

Sternentstehung - Star Formation

Winter term 2024/2025

Henrik Beuther, Thomas Henning & Caroline Gieser

15.10 Today: Introduction & Overview	(Beuther)
22.10 Physical processes I	(Beuther)
29.10 --	
05.11 Physical processes II	(Beuther)
12.11 Molecular clouds as birth places of stars	(Beuther)
19.11 Molecular clouds (cont.), Jeans Analysis	(Henning)
26.11 Collapse models I	(Beuther)
03.12 Collapse models II	(Beuther)
10.12 Protostellar evolution	(Gieser)
17.12 Pre-main sequence evolution & outflows/jets	(Henning)
07.01 Accretion disks I	(Henning)
14.01 Accretion disks II	(Henning)
21.01 High-mass star formation, clusters and the IMF	(Gieser)
28.01 Extragalactic star formation	(Henning)
04.02 Planetarium@HdA, outlook, questions	
11.02 Examination week, no star formation lecture	(Beuther, Gieser, Henning)

Book: Stahler & Palla: The Formation of Stars, Wileys

More Information and the current lecture files: http://www.mpia.de/homes/beuther/lecture_ws2425.html
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Last Week

- Main tools: Spectral line emission, and thermal emission and extinction from dust.

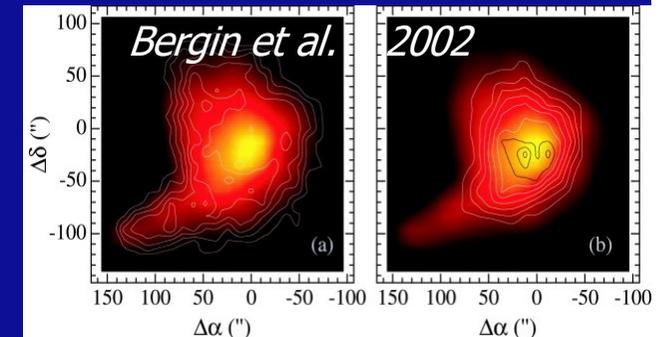
- Molecules interesting for themselves and chemistry.



- However, also extremely useful to trace physical processes.

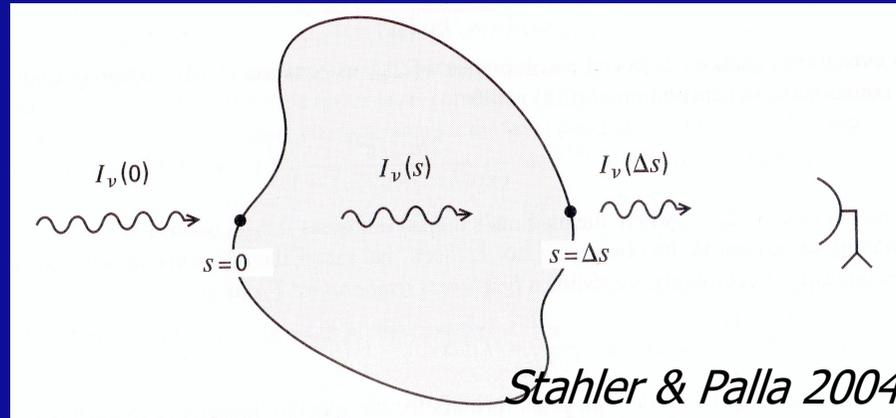
- Molecules deplete on grains at low temperatures.

- Discussed main cooling and heating processes.



- Discussed basic line radiation transfer and column density determination.

Radiation transfer I



$$dI_\nu = -\kappa_\nu I_{\nu,0} ds + \varepsilon_\nu ds$$

with the opacity

$$d\tau_\nu = -\kappa_\nu ds$$

and the source function

$$S_\nu = \varepsilon_\nu / \kappa_\nu$$

$$\Rightarrow dI_\nu / d\tau_\nu = I_{\nu,0} - S_\nu$$

Assuming a spatially constant source function \rightarrow radiation transfer equation

$$\Rightarrow I_\nu = S_\nu (1 - e^{-\tau(\nu)}) + I_{\nu,0} e^{-\tau(\nu)}$$

κ : absorption coef.
 ε : emission coef.

Radiation transfer II

The excitation temperature T_{ex} is defined via a Boltzmann distribution as

$$n_J/n_{J-1} = g_J/g_{J-1} \exp(-h\nu/kT_{\text{ex}})$$

with n_J and g_J the number density and statistical weights.

In case of rotational transitions

$$g_J = 2J + 1$$

J: rot. quantum
number

In thermal equilibrium

$$T_{\text{ex}} = T_{\text{kin}}$$

In a uniform molecular cloud the source function S_ν equals Planck function

$$S_\nu = B_\nu(T_{\text{ex}}) = 2h\nu^3/c^2 (\exp(h\nu/kT_{\text{ex}}) - 1)^{-1}$$

Radiation transfer III

Then the radiation transfer equation

$$\Rightarrow I_\nu = B_\nu(T_{\text{ex}}) (1 - e^{-\tau(\nu)}) + I_{\nu,0} e^{-\tau(\nu)}$$

In the Rayleigh-Jeans limits ($h\nu \ll kT$) B equals

$$B = (2k\nu^2/c^2) T \quad (\text{def.} \rightarrow T = c^2/(2k\nu^2) I_\nu)$$

And the radiation transfer equation using now the radiation temperature is

$$T_r = J_\nu(T_{\text{ex}}) (1 - e^{-\tau(\nu)}) + J_{\nu,0}(T_{\text{bg}}) e^{-\tau(\nu)}$$

with

$$J_\nu = h\nu/k (\exp(h\nu/kT) - 1)^{-1}$$

Molecular column densities I

To derive molecular column densities, 3 quantities are important:

- 1) Intensity T of the line
- 2) Optical depth τ of the line (observe isotopologues or hyperfine structure)
- 3) Partition function Q

The optical depth τ of a molecular transition can be expressed like

$$\tau = c^2/8\pi\nu^2 A_{ul}N_u (\exp(h\nu/kT) - 1) \phi$$

with the Einstein A_{ul} coefficient

$$A_{ul} = 64\pi^4\nu^3/(3c^3h) \mu^2 J_u/(2J_u-1)$$

and the line form function ϕ

$$\phi = c/\nu 2\text{sqrt}(\ln 2)/(\text{sqrt}(\pi)\Delta\nu)$$

Molecular column densities II

Using furthermore the radiation transfer eq. ignoring the background

$$T = J_\nu(T_{\text{ex}}) \tau (1 - e^{-\tau}) / \tau$$

And solving τ -equation for N_u , one gets

$$N_u = \frac{3k}{8\pi^3 \nu} \frac{1}{\mu^2} \frac{(2J_u - 1)}{J_u} \tau / (1 - e^{-\tau}) \left(T \Delta \nu \frac{\sqrt{\pi}}{2\sqrt{\ln 2}} \right)$$

The last expression equals the integral $\int T dv$.

$$\rightarrow N_u \sim \tau / (1 - e^{-\tau}) \int T dv$$

The column density in the upper level N_u relates to the total column density N_{tot}

$$N_{\text{tot}} = N_u / g_u \exp(E_u / kT) Q$$

For linear molecule like CO, partition function Q approximated: $Q = kT/hB$.
(B : rotational constant)

However, for more complex molecules Q can become very complicated.

Conversion from CO to H₂ column densities

Classical way to derive conversion factors from CO to H₂ column densities:

- 1) Derive ratio between colour excess E_{B-V} and optical extinction A_V
$$A_V = 3.1 E_{B-V} \quad (\text{Savage and Mathis, 1979})$$
 - 2) The ratio $N(\text{H}_2)/E_{B-V}$: One can measure the H₂ column density, e.g., directly from UV Absorption lines.
 - 3) The ratio $N(\text{CO})/A_V$: In regions of molecular gas emission, one can estimate A_V by star counts in the Infrared regime
- ⇒ Combining these three ratios: CO → H₂ column densities.

Topics today

- Line profiles and a few applications for line emission
- Magnetic field measurements (Zeeman and dust)
- Maser emission
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

Line broadening

- Natural line broadening: Disturbance of molecule by zero-point vibrations of electromagnetic field

$$d\nu = 32\pi^3\nu^3 \mu^2 / (3hc^3) \quad (\mu: \text{Dipole moment})$$

For CO(1-0) $\rightarrow d\nu \sim 3.5 \times 10^{-8}$ Hz or $d\nu \sim 9 \times 10^{-14}$ km/s \rightarrow Negligible!

- Pressure broadening: Arises from collisions between molecules.
Quantum-mechanical problem of intermolecular forces.
 \rightarrow At densities of star-forming regions negligible.

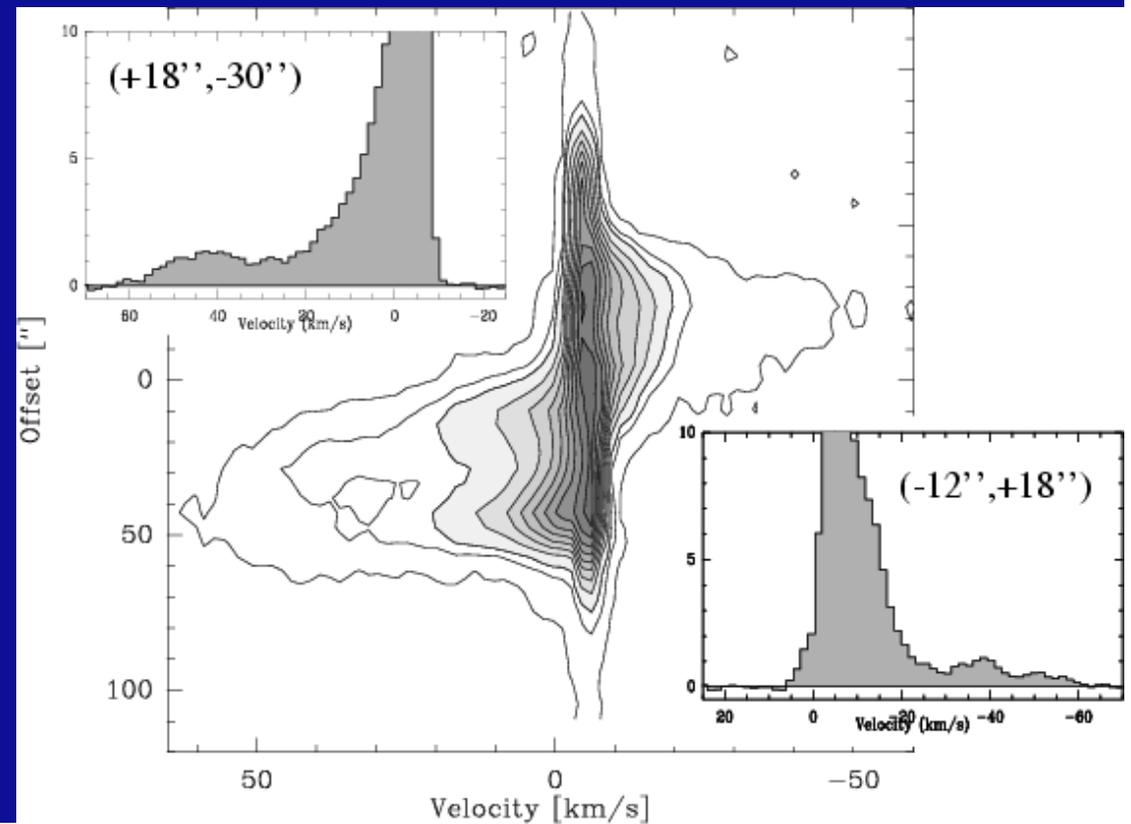
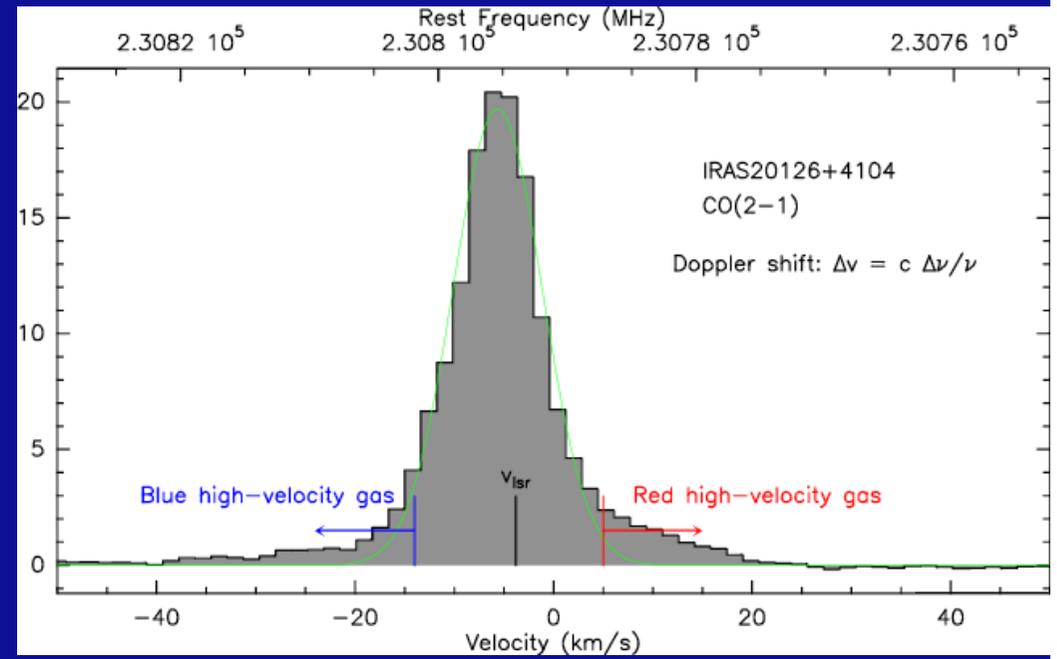
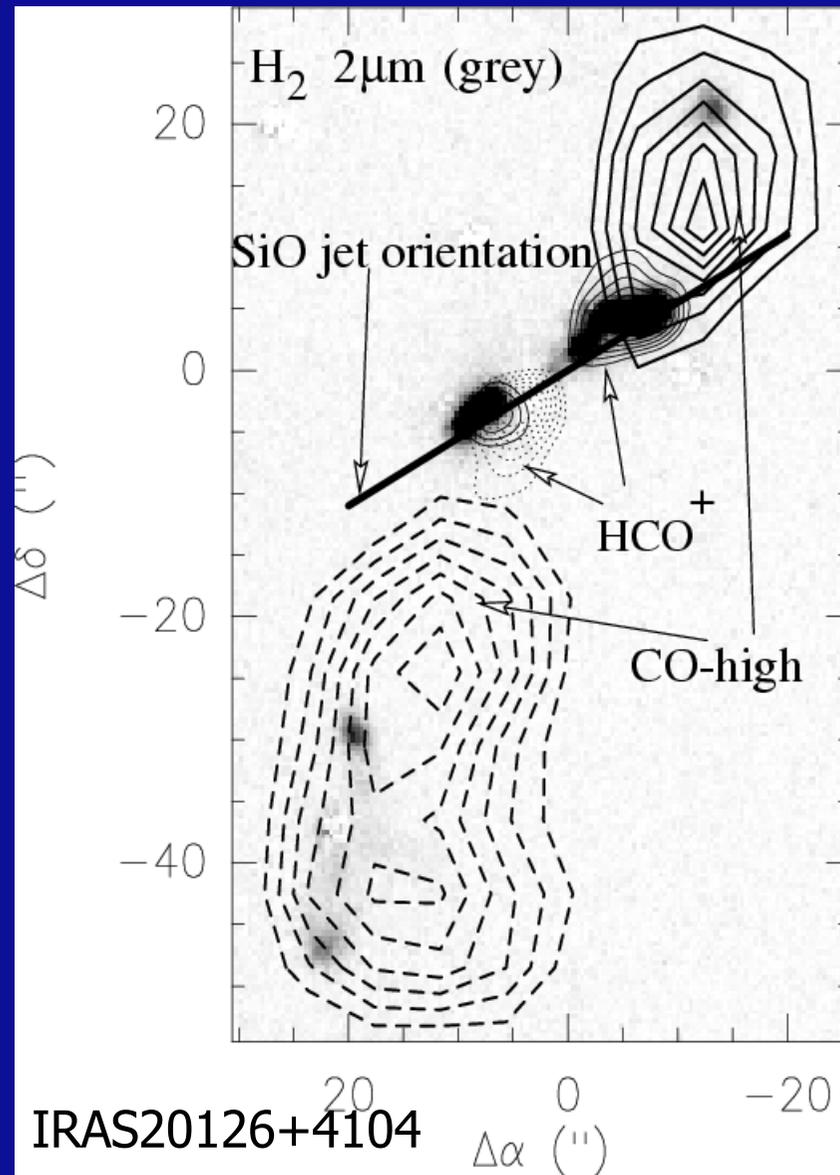
- Thermal line broadening: Thermal motions of gas cause doppler broadening:

$$d\nu = \sqrt{(8 \ln 2) kT / m_{\text{mol}}}$$

$$\rightarrow d\nu(\text{NH}_3 @ 30\text{K}) \sim 0.28 \text{ km/s}$$

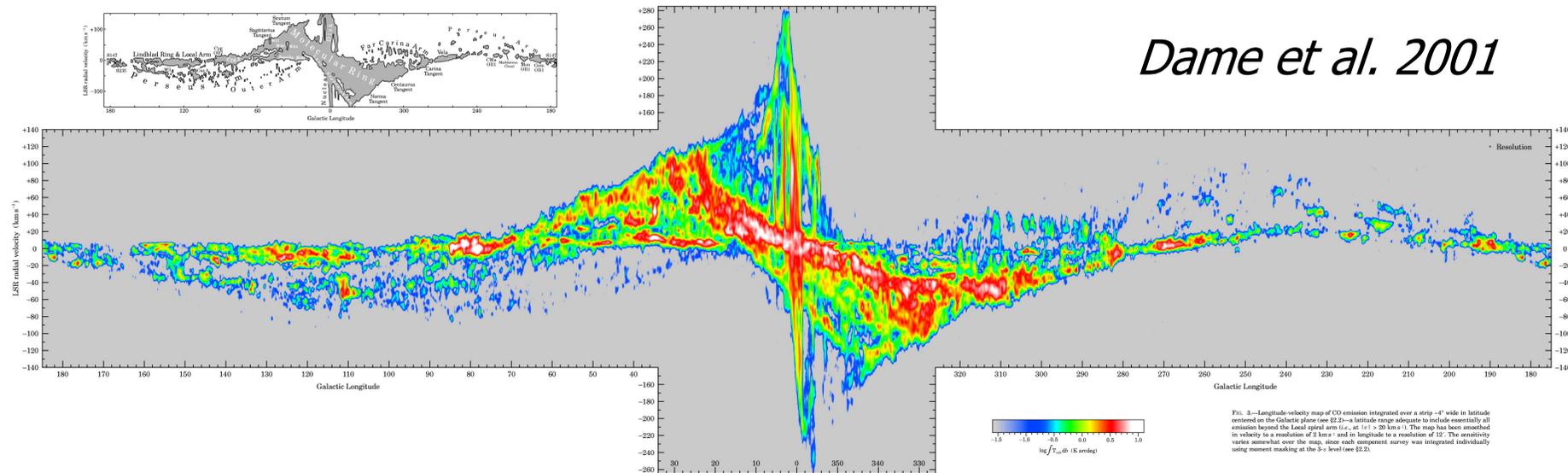
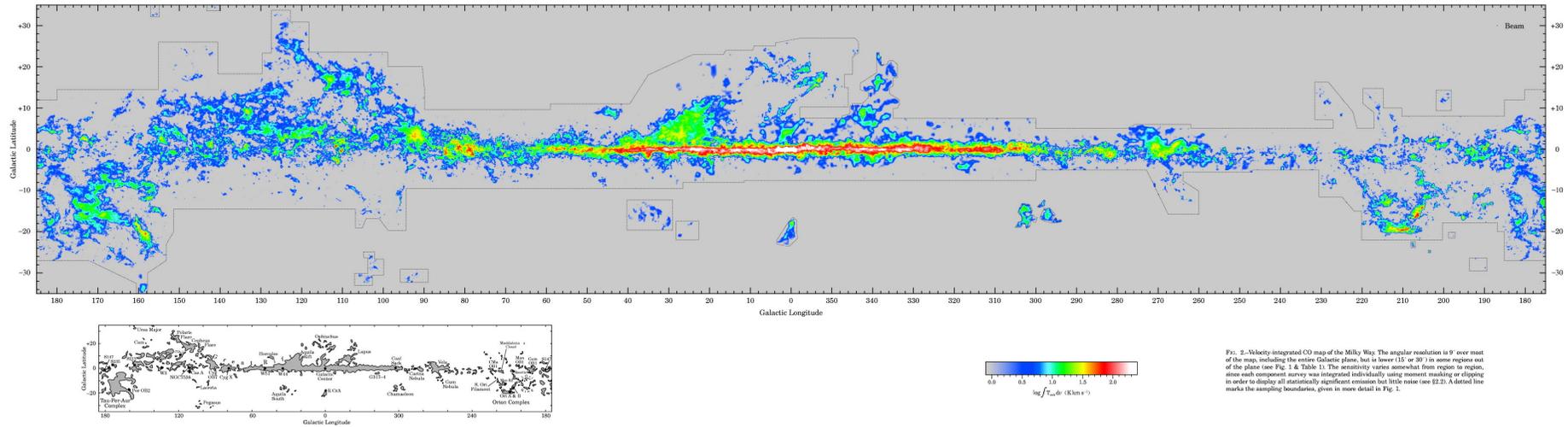
\rightarrow Other physical effects: Line broadening due to outflow motions, rotation ...

Molecular outflows



Lebron et al. 2006

Molecular gas structure of the Galaxy based on CO observations

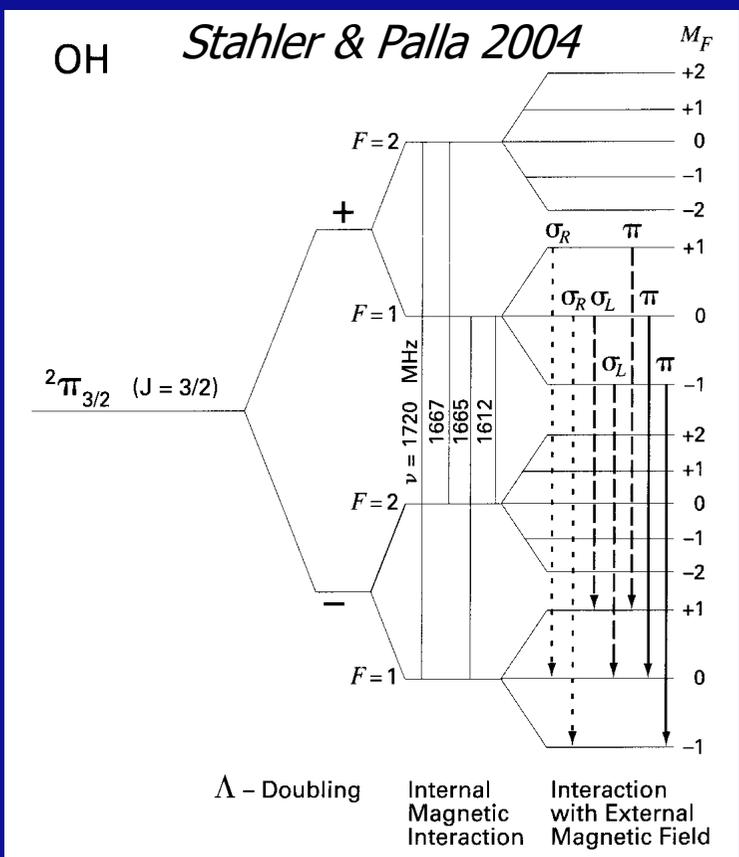
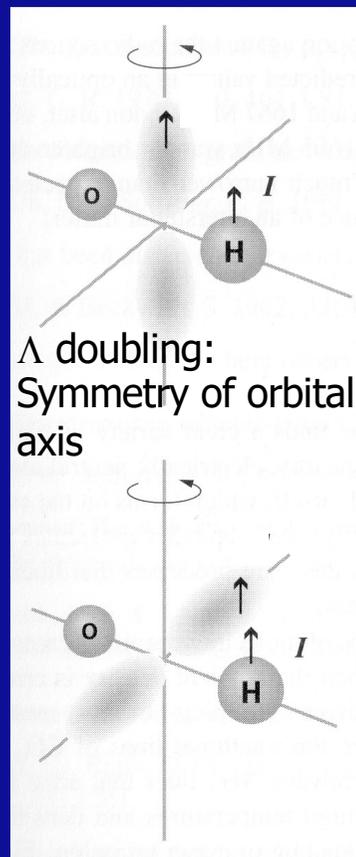
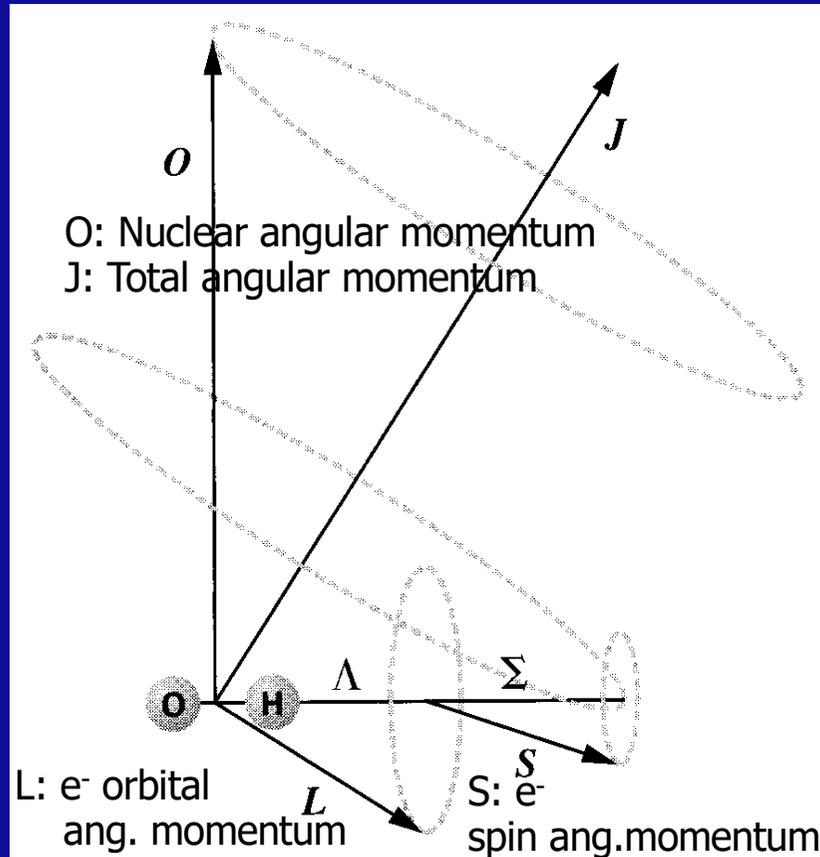


Dame et al. 2001

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- Magnetic field measurements (Zeeman and dust)
- Maser emission
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

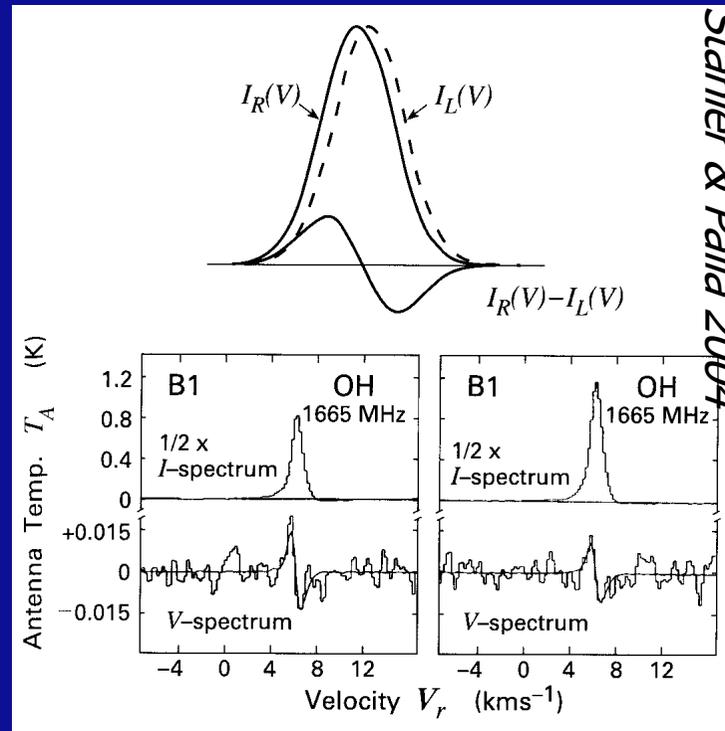
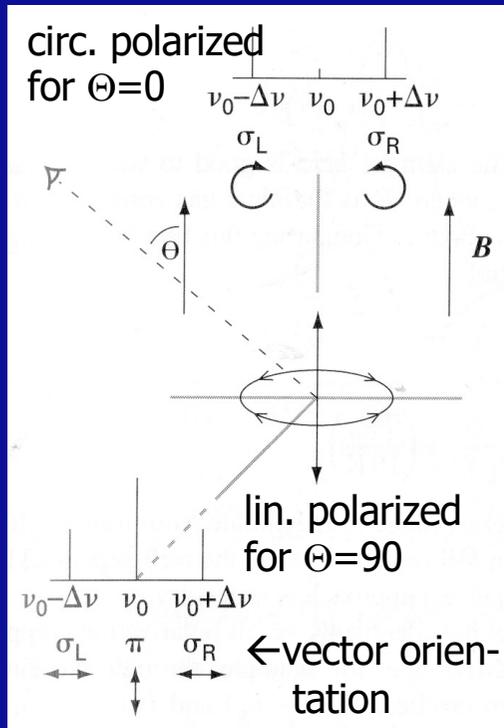
The Zeeman effect and magnetic fields I



- OH free radical with unpaired free e⁻ and hence non-zero electronic angular momentum. Highly reactive in lab, but can survive in space.
- Λ doubling \rightarrow symmetry difference of the e⁻ orbital to rotation axis \rightarrow energy splitting.
- Interaction between spins of e⁻ and H nucleus \rightarrow magn. hyperfine splitting.

External magnetic field \rightarrow produces Zeeman splitting.

The Zeeman effect and magnetic fields II

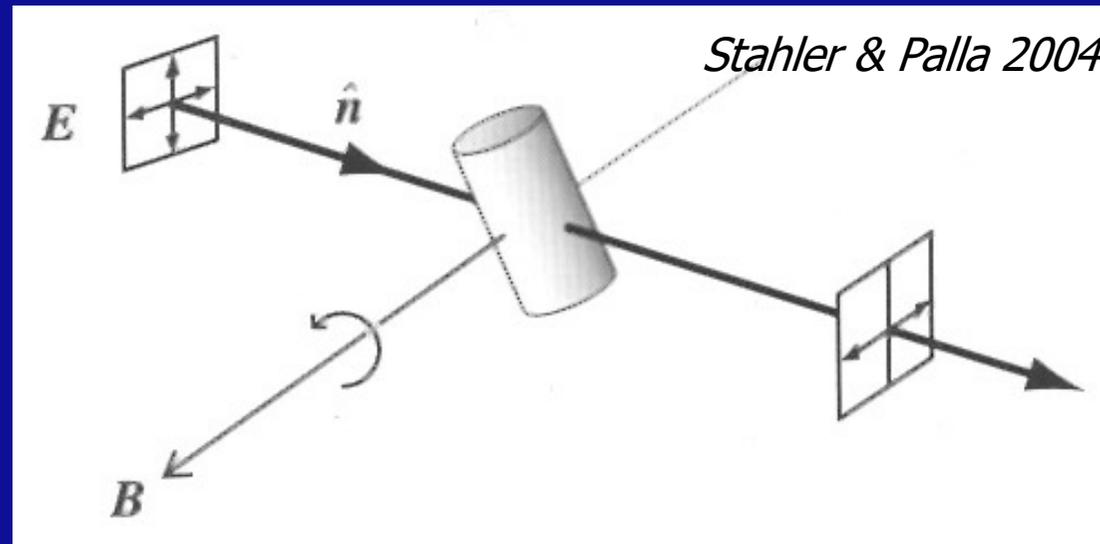


$\Delta v_{\text{mag}} \sim B$
usually of the order a few $10 \mu\text{G}$

← Subtraction of left- from right-handed circ. pol. results in Stokes-V spec.

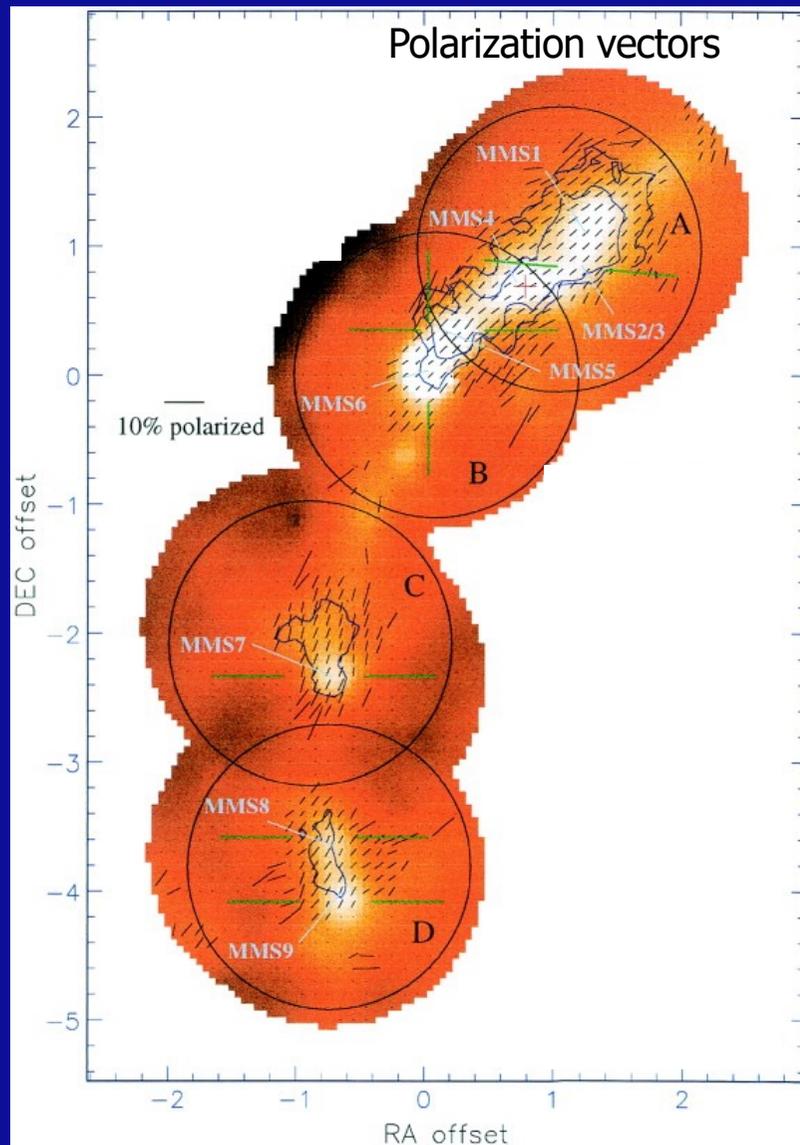
- Zeeman splitting of $\Delta v_{\text{mag}} = (b/2) B$ (b: constant, B: Magnetic field)
- Orientation between \mathbf{B} and line of sight causes different polarization properties
→ $\Theta=0$ (l.o.s) circular pol., $\Theta=90$ lin. pol., in reality elliptical polarization.
- Thermal line broadening complicates matter: $\Delta v_{\text{mag}} / \Delta v_{\text{therm}} \sim 10^{-3} B (\mu\text{G})$
 - One measures two polarizations differentially.
 - Only sensitive to the B component along the line of sight.

IR dust polarization & dichroic extinction



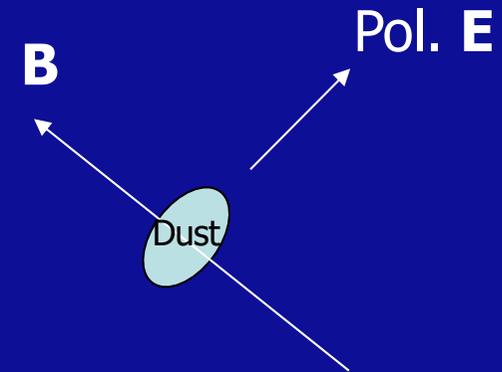
- Incident radiation unpolarized.
- Grains not spheres \rightarrow small electric charge and paramagnetic
 \rightarrow rotate about short axis, and magn. moment \mathbf{M} points along rotation axis.
- External \mathbf{B} field creates torque $\mathbf{D}=\mathbf{M}\times\mathbf{B}$ \rightarrow grain's short axis aligns with \mathbf{B} .
- Absorption best along major axis
 \rightarrow Polarization afterwards largely along axis of magn. field.

Dust polarization and magnetic fields



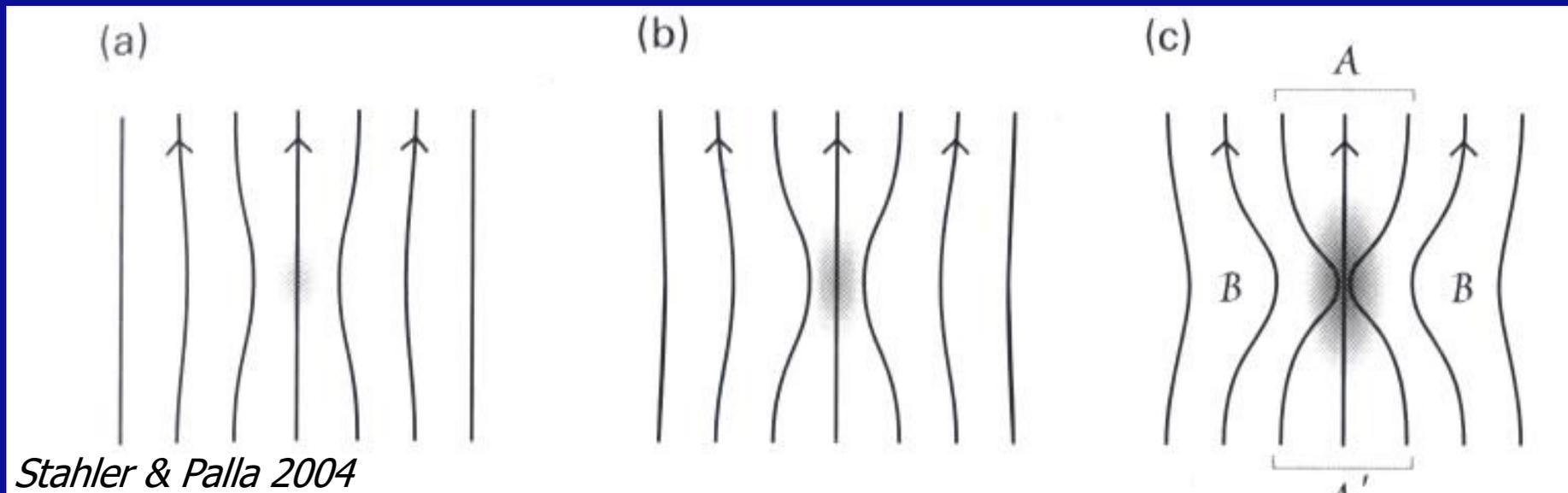
Polarized submm continuum emission

In contrast, thermal dust emission at (sub)mm wavelengths perpendicular to magnetic field!

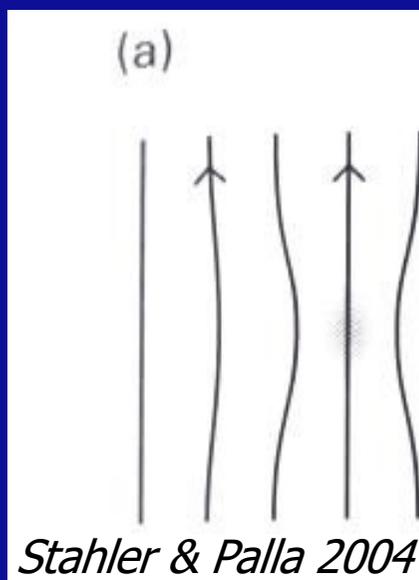


Molecular filaments can collapse along their magnetic field lines.

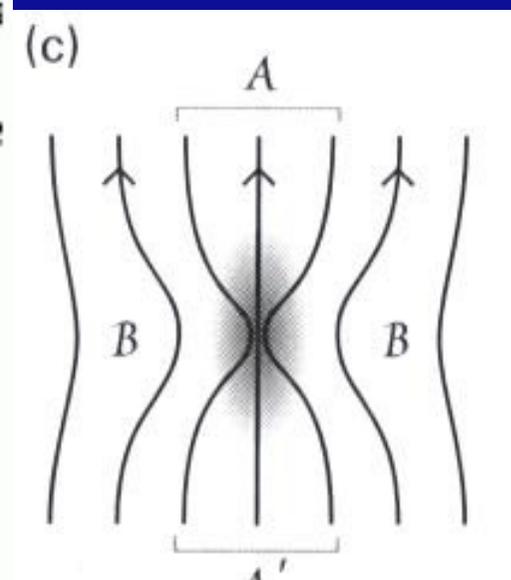
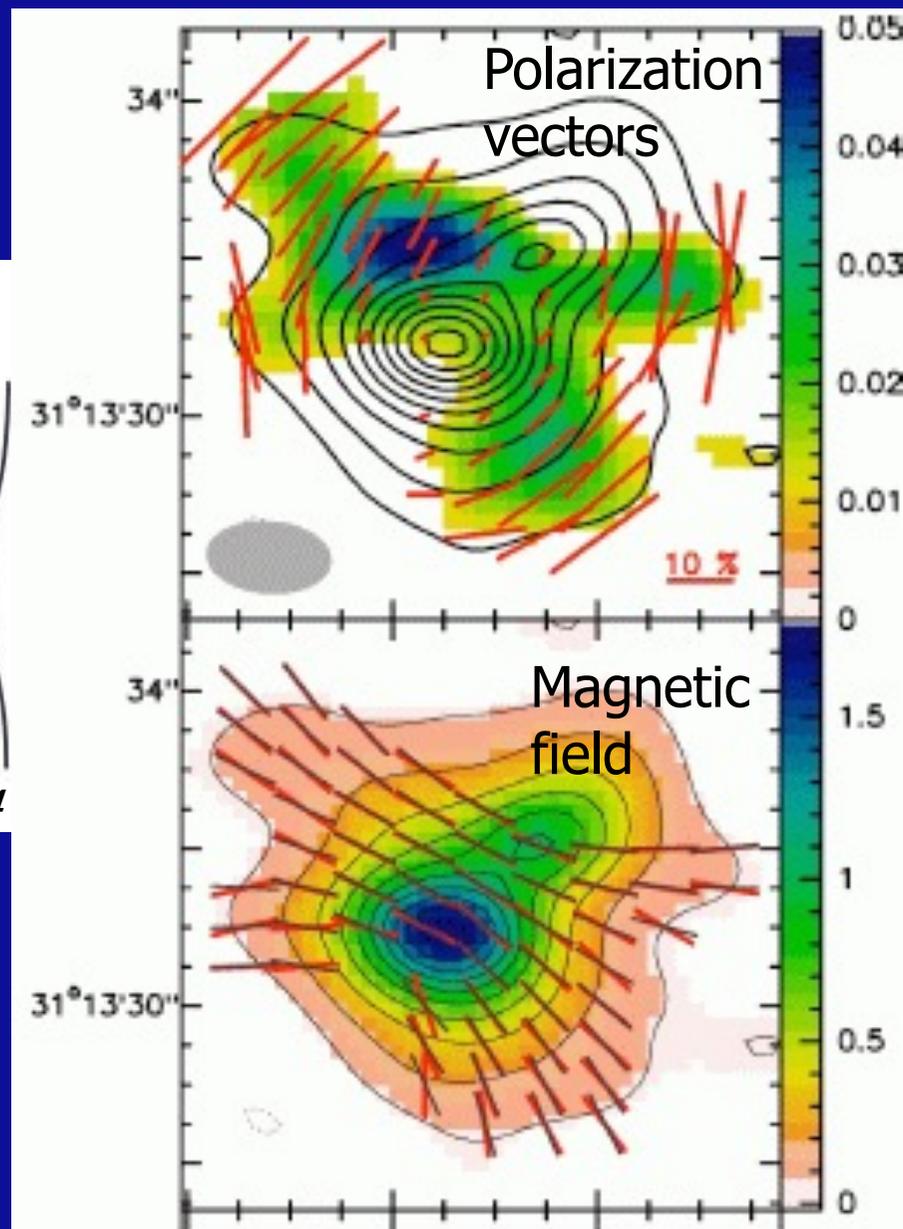
Ambipolar diffusion



Ambipolar diffusion



$B_{\text{pos}} \sim 5\text{mG}$

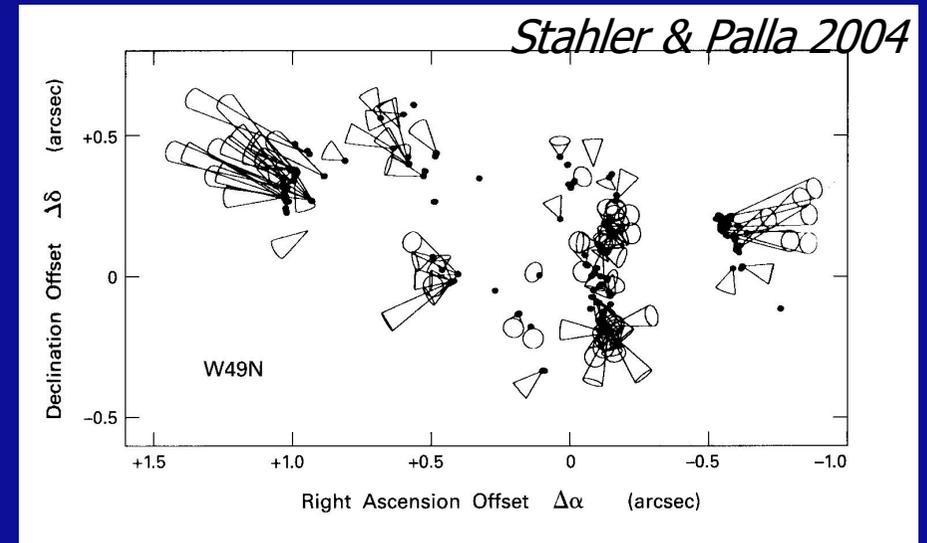
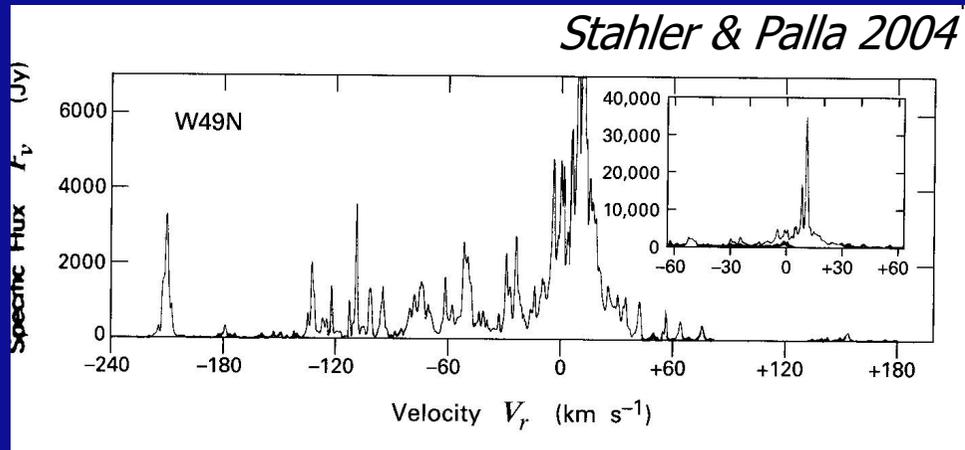


Girart et al. 2006

Topics today

- Line profiles and a few applications for line emission
- Magnetic field measurements (Zeeman and dust)
- **Maser emission**
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

Molecular Masers I

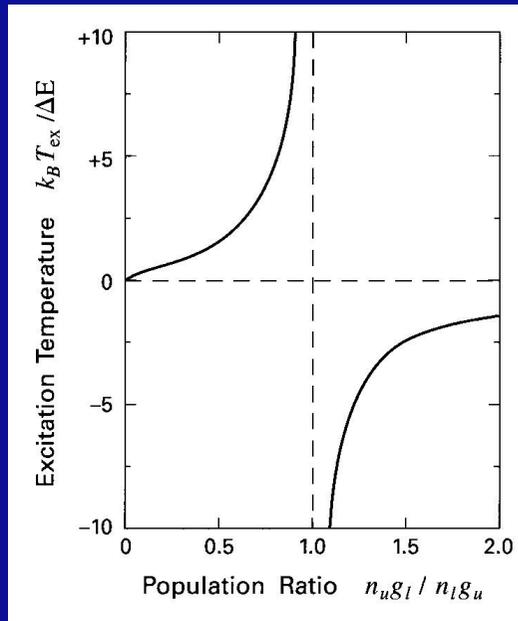


- Rayleigh-Jeans limit: $T = c^2/2k\nu^2I$ with $I=F/\Omega$ (Ω : solid angle).
- Small spot diameters (\sim some AU) \rightarrow T as high as 10^{15}K
 \rightarrow no thermal equilibrium and no Boltzmann distribution.
- Narrow line-width with potential broad velocity distribution (many components).
- They allow to study proper motions.

Molecular Masers II

- Excitation temperature for Boltzmann: $n_u/n_l = g_u/g_l \exp(-h\nu/kT_{\text{ex}})$.
- Maser activity requires population inversion: $n_u/g_u > n_l/g_l$.
 - Negative excitation temperatures
- In thermal conditions at a few 100K, for typical microwave lines $E_{\text{line}} = h\nu/k < T_{\text{kin}} \sim T_{\text{ex}} \rightarrow n_u/g_u \sim n_l/g_l$
 - Only a relatively small shift is required in get population inversion

Stahler & Palla 2004



$$T_{\text{ex}}/E_{\text{line}} = -1/\ln(n_u g_l / n_l g_u)$$

Rising T_{ex}

- Level populations approach each other
- Only "overcome the border".

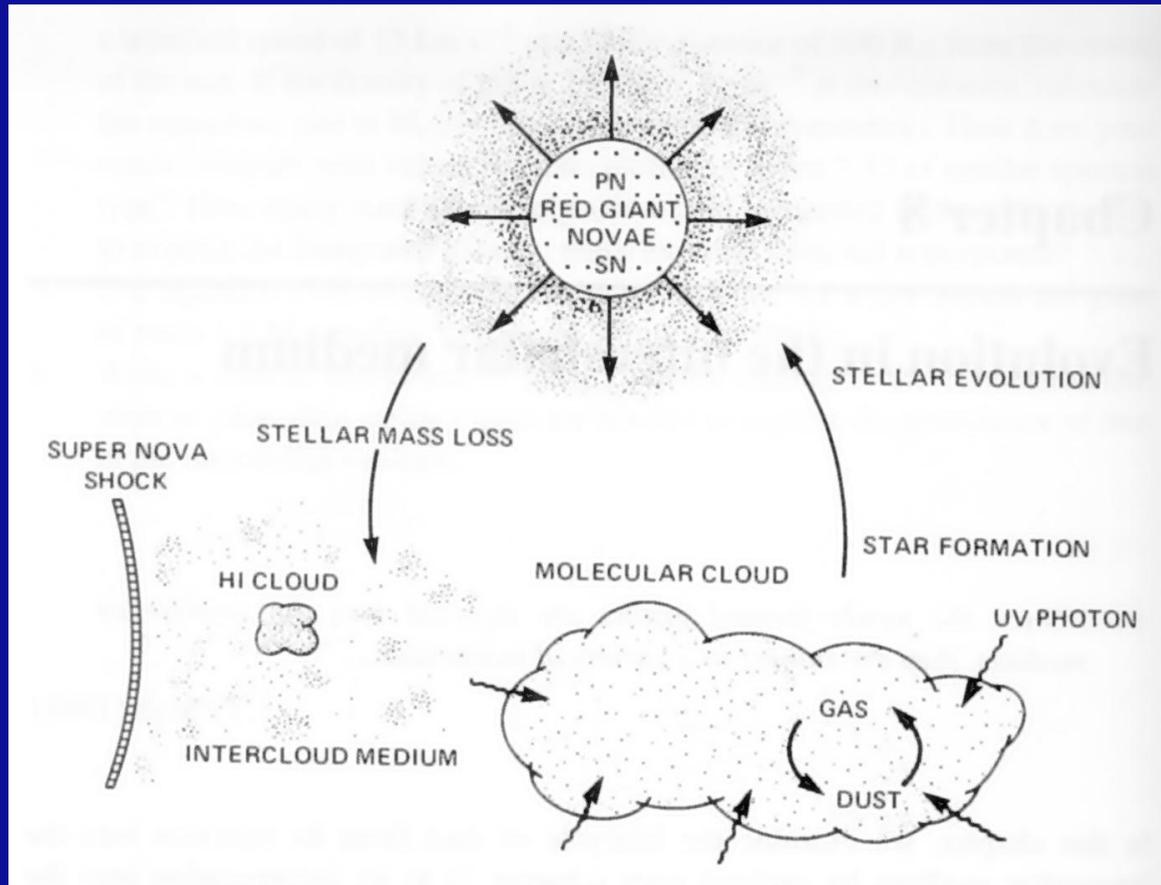
Pumping mechanisms, e.g.:

- Collisional pumping in shocks of protostellar jets for H₂O masers.
- Radiative pumping in shocks or from protostars (e.g., CH₃OH masers)
 - In both cases, very high densities and temperatures required.

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- Magnetic field measurements (Zeeman and dust)
- Maser emission
- **Dust properties**
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

Dust within the big circle of matter



Dust composition:

Graphite/carbon	C
Silicon carbide	SiC
Enstatite	(Fe,Mg)SiO ₃
Olivine	(Fe,Mg) ₂ SiO ₄
Iron	Fe
Magnetite	Fe ₃ O ₄

Size distribution:

Between 0.005 and 1 μ m
 $n(a) \sim a^{-3.5}$ (a: size)
(Mathis, Rumpl, Nordsieck 1977)

Gas to dust mass ratio:

Canonical 1:100

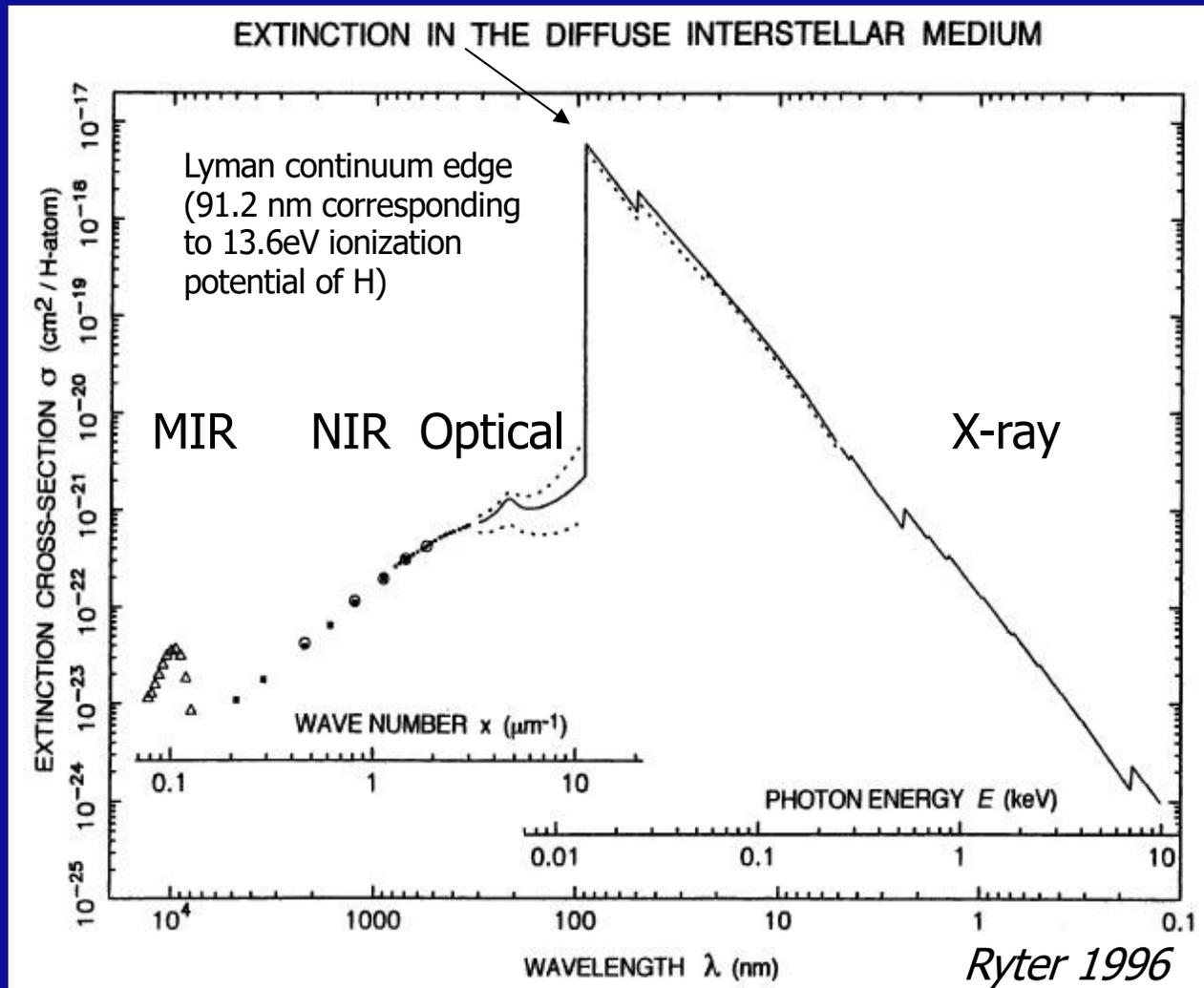
Recent work suggests

1:150 (Draine et al. 2011)

Producers:

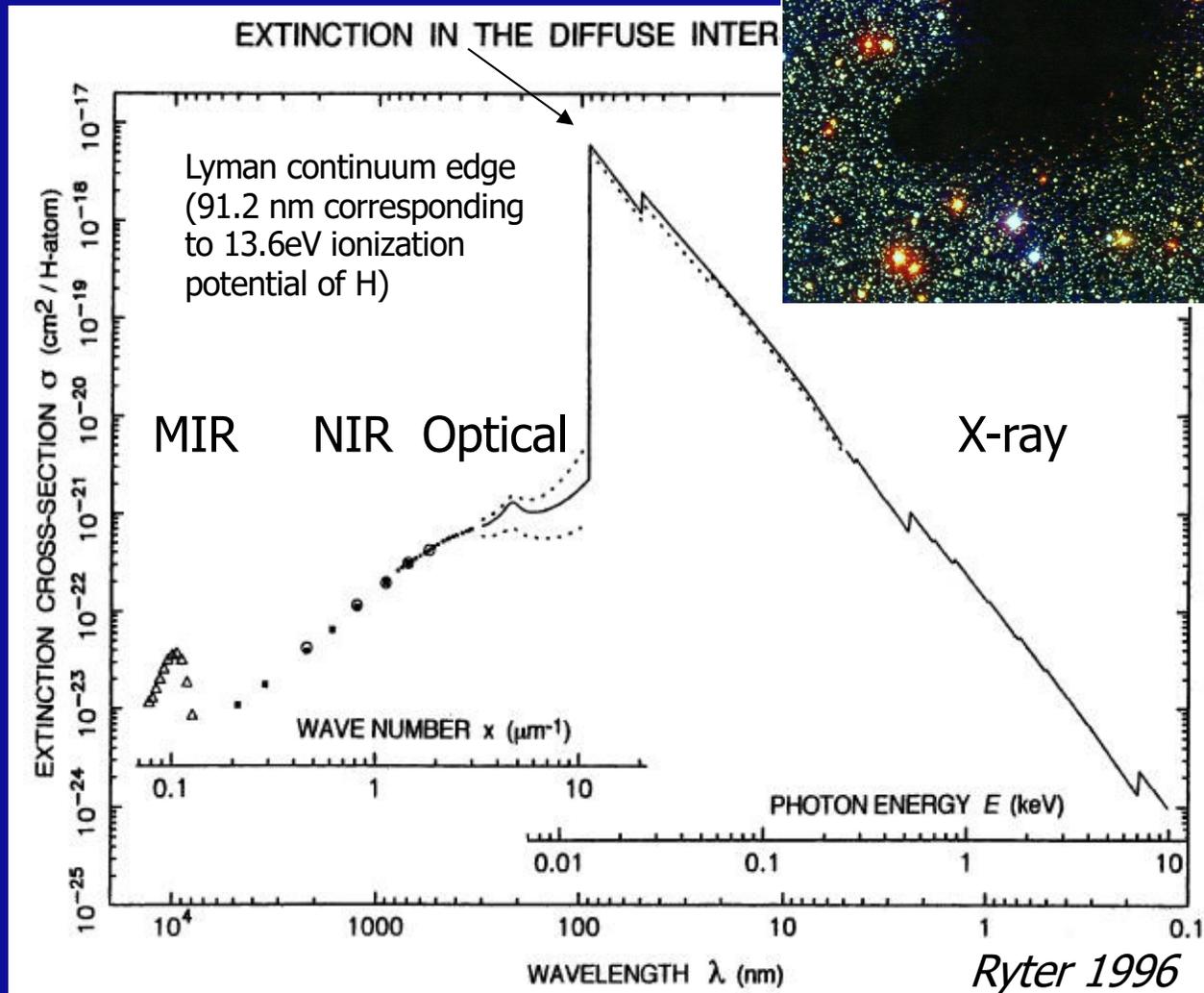
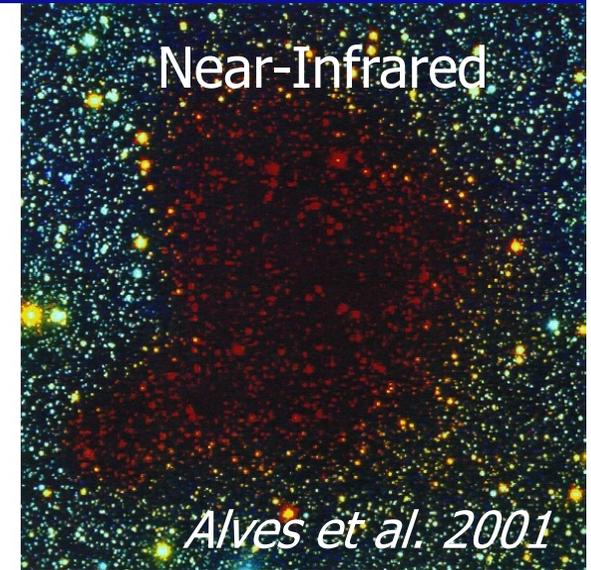
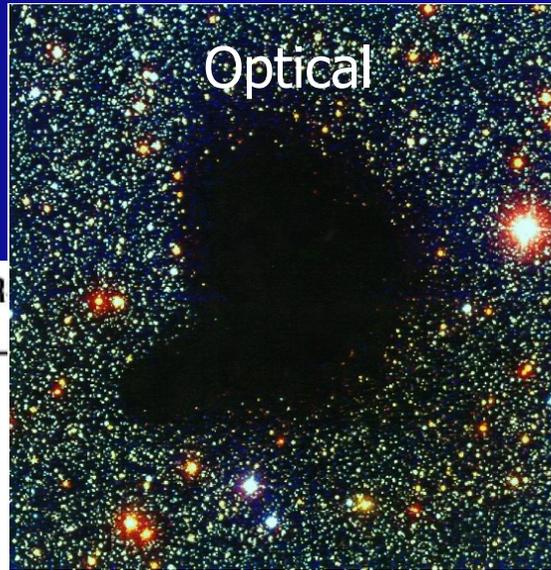
- Outer atmosph. of Red Giants, Planetary Nebulae (PN)
- Supernovae (SN)
- More recent: Dust can also form in the general interstellar medium (ISM).

Interstellar dust: Extinction at shorter wavelengths



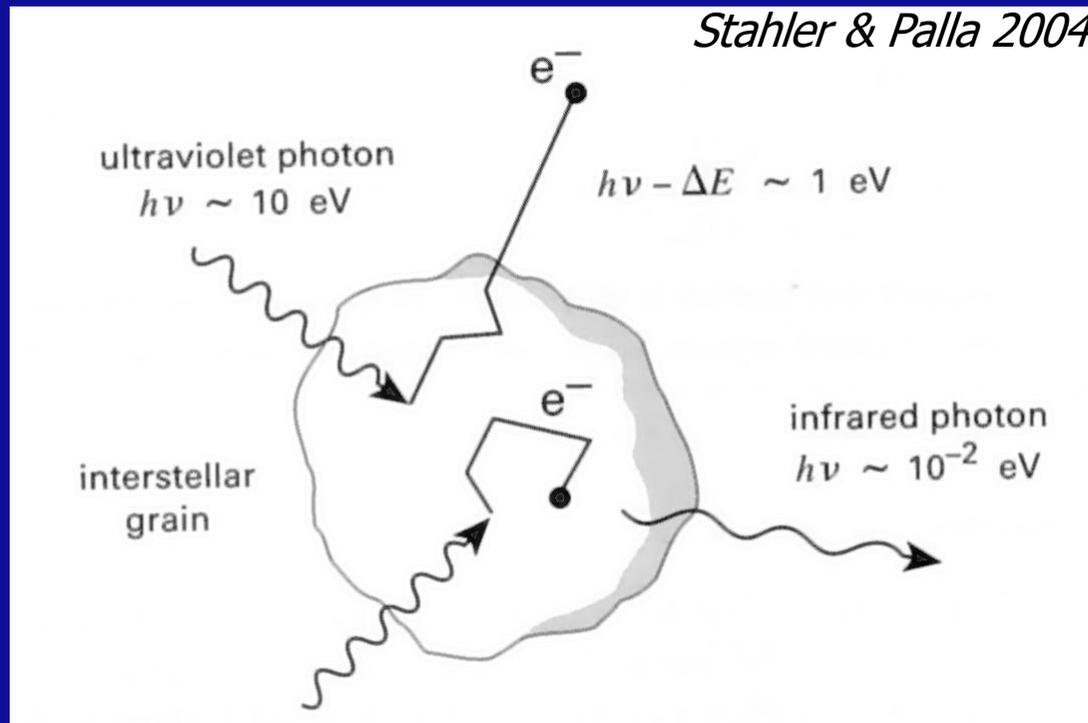
Extinction dims *and* reddens the light

Interstellar dust: Extinction at shorter wavelengths



Extinction dims *and* reddens the light

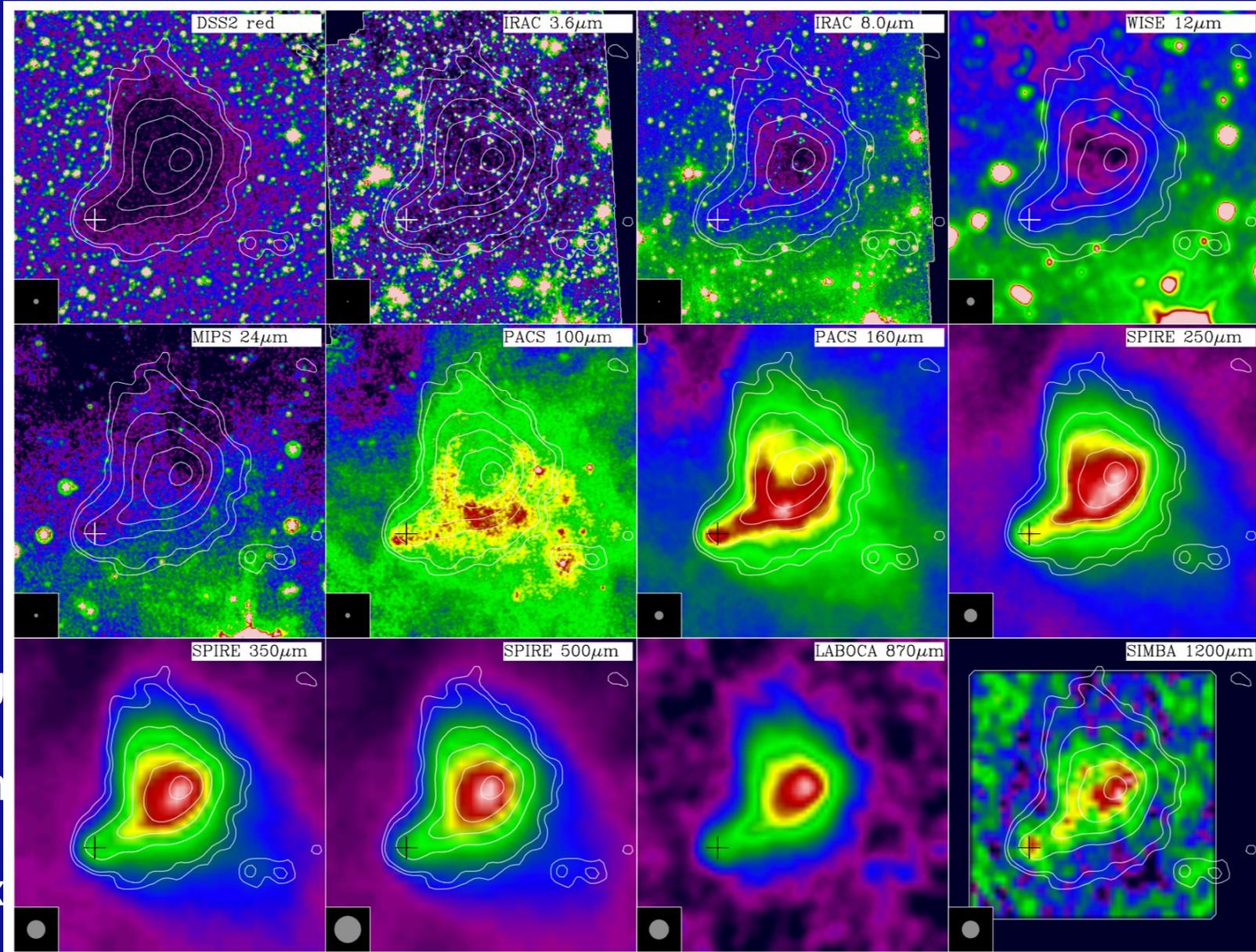
Dust action at longer wavelengths: Re-emission



Dust grain hit by UV photon:

- 1) Photoelectrical effect \rightarrow give energy to e^- \rightarrow leaves grain and heats gas.
- 2) Excites lattice vibrations \rightarrow transformed to (far)-IR photons and re-emitted.

Dust action at longer wavelengths: Re-emission



Dust g

1) Ph

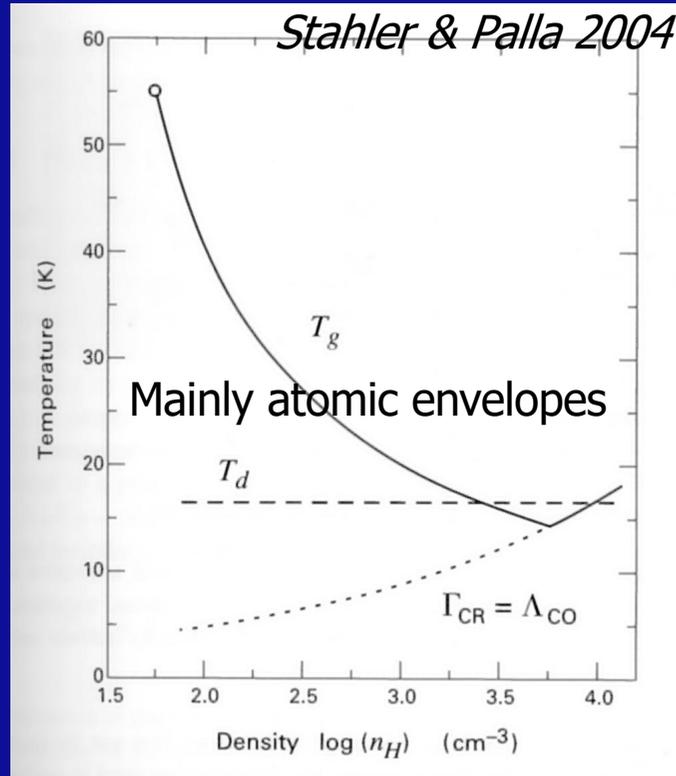
2) Ex

gas.
mitted.

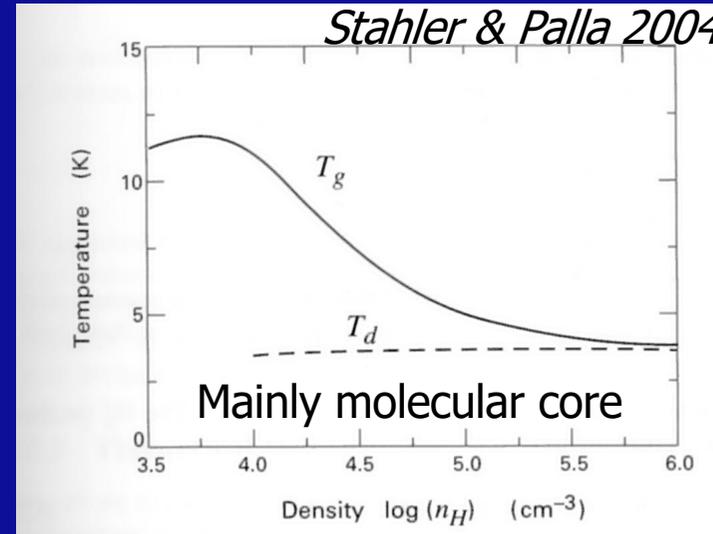
Nielbock et al. 2012, Contours 870μm

Continue next week

Dust and gas coupling



Cosmic ray heating more sensitive to density than CO cooling. Hence T_g rises again.

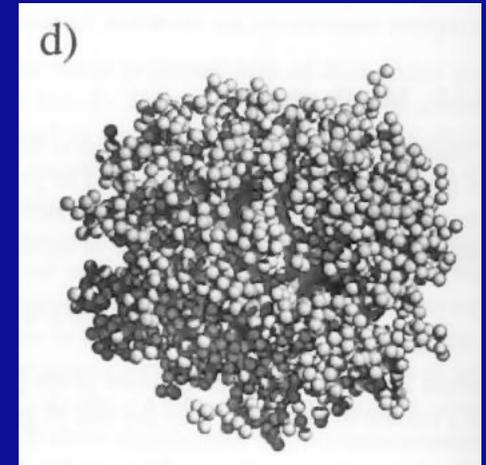
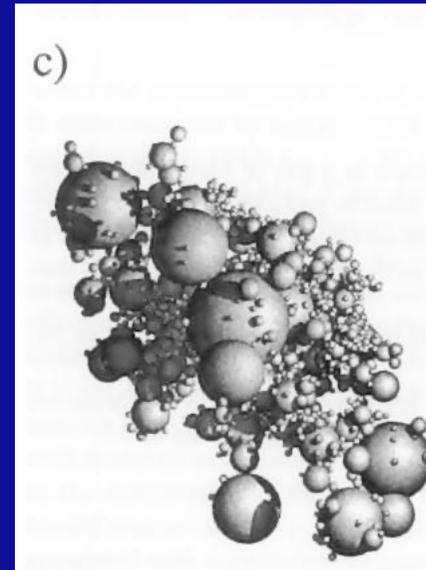
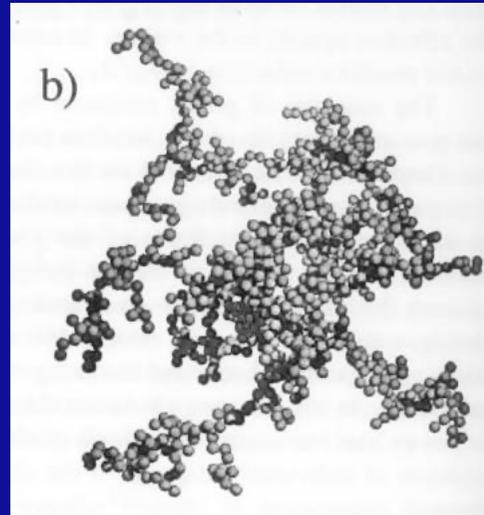
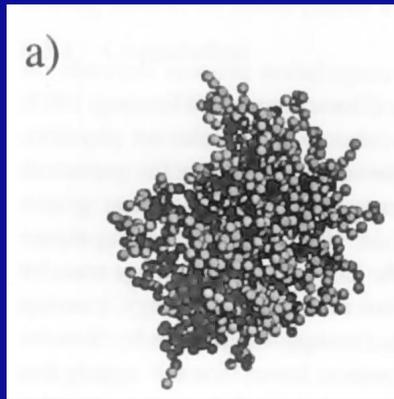


simplified model \rightarrow
lowest obs.
 $T_d \sim 7-10\text{K}$

Γ – heating rate Λ – Cooling rate

- Low densities: gas and dust de-coupled; at high densities coupled.
- Low densities gas cooling mainly CO; high densities via CO & dust.
- At very high densities gas and dust temperatures approach each other
 \rightarrow CO cooling becomes insignificant then!

Dust incarnations



Dust can grow and coagulate in very dense environments, e.g., disks.

Figures: Simulations of dust grain cluster growth for different initial parameters (gas and dust density, temperature, stickiness, grain charge, coagulation time ...).
(From Dorschner & Henning 1995)

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- Magnetic field measurements (Zeeman and dust)
- Maser emission
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)
---> shifted to next week

Summary

- Line profiles (thermal and kinematic broadening) and some applications
- Magnetic fields are very important but difficult to measure:
 - Zeeman effect traces **B** component along line of sight.
 - Dust polarisation traces **B** in plane of the sky.
(Other magnetic field measurements possible.)
- Masers are non-thermal processes. Good for high spatial accuracy and proper motion studies.
- Dust important from many points of view:
 - Traces warm and cold components of ISM.
 - Important coolant at high densities.
 - Traces magnetic field.
 - Chemical catalyst.
- Physical distributions and their applicability to the ISM.

Sternentstehung - Star Formation

Winter term 2024/2025

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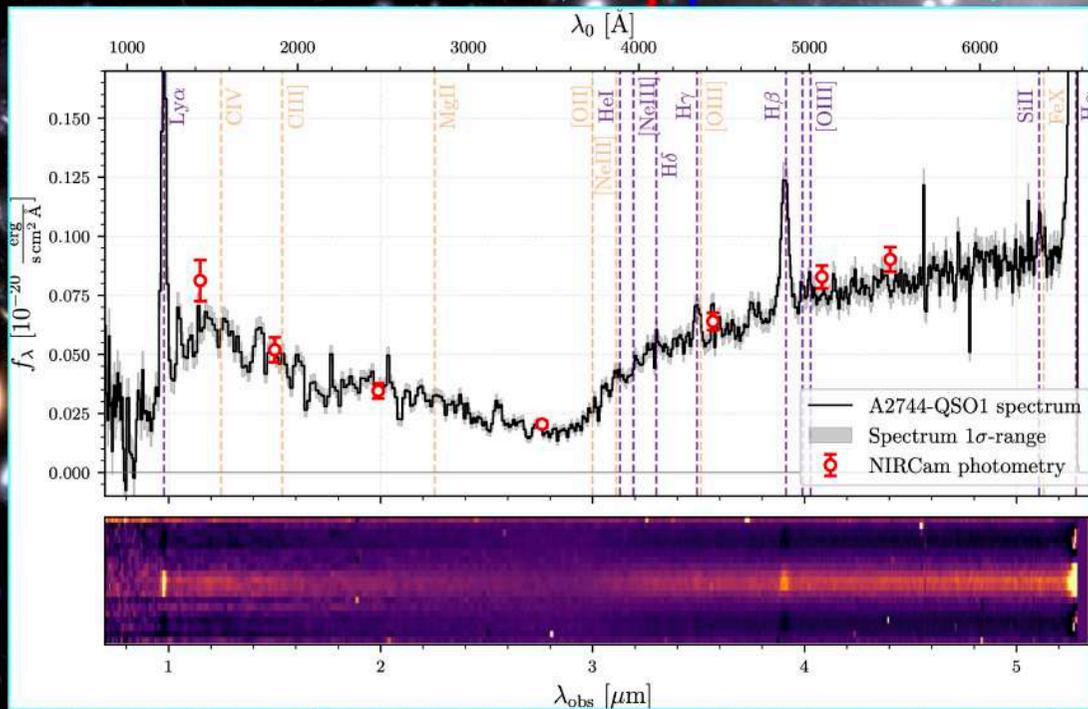
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11.02	Examination week, no star formation lecture	(Beuther, Gieser, Henning)

Book: Stahler & Palla: The Formation of Stars, Wileys

More Information and the current lecture files: http://www.mpia.de/homes/beuther/lecture_ws2425.html
beuther@mpia.de, henning@mpia.de, gieser@mpia.de

Tuesday November 5th Main Lecture Theatre, Philosophenweg 12, 16:30 CEST

Jenny Greene (Princeton University): The Nature of "Little Red Dots"



<https://www.physik.uni-heidelberg.de/hephysto/>

Host: Nadine Neumayer (neumayer.@mpia.de)