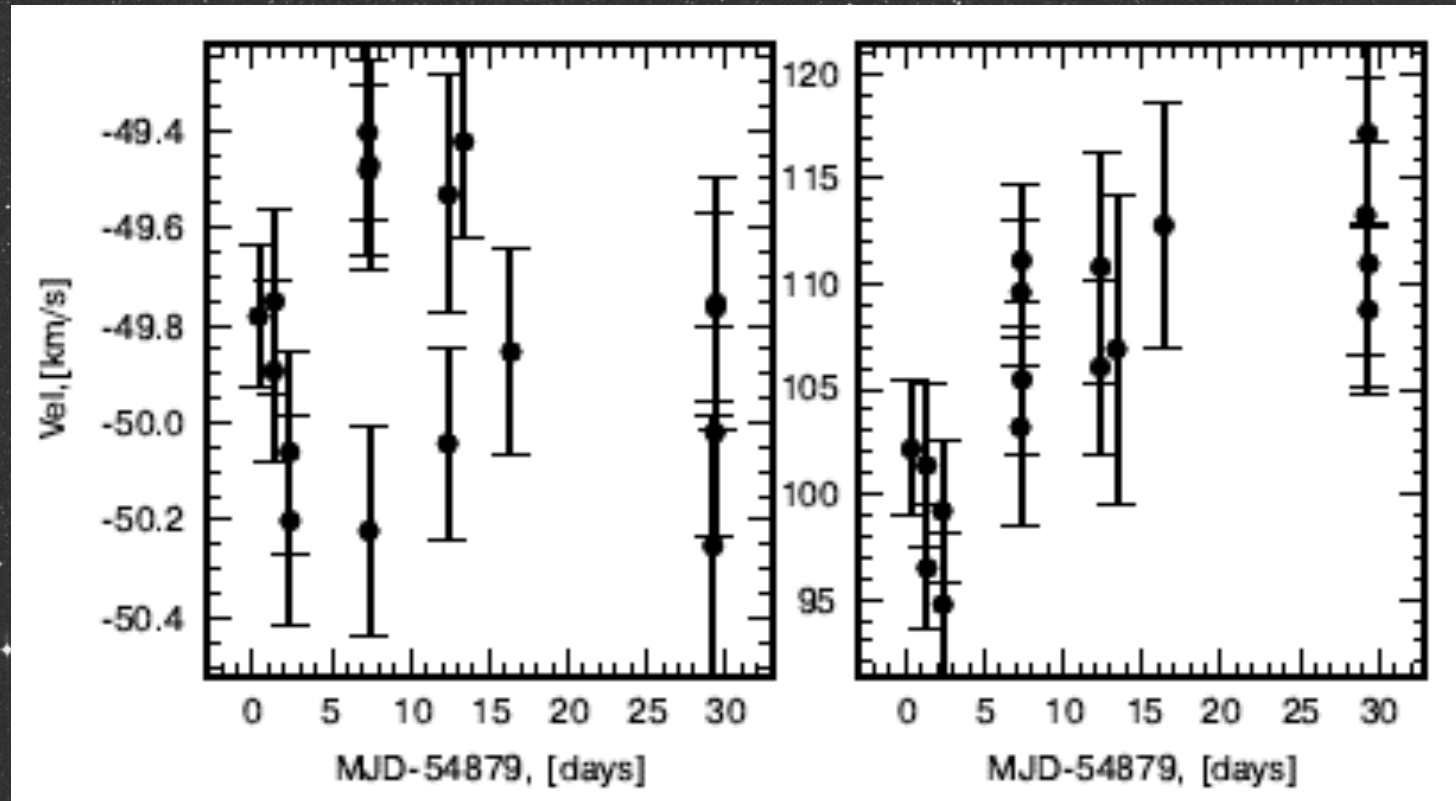


Segue 1 (Simon et al. 2011)



Segue 2 (Belokurov et al. 2009)

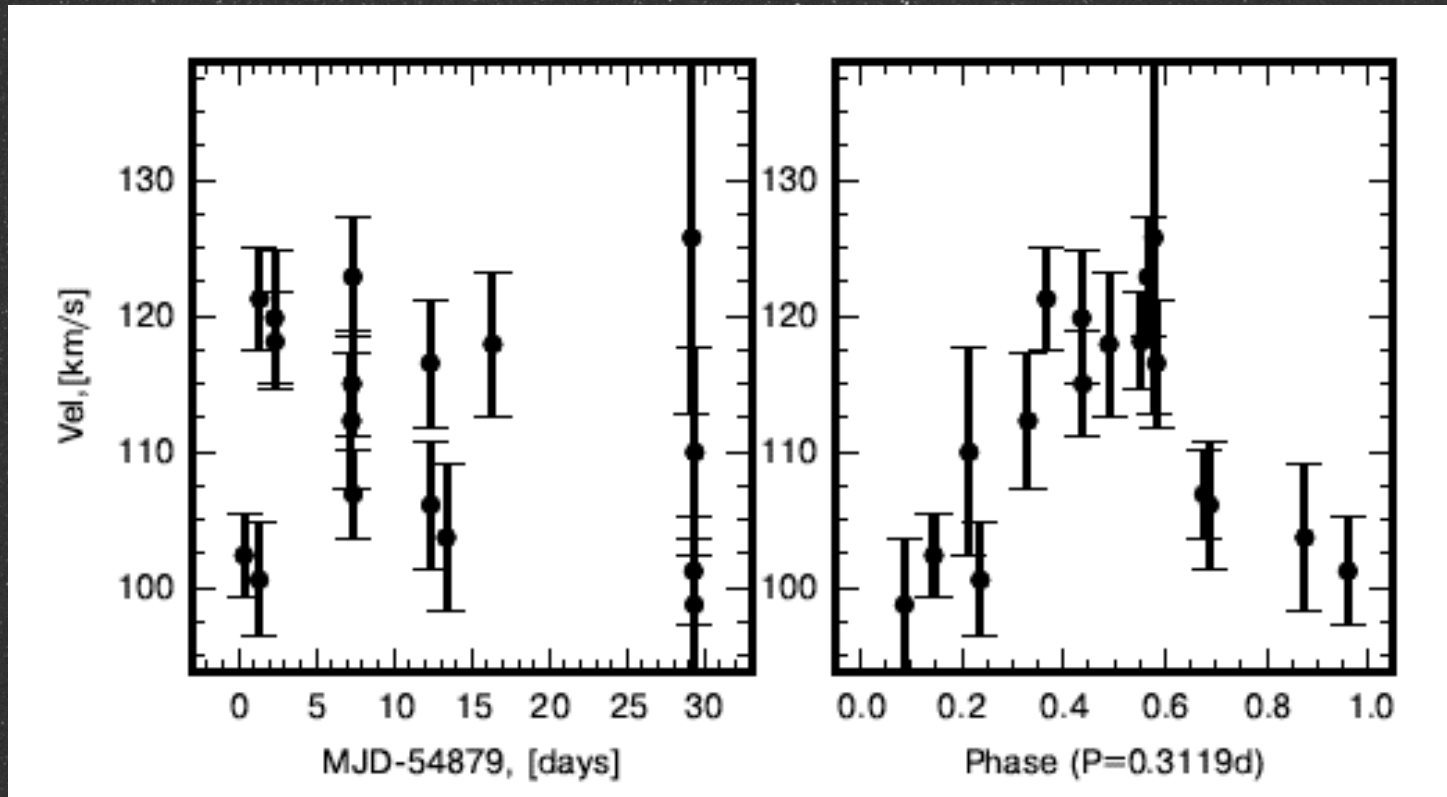
# Resolved Velocity Variability



Bootes I (Koposov et al 2011)

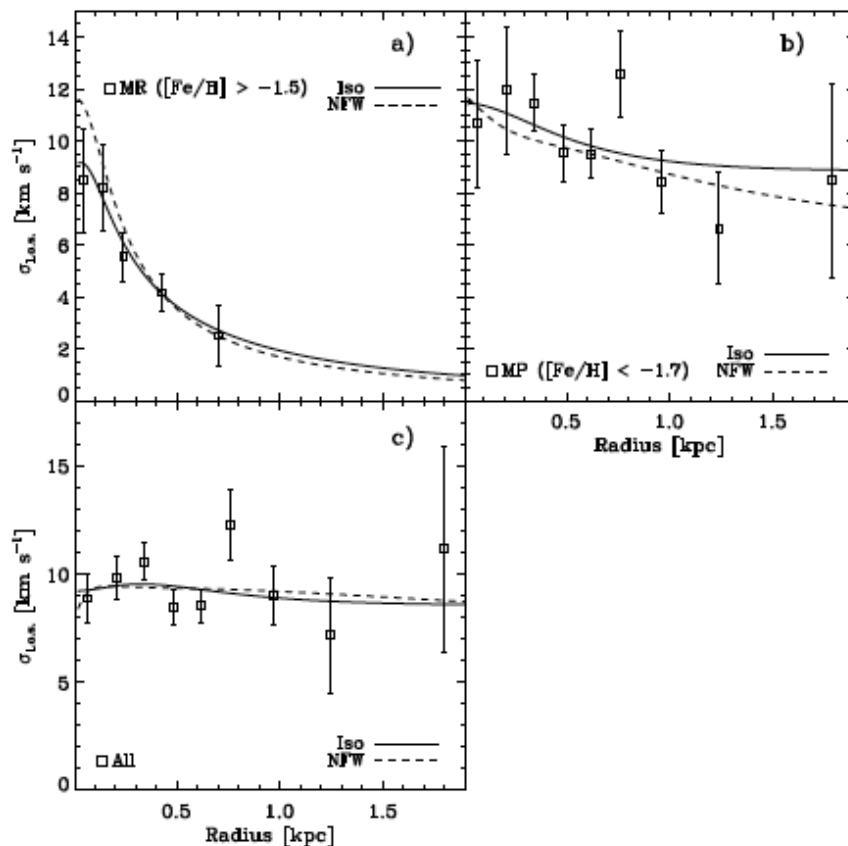
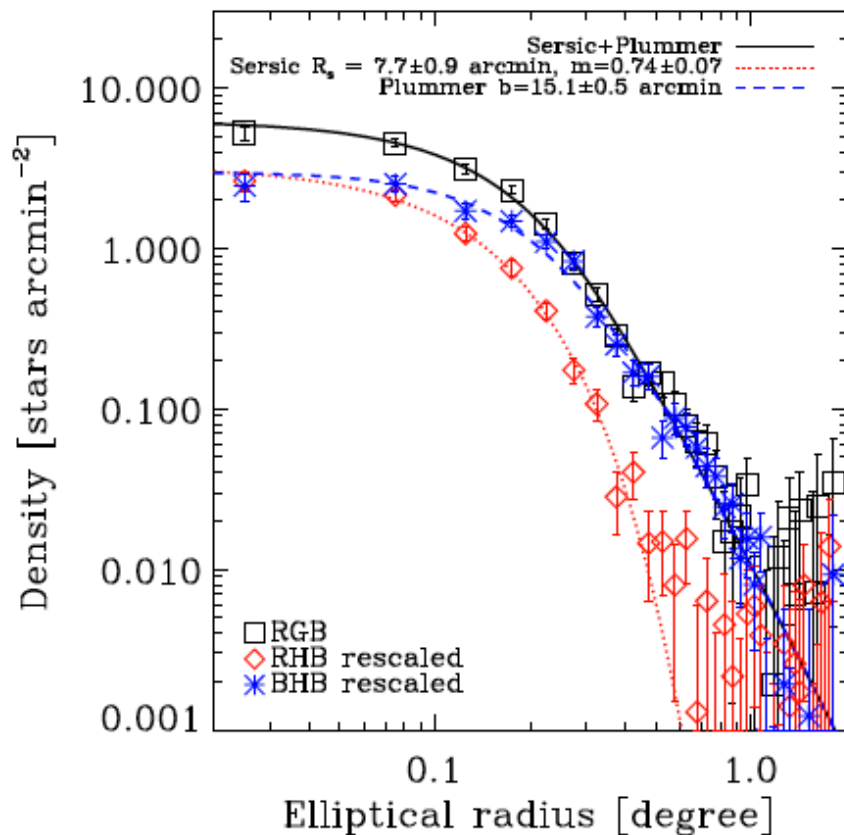


# *Resolved Velocity Variability*



Bootes I (Koposov et al 2011)

# Multiple stellar components



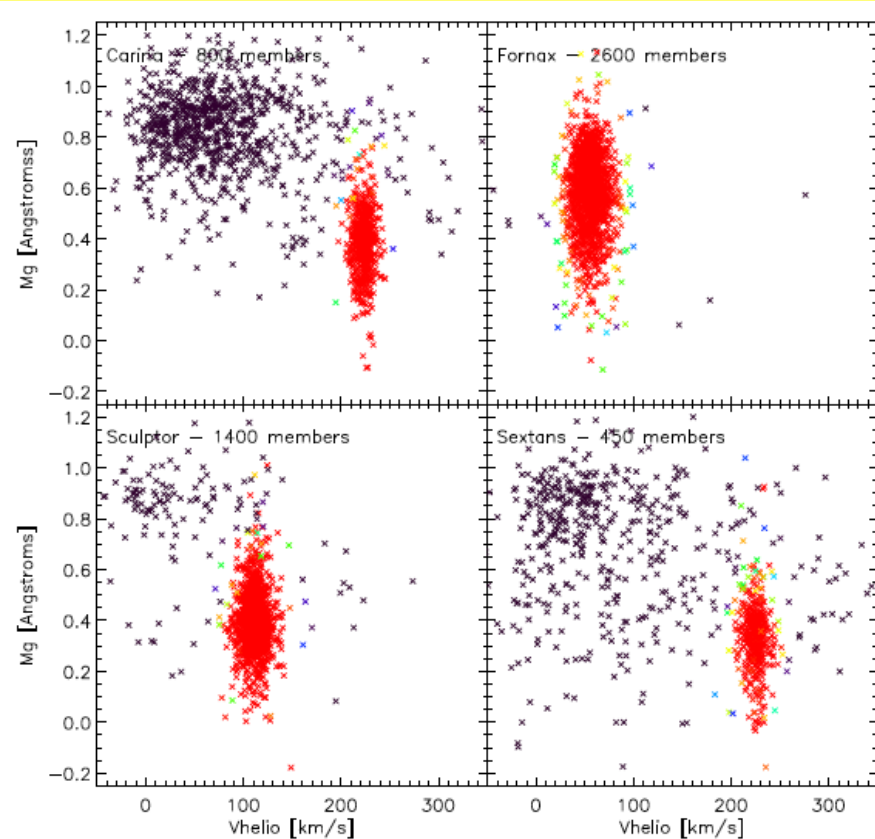
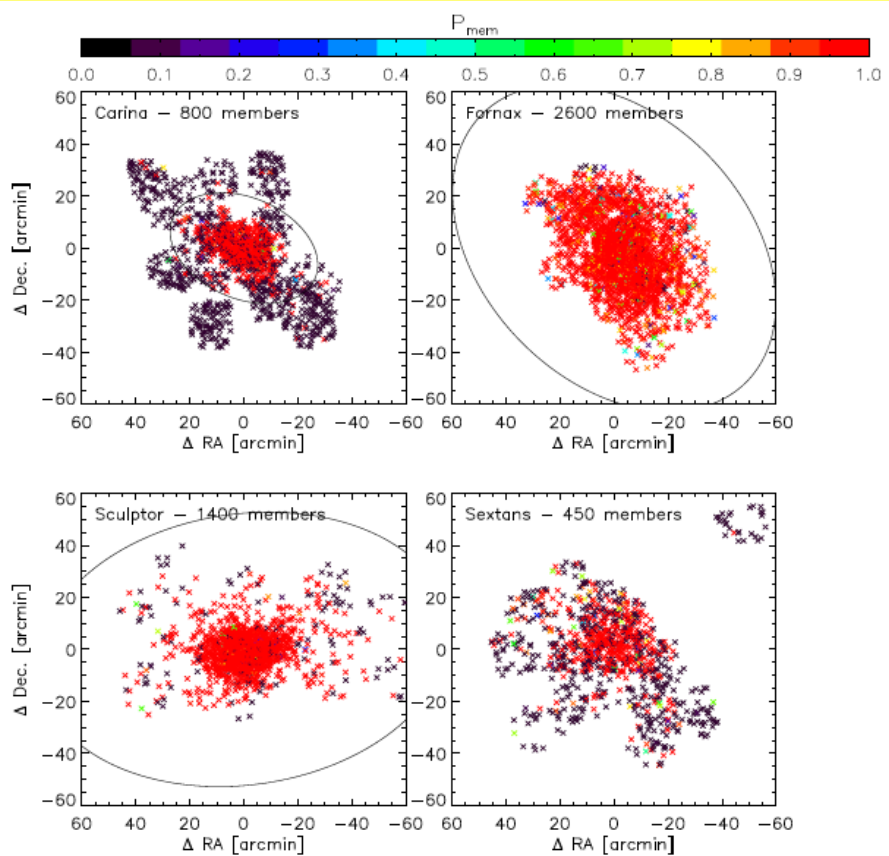
Sculptor (Tolstoy et al. 2004, Battaglia et al. 2008)

Similar for Fornax (Battaglia et al. 2006) and Sextans (Battaglia et al. 2011)



# Magellan samples

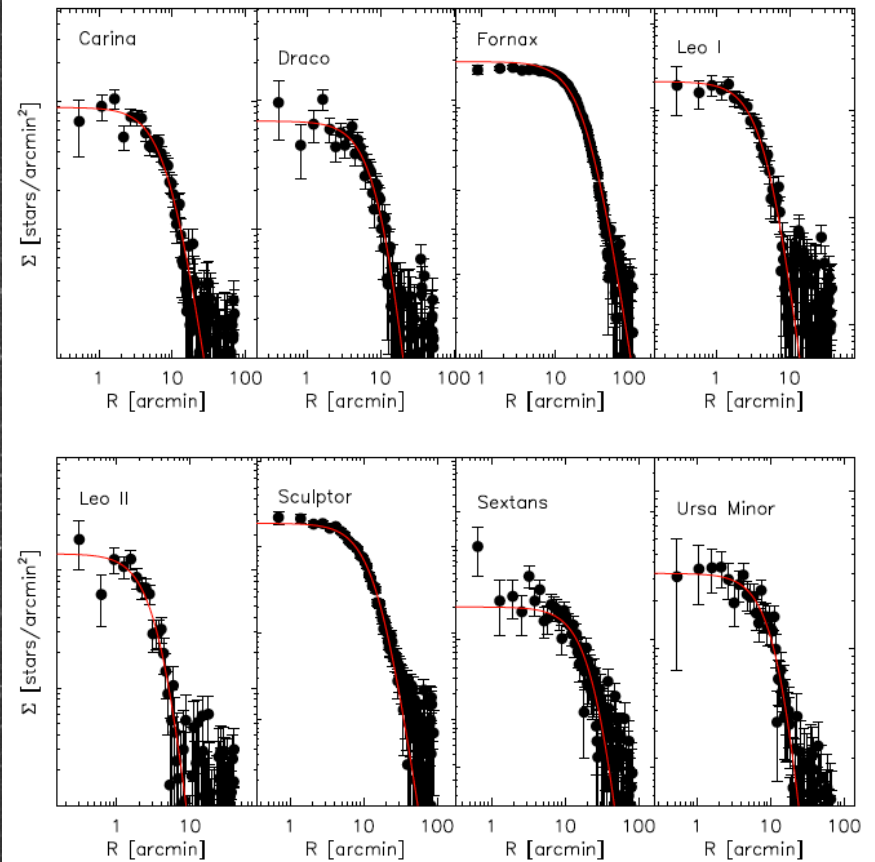
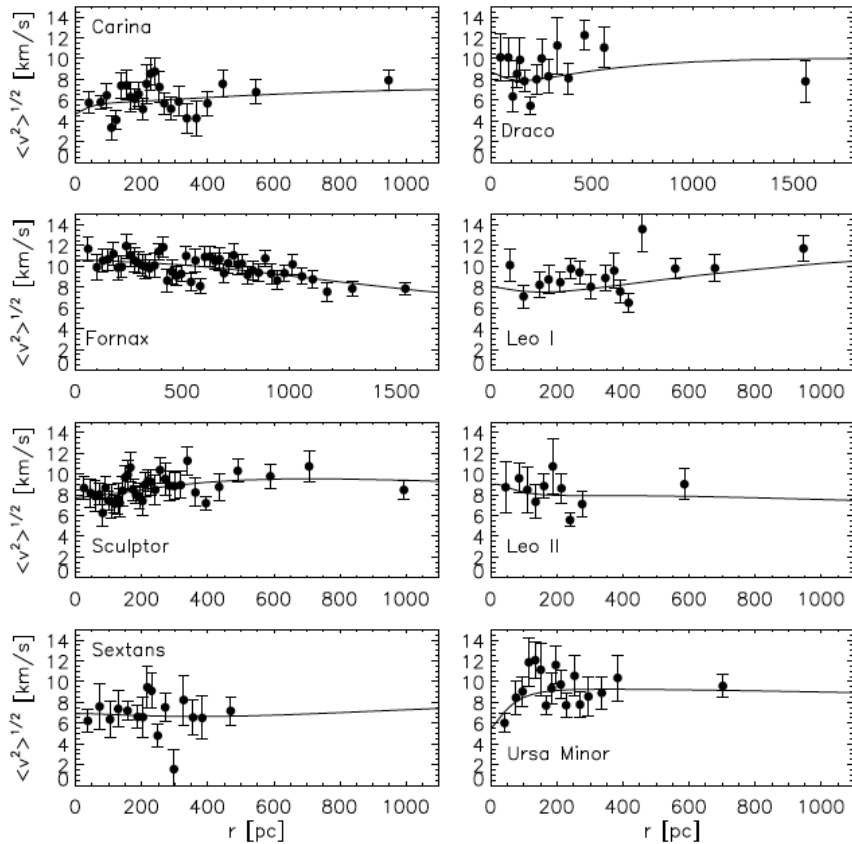
(see also VLT surveys of same galaxies)



Walker, Mateo & Olszewski (2009)

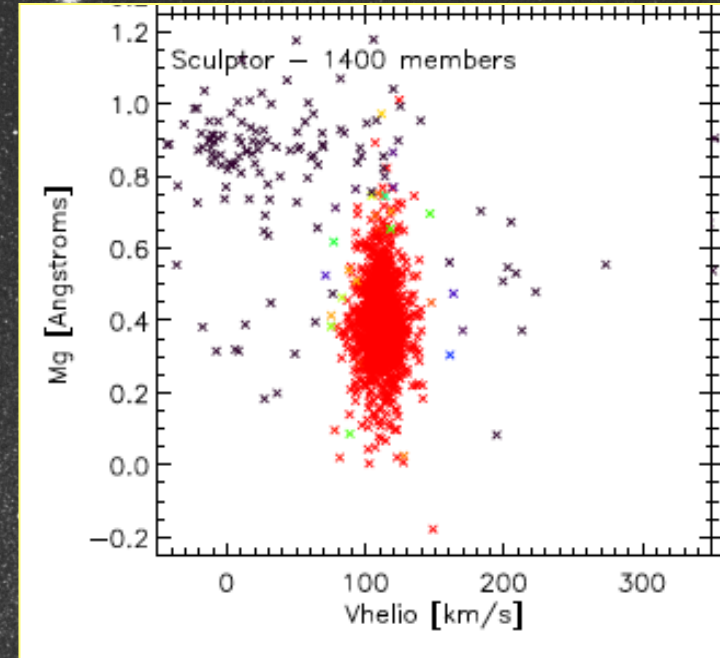
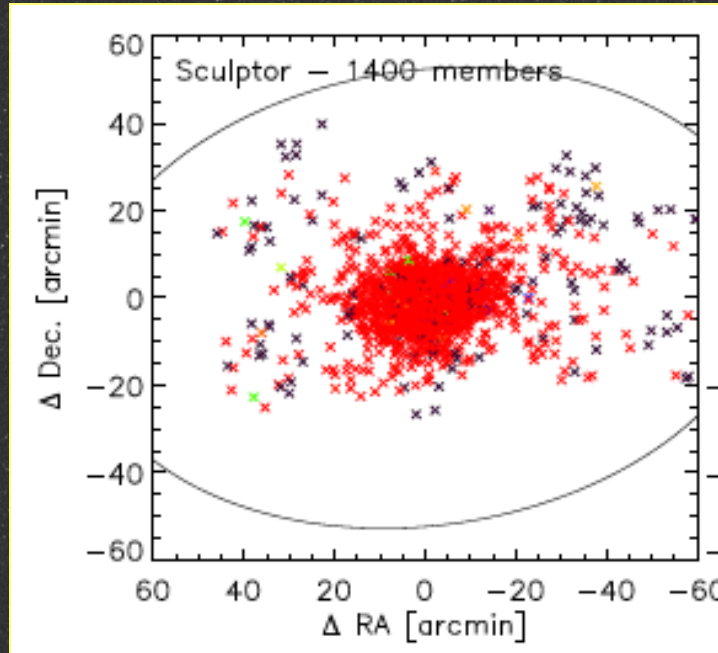
# Jeans models

$$\sigma_p^2(R) = \frac{2}{I(R)} \int_R^\infty \left(1 - \beta \frac{R^2}{r^2}\right) \frac{\nu(r) \bar{v}_r^2 r}{\sqrt{r^2 - R^2}} dr$$





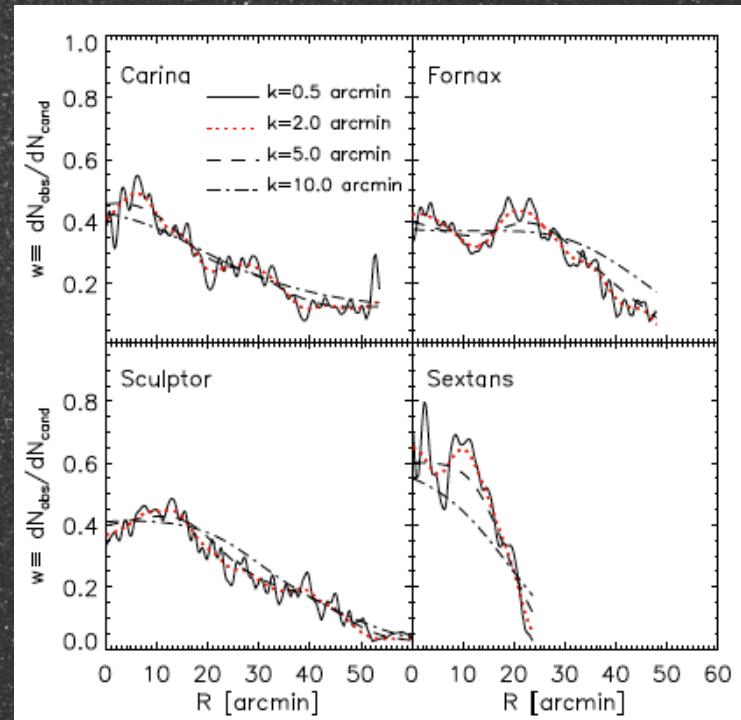
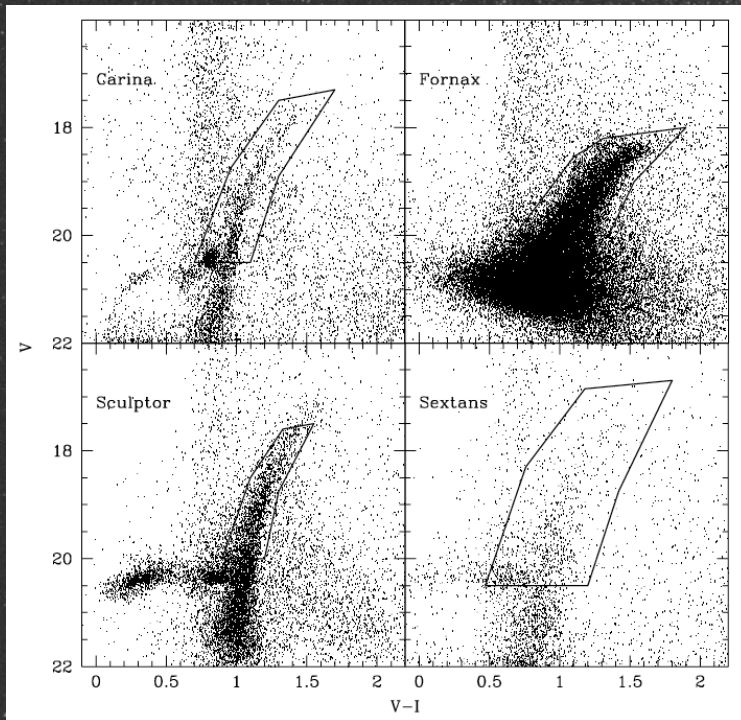
# attempted respect of data



$$L(\{R_i, V_i, W'_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_1(R_i, V_i, W'_i)}{\int \int \int w(R) p_1(R, V, W') dR dV dW'} + f_2 \frac{w(R_i) p_2(R_i, V_i, W'_i)}{\int \int \int w(R) p_2(R, V, W') dR dV dW'} \right. \\ \left. + (1 - f_1 - f_2) \frac{w(R_i) p_{\text{MW}}(R_i, V_i, W'_i)}{\int \int \int w(R) p_{\text{MW}}(R, V, W') dR dV dW'} \right]$$

# (spatial) sampling bias

$$L(\{R_i, V_i, W'_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_1(R_i, V_i, W'_i)}{\int \int \int w(R) p_1(R, V, W') dR dV dW'} + f_2 \frac{w(R_i) p_2(R_i, V_i, W'_i)}{\int \int \int w(R) p_2(R, V, W') dR dV dW'} \right. \\ \left. + (1 - f_1 - f_2) \frac{w(R_i) p_{\text{MW}}(R_i, V_i, W'_i)}{\int \int \int w(R) p_{\text{MW}}(R, V, W') dR dV dW'} \right]$$





# Assumptions

$$L(\{R_i, V_i, W_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_1(R_i, V_i, W_i)}{\int \int \int w(R) p_1(R, V, W') dR dV dW'} + f_2 \frac{w(R_i) p_2(R_i, V_i, W_i)}{\int \int \int w(R) p_2(R, V, W') dR dV dW'} \right. \\ \left. + (1 - f_1 - f_2) \frac{w(R_i) p_{\text{MW}}(R_i, V_i, W_i)}{\int \int \int w(R) p_{\text{MW}}(R, V, W') dR dV dW'} \right]$$

$$p_{R,1}(R) = \frac{2R/r_{h,1}^2}{(1 + R^2/r_{h,1}^2)^2}$$

Plummer

$$p_{V,1}(V, \alpha_*, \delta_*) = \frac{1}{\sqrt{2\pi(\sigma_{V,1}^2 + \epsilon_V^2)}} \exp \left[ -\frac{1}{2} \frac{(V - \langle V \rangle_{\alpha_*, \delta_*})^2}{\sigma_{V,1}^2 + \epsilon_V^2} \right]$$

Gaussian

$$p_{W,1}(W) = \frac{1}{\sqrt{2\pi(\sigma_{W,1}^2 + \epsilon_W^2)}} \exp \left[ -\frac{1}{2} \frac{(W - \langle W \rangle_1)^2}{\sigma_{W,1}^2 + \epsilon_W^2} \right]$$

Gaussian

# 12 free parameters

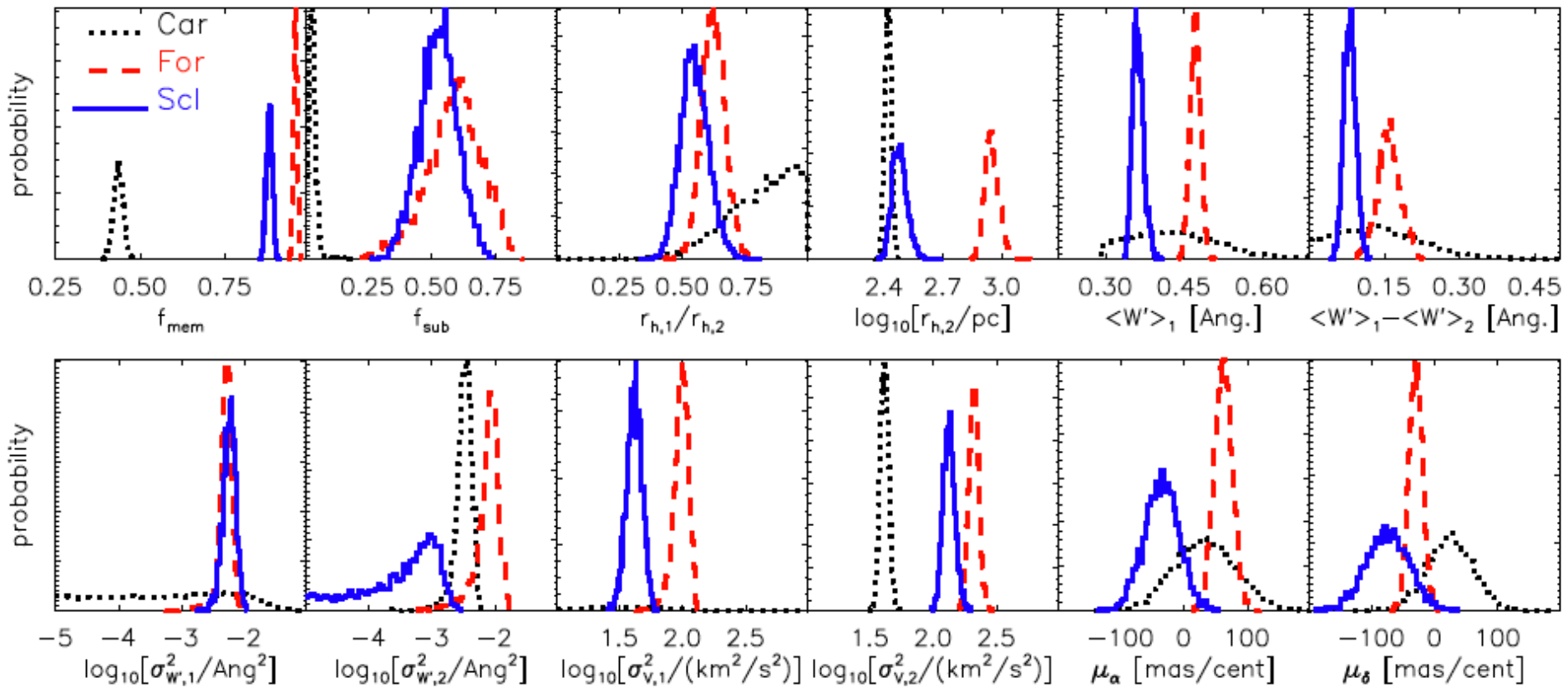
$$L(\{R_i, V_i, W_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_1(R_i, V_i, W_i')}{\int \int \int w(R) p_1(R, V, W') dR dV dW'} + f_2 \frac{w(R_i) p_2(R_i, V_i, W_i')}{\int \int \int w(R) p_2(R, V, W') dR dV dW'} \right. \\ \left. + (1 - f_1 - f_2) \frac{w(R_i) p_{\text{MW}}(R_i, V_i, W_i')}{\int \int \int w(R) p_{\text{MW}}(R, V, W') dR dV dW'} \right]$$

MCMC PARAMETERS AND TOP-HAT PRIORS FOR TWO-COMPONENT MODEL

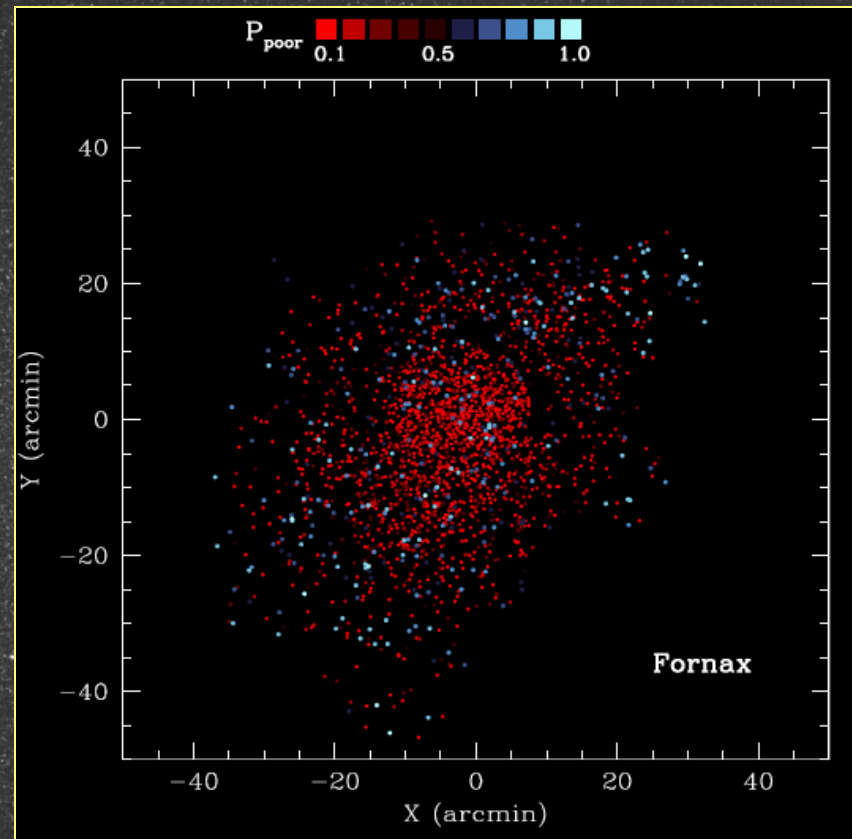
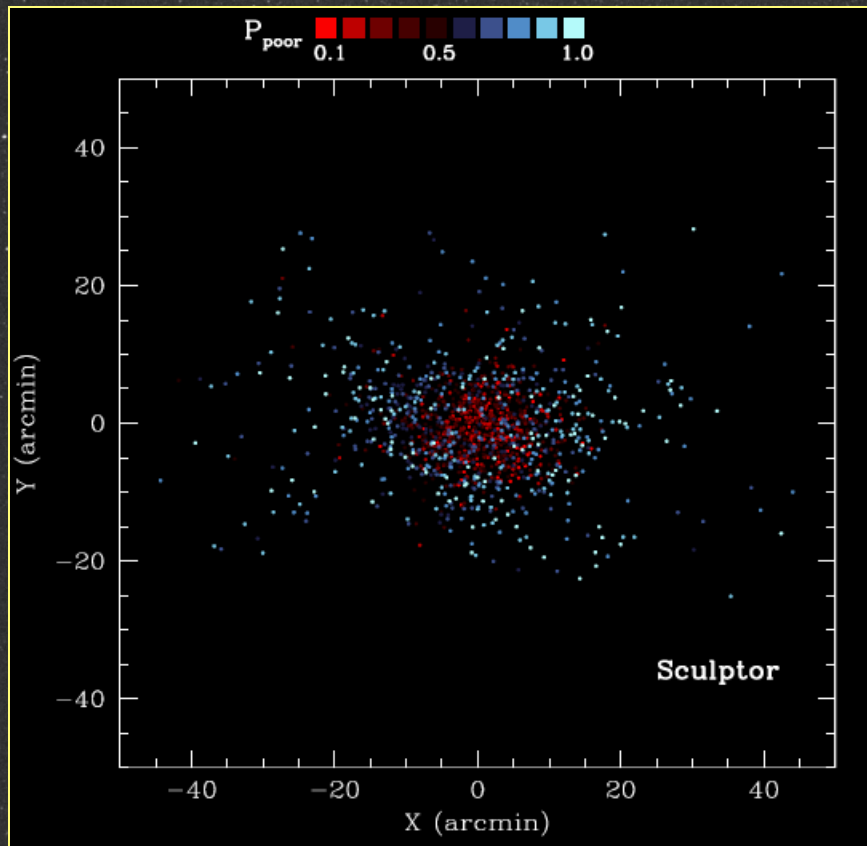
Parameter	Minimum	Maximum	Description
$f_{\text{mem}}$	0	1	$\equiv (N_1 + N_2)/(N_1 + N_2 + N_{\text{MW}})$ , fraction of stars belonging to dSph
$f_{\text{sub}}$	0	1	$\equiv N_1/(N_1 + N_2)$ , fraction of members belonging to MR component
$r_{h,1}/r_{h,2}$	0	1	ratio of half-light radii for metal-rich (MR) and metal-poor (MP) components
$\log_{10}[r_{h,2}/\text{pc}]$	0	3	half-light radius of MP component
$\langle W \rangle_1/\text{\AA}$	-3	+3	mean reduced Mg index of MR component
$(\langle W \rangle_1 - \langle W \rangle_2)/\text{\AA}$	0	3	offset of mean Mg indices
$\log_{10}[\sigma_{W,1}^2/\text{\AA}^2]$	-5	+1	squared dispersion of reduced Mg index, MR component
$\log_{10}[\sigma_{W,2}^2/\text{\AA}^2]$	-5	+1	squared dispersion of reduced Mg index, MP component
$\log_{10}[\sigma_{V,1}^2/(\text{km}^2 \text{s}^{-2})]$	-5	+5	squared velocity dispersion, MR component
$\log_{10}[\sigma_{V,2}^2/(\text{km}^2 \text{s}^{-2})]$	-5	+5	squared velocity dispersion, MP component
$\mu_{\alpha}/(\text{mas/century})$	-1000	+1000	RA proper motion of dSph
$\mu_{\delta}/(\text{mas/century})$	-1000	+1000	Dec. proper motion of dSph



# Results

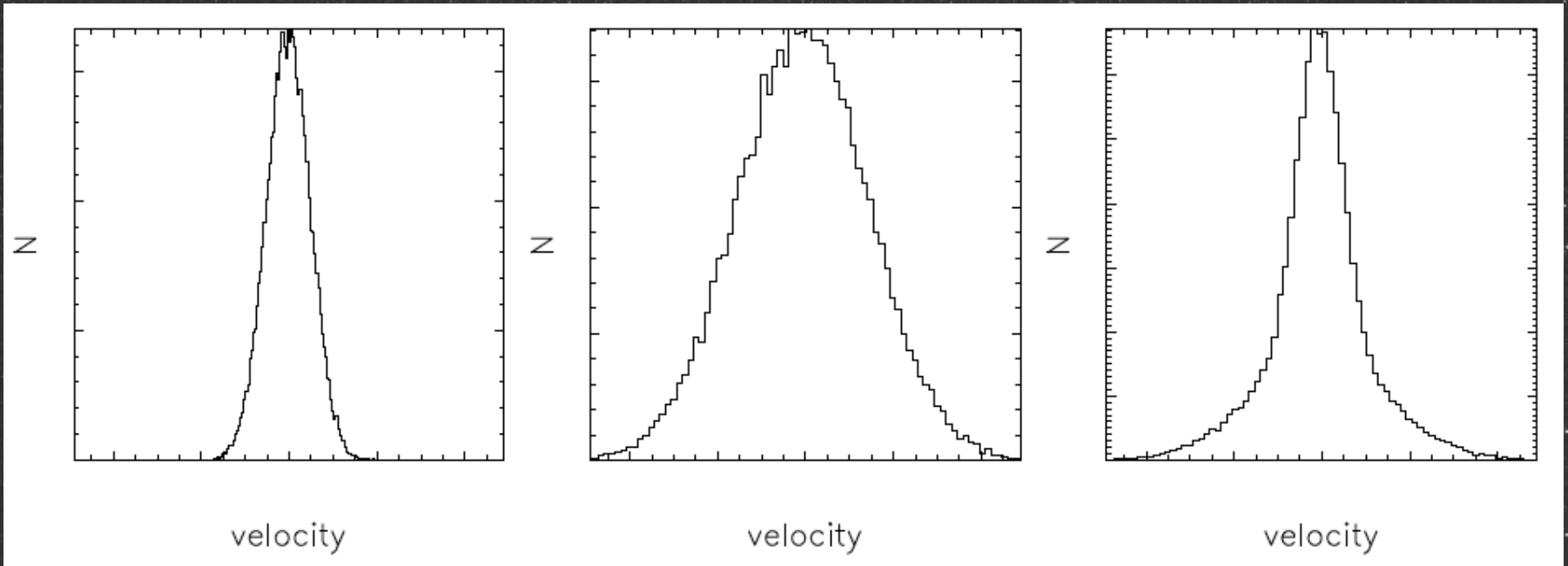


# probabilistic view of two components





# two components and line profiles





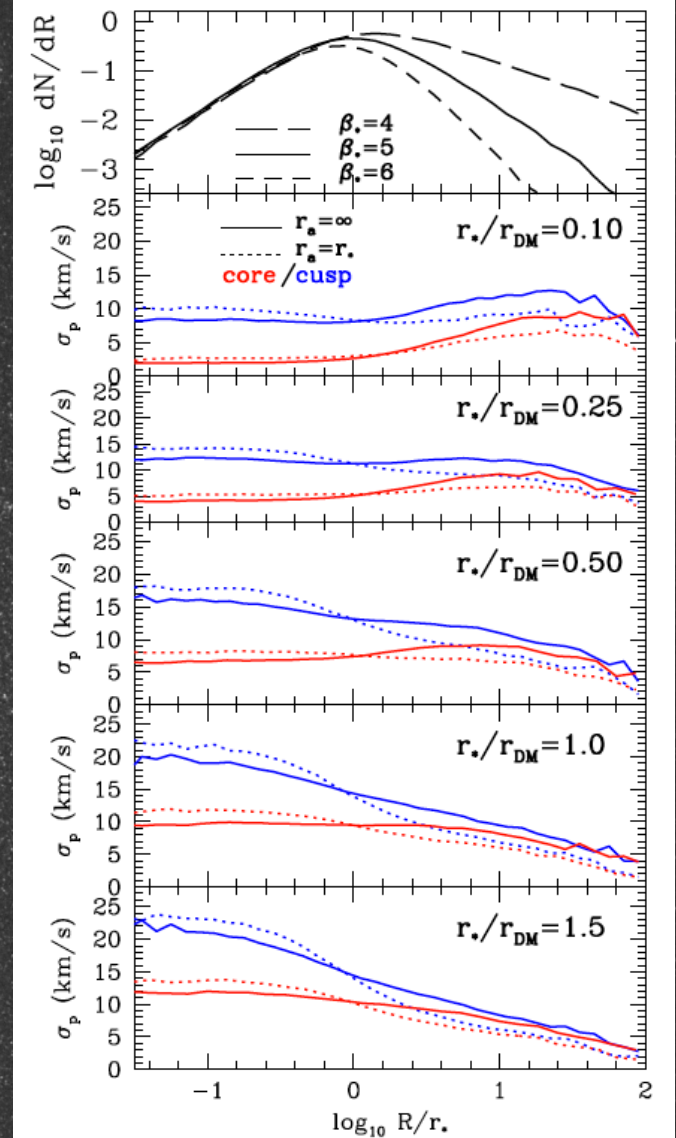
END



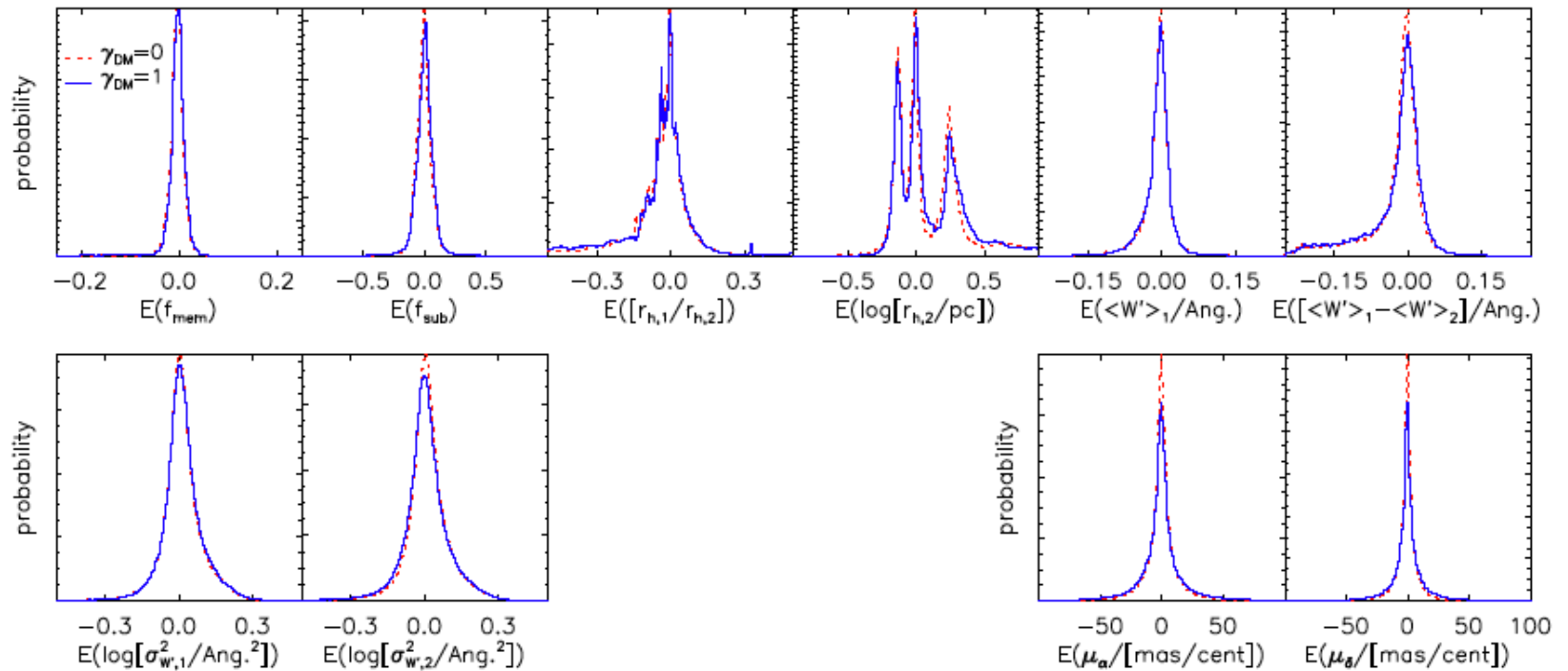
# Tests

TABLE 3  
TESTS ON SYNTHETIC DATA: GRID OF INPUT PARAMETERS FOR  
DYNAMICAL TEST MODELS

Profile	Parameter	values considered
Stellar Subcomponent (Eq. 15)		
	$r_*/r_{DM}$	0.10, 0.25, 0.50, 1.0, 1.5
	$\alpha_*$	2
	$\beta_*$	4, 5, 6
	$\gamma_*$	0.1
	$r_a/r_*$	1, $\infty$
Dark Matter Halo (Eq. 16)		
	$\rho_0/(M_\odot \text{pc}^{-3})$	0.064
	$r_{DM}/\text{kpc}$	1
	$\alpha_{DM}$	1
	$\beta_{DM}$	3
	$\gamma_{DM}$	0, 1

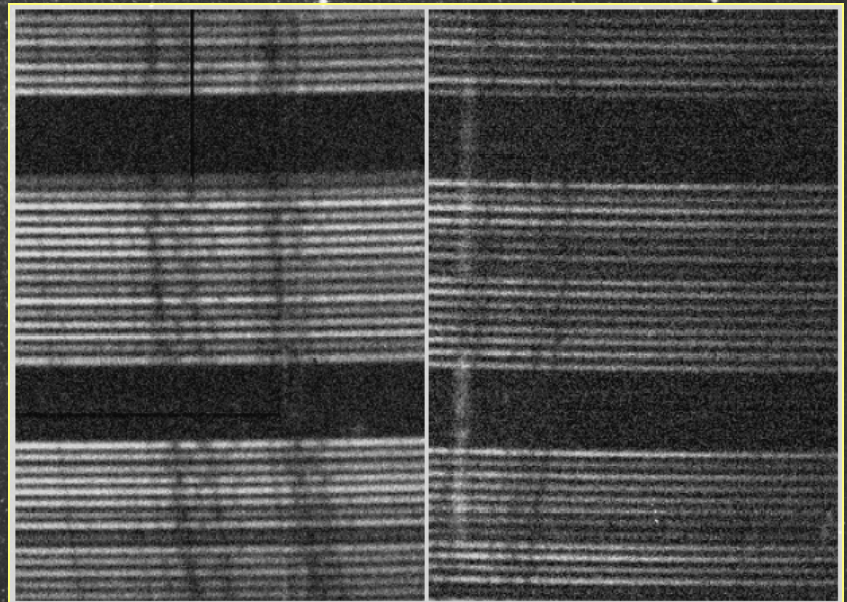
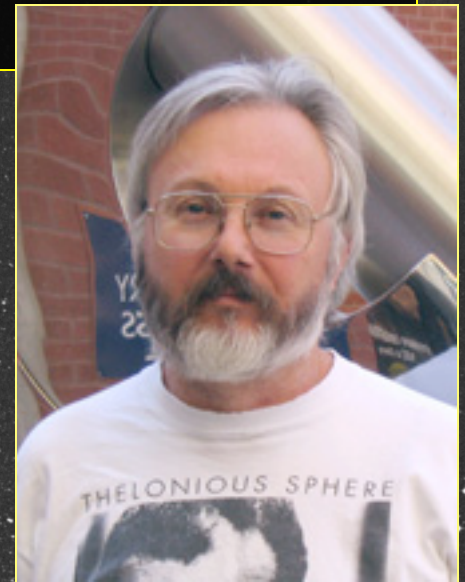
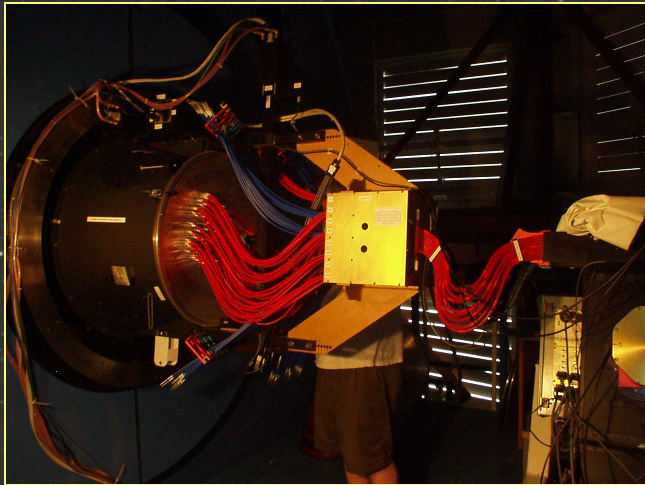


# Errors—parameter estimates





# Magellan Spectroscopic Observations w/ Mario Mateo & Ed Olszewski

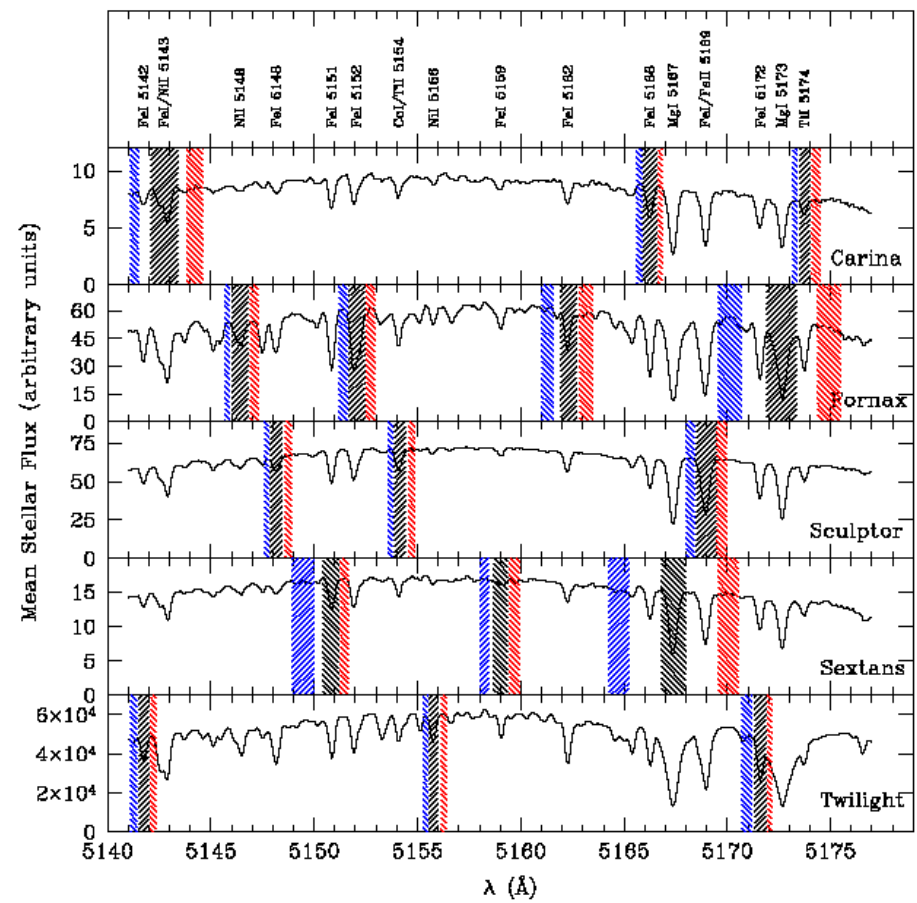
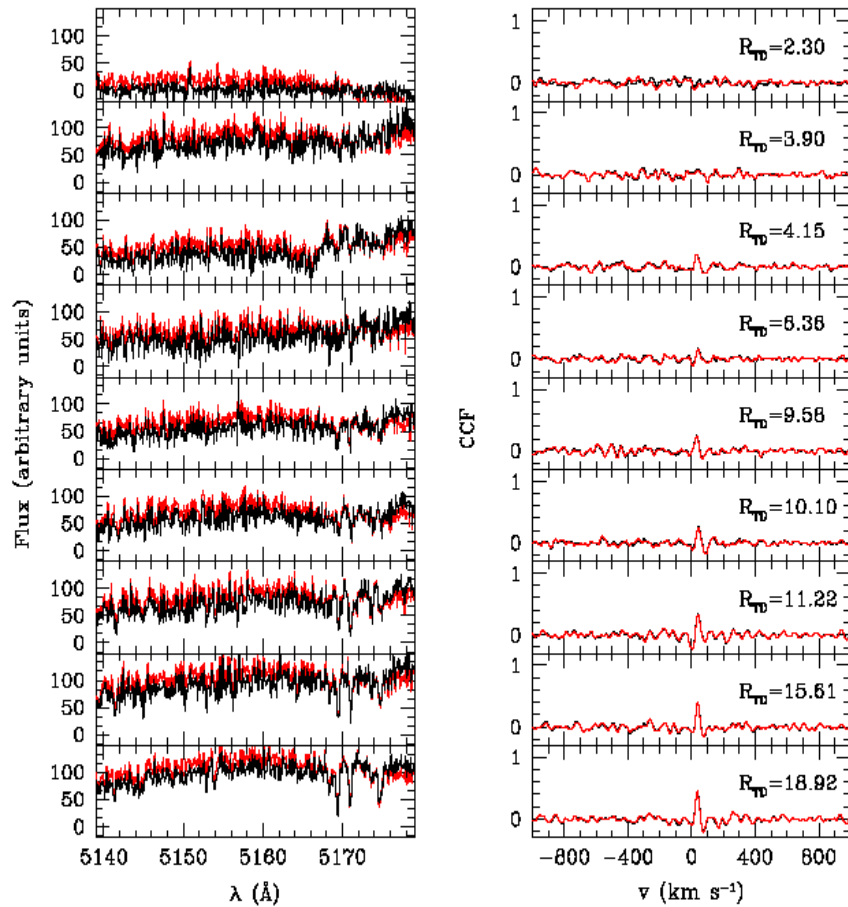




# Observations: Spectroscopy of “Classical” dSphs

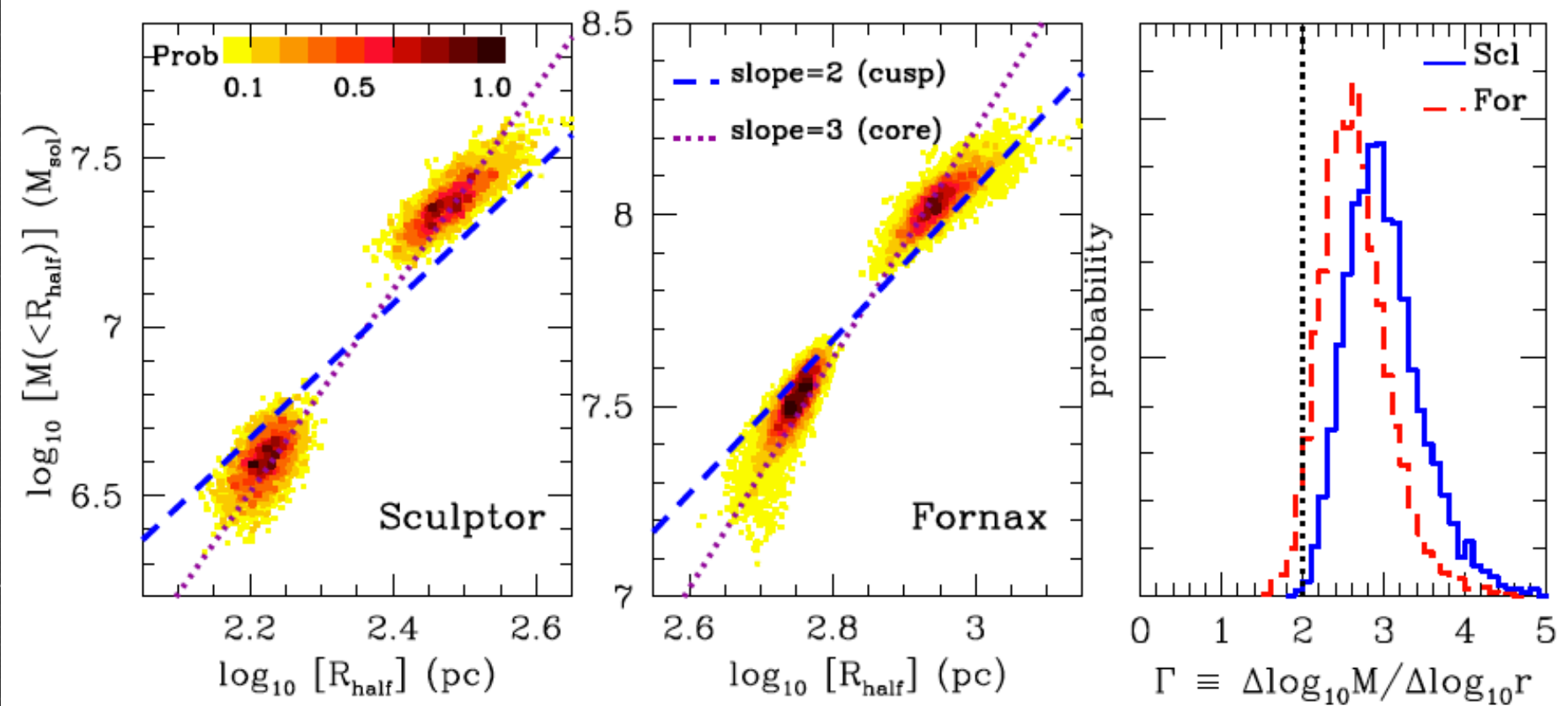
$$CCF(v) = \int S(v)[T(v) - v] dv$$

$$W = \int_{\lambda_1}^{\lambda_2} [1 - S(\lambda)/C(\lambda)] d\lambda$$





# Results



$$\Gamma \equiv \frac{\Delta \log M}{\Delta \log r} = \frac{\log[M(r_{h,2})/M(r_{h,1})]}{\log[r_{h,2}/r_{h,1}]} \approx 1 + \frac{\log[\sigma_{V,2}^2/\sigma_{V,1}^2]}{\log[r_{h,2}/r_{h,1}]}$$