### Sternentstehung - Star Formation

Winter term 2024/2025

Henrik Beuther, Thomas Henning & Caroline Gieser

15.10 Today: Introduction & Overview (Beuther) 22.10 Physical processes I (Beuther) 29.10 ---05.11 Physcial processes II 12.11 Molecular clouds as birth places of stars 19.11 Molecular clouds (cont.), Jeans Analysis 26.11 Collapse models I 03.12 Collapse models II 10.12 Protostellar evolution 17.12 Pre-main sequence evolution & outflows/jets 07.01 Accretion disks I 14.01 Accretion disks II 21.01 High-mass star formation, clusters and the IMF 28.01 Extragalactic star formation 04.02 Planetarium@HdA, outlook, questions 11.02 Examination week, no star formation lecture (Beuther, Gieser, Henning) Book: Stahler & Palla: The Formation of Stars, Wileys

More Information and the current lecture files: http://www.mpia.de/homes/beuther/lecture\_ws2425.html beuther@mpia.de, henning@mpia.de, gieser@mpia.de

(Beuther) (Beuther) (Henning) (Beuther) (Beuther) (Gieser) (Henning) (Henning) (Henning) (Gieser) (Henning)

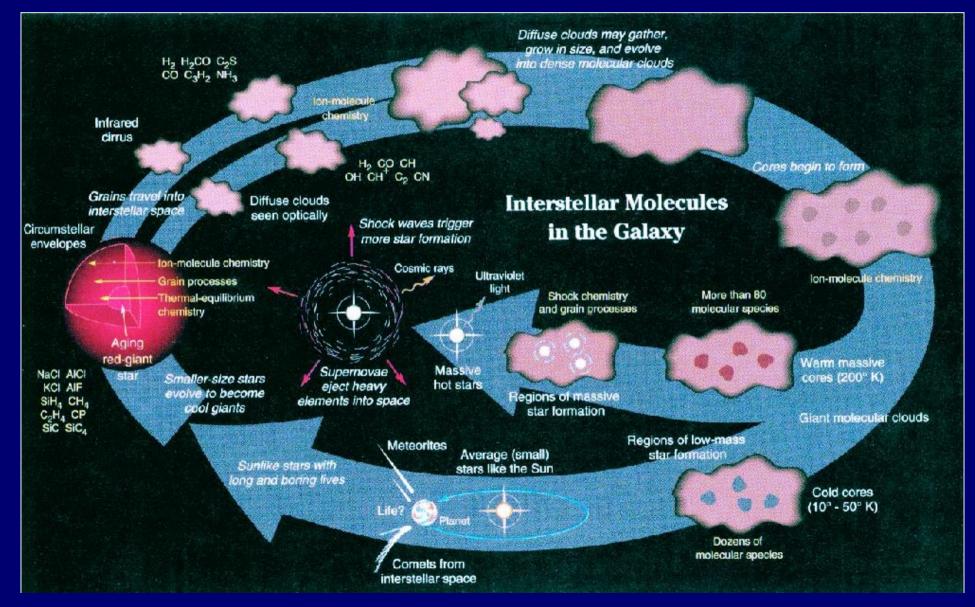
#### **Topics today**

#### - The ISM, molecules and depletion

- Heating and cooling

- Radiation transfer and column density determination

### The cosmic cycle



http://www.astro.uni-koeln.de

## **Properties of Molecular Clouds**

Туре	n [cm <sup>-3</sup> ]	Size [pc]	Т [K]	Mass [M <sub>sun</sub> ]
Giant Molecular Cloud	<b>10</b> <sup>2</sup>	50	15	<b>10</b> <sup>5</sup>
Dark Cloud Complex	5x10 <sup>2</sup>	10	10	104
Individual Dark Cloud	10 <sup>3</sup>	2	10	30
Dense low-mass cores	10 <sup>4</sup>	0.1	10	10
Dense high-mass cores	>10 <sup>5</sup>	0.1-1	10-30	100-10000



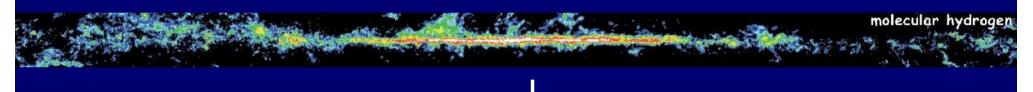
#### Neutral and ionized medium

atomic hydrogen

radio continuum (2.5 GHz)

http://adc.gsfc.nasa.gov

#### Stars form in the dense molecular gas and dust cores



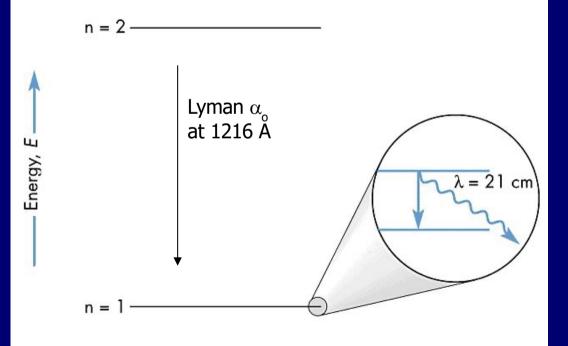
#### Most important astrophysical tools:

Spectral lines emitted by various molecules

Absorption and thermal emission from dust

### The Interstellar Medium I

Atomic Hydrogen



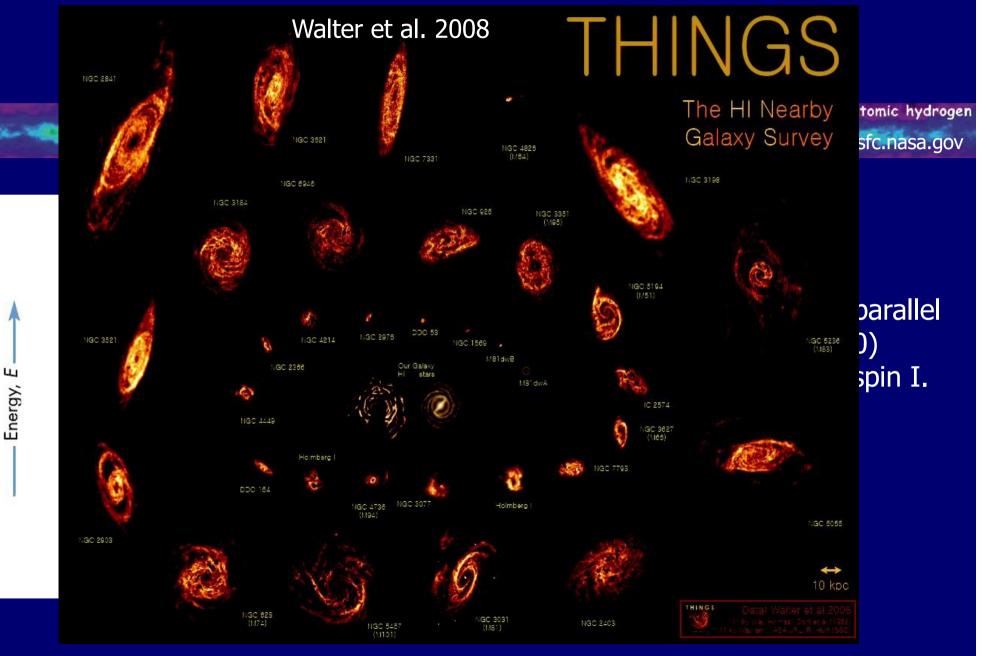
<u>21cm line:</u> electron spin S flip from parallel (F=1) to antiparallel (F=0) compared to the Proton spin I.

atomic hydrogen

http://adc.gsfc.nasa.gov

 $\Delta E = 5.9 \times 10^{-5} \, eV$ 

## The Interstellar Medium I



## The Ionized gas

Ionized gas

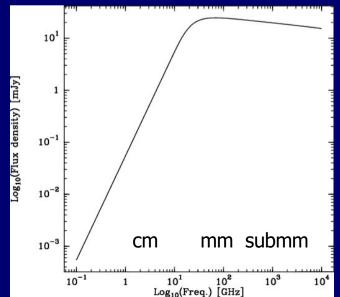
#### http://adc.gsfc.nasa.gov

radio continuum (2.5 GHz)

- Hydrogen recombination lines from optical to cm wavelengths
- Emission lines from heavier elements --> derive atomic abundances

- Free-free emission between e<sup>-</sup> and H<sup>+</sup>

He/H	0.1
C/H	3.4x10 <sup>-4</sup>
N/H	6.8x10 <sup>-5</sup>
O/H	3.8x10 <sup>-4</sup>
Si/H	3.0x10 <sup>-6</sup>



## The Molecular ISM Molecular Hydrogen http://adc.gsfc.nasa.gov molecular hydroge Carbon monoxide CO Cyanoacetyline HC<sub>3</sub>N Formaldehyde H<sub>2</sub>CO http://www.cdms.de

#### Excitation mechanisms:

- Rotation
- Vibration
- Electronic transitions
- --> usually cm and (sub)mm wavelengths
- --> usually submm to FIR wavelengths
- --> usually MIR to optical wavelengths

### **Molecular ISM Basics**

History:

- Late 1930s: Detection of CH, CH<sup>+</sup> and CN in diffuse clouds by absorption of optical light from background stars
- 1960s: Detection of OH, NH<sub>3</sub> and H<sub>2</sub>O at radio wavelength
- 1970: CO

Formation of molecules is an energy problem: Two atoms approach each other with positive total energy → rebound if no energy can be given away

Possibilities:

- Simultaneous collision with 3rd atom carrying away energy
  --> unlikely at the given low densities
- Form a molecule in excited state, and then radiating away energy
  --> probalility of such radiative association low as well

## Molecular ISM Basics

- Ion-molecule or ion-atom reactions can solve energy problem
- Neutral-neutral reactions on dust grain surfaces (catalytic) important
- Ion induces dipole moment in atom or molecule
  --> creates electrostatic attraction between the two.
  --> effective cross section increases over geometric values

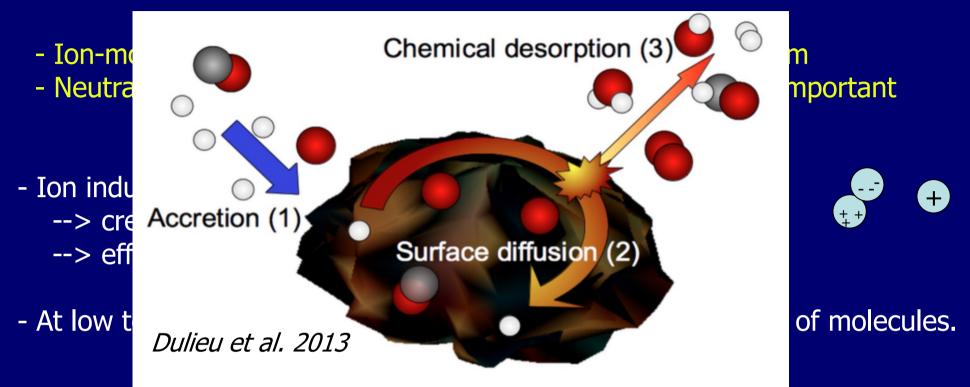


However, not enough ions to account for large H<sub>2</sub> abundances
 --> grain surface chemistry important

- Simple molecules like CO or CS  $\rightarrow$  ion-molecule chemistry,
- More complex molecules

 $\rightarrow$  grain surface chemistry important

## Molecular ISM Basics



However, not enough ions to account for large H<sub>2</sub> abundances
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 $\rightarrow$  grain surface chemistry important

#### Molecules in Space

#### Molecules in the Interstellar Medium or Circumstellar Shells (as of 09/2024)

2 atoms	3 atoms	4 atoms	5 atoms	6 atoms	7 atoms	8 atoms	9 atoms	10 atoms	11 atoms	12 atoms	>12 atoms
CH <sup>+</sup>	C <sub>3</sub> *	c-C <sub>3</sub> H	C5*	C <sub>5</sub> H	C <sub>6</sub> H	CH <sub>3</sub> C <sub>3</sub> N	CH <sub>3</sub> C <sub>4</sub> H	CH <sub>3</sub> C <sub>5</sub> N	HC <sub>9</sub> N	c-C <sub>6</sub> H <sub>6</sub> *	C <sub>60</sub> *
СН	C <sub>2</sub> H	I-C <sub>3</sub> H	C <sub>4</sub> H	I-H <sub>2</sub> C <sub>4</sub>	CH <sub>2</sub> CHCN	HC(O)OCH <sub>3</sub>	CH <sub>3</sub> CH <sub>2</sub> CN	(CH <sub>3</sub> ) <sub>2</sub> CO	CH <sub>3</sub> C <sub>6</sub> H	n-C <sub>3</sub> H <sub>7</sub> CN	C <sub>70</sub> *
CN	C <sub>2</sub> O	C <sub>3</sub> N	C <sub>4</sub> Si	$C_2H_4^{\star}$	CH <sub>3</sub> C <sub>2</sub> H	CH <sub>3</sub> COOH	(CH <sub>3</sub> ) <sub>2</sub> O	(CH <sub>2</sub> OH) <sub>2</sub>	C <sub>2</sub> H <sub>5</sub> OCHO	i-C <sub>3</sub> H <sub>7</sub> CN	C <sub>60</sub> **
ОН	C <sub>2</sub> S	C <sub>3</sub> O	I-C <sub>3</sub> H <sub>2</sub>	CH <sub>3</sub> CN	HC <sub>5</sub> N	C <sub>7</sub> H	CH <sub>3</sub> CH <sub>2</sub> OH	CH <sub>3</sub> CH <sub>2</sub> CHO	CH <sub>3</sub> OC(O)CH <sub>3</sub>	C <sub>2</sub> H <sub>5</sub> OCH <sub>3</sub>	c-C <sub>6</sub> H <sub>5</sub> CN
со	CH <sub>2</sub>	C <sub>3</sub> S	c-C <sub>3</sub> H <sub>2</sub>	CH <sub>3</sub> NC	CH <sub>3</sub> CHO	C <sub>6</sub> H <sub>2</sub>	HC <sub>7</sub> N	CH <sub>3</sub> CHCH <sub>2</sub> O	CH <sub>3</sub> C(O)CH <sub>2</sub> OH	1-c-C <sub>5</sub> H <sub>5</sub> CN	HC <sub>11</sub> N
H <sub>2</sub>	HCN	C <sub>2</sub> H <sub>2</sub> *	H <sub>2</sub> CCN	CH <sub>3</sub> OH	CH <sub>3</sub> NH <sub>2</sub>	CH <sub>2</sub> OHCHO	C <sub>8</sub> H	CH <sub>3</sub> OCH <sub>2</sub> OH	c-C <sub>5</sub> H <sub>6</sub>	2-c-C <sub>5</sub> H <sub>5</sub> CN	1-C <sub>10</sub> H <sub>7</sub> CN
SiO	HCO	NH <sub>3</sub>	$CH_4^*$	CH <sub>3</sub> SH	c-C <sub>2</sub> H <sub>4</sub> O	I-HC <sub>6</sub> H*	CH <sub>3</sub> C(O)NH <sub>2</sub>	c-C <sub>6</sub> H <sub>4</sub>	HOCH <sub>2</sub> CH <sub>2</sub> NH <sub>2</sub>	CH <sub>3</sub> C <sub>7</sub> N (?)	2-C10H7CN
CS	HCO+	HCCN	HC <sub>3</sub> N	HC <sub>3</sub> NH <sup>+</sup>	H <sub>2</sub> CCHOH	CH <sub>2</sub> CHCHO	C <sub>8</sub> H <sup>-</sup>	H <sub>2</sub> CCCHC <sub>3</sub> N	H <sub>2</sub> CCCHC <sub>4</sub> H	n-C <sub>3</sub> H <sub>7</sub> OH	c-C <sub>9</sub> H <sub>8</sub>
SO	HCS <sup>+</sup>	HCNH <sup>+</sup>	HCCNC	НСССНО	C <sub>6</sub> H⁻	CH <sub>2</sub> CCHCN	C <sub>3</sub> H <sub>6</sub>	C <sub>2</sub> H <sub>5</sub> NCO	C <sub>10</sub> H <sup>-</sup> (2023)	i-C <sub>3</sub> H <sub>7</sub> OH	1-c-C <sub>5</sub> H <sub>5</sub> CCH
SiS	HOC+	HNCO	HCOOH	NH <sub>2</sub> CHO	CH <sub>3</sub> NCO	H <sub>2</sub> NCH <sub>2</sub> CN	CH <sub>3</sub> CH <sub>2</sub> SH	C <sub>2</sub> H <sub>5</sub> NH <sub>2</sub> (?)	H <sub>2</sub> C(CH) <sub>3</sub> CN (2023)	(CH <sub>3</sub> ) <sub>2</sub> C=CH <sub>2</sub> (2023)	2-c-C <sub>5</sub> H <sub>5</sub> CCH
NS	H <sub>2</sub> O	HNCS	H <sub>2</sub> CNH	C <sub>5</sub> N	HC <sub>5</sub> O	CH <sub>3</sub> CHNH	CH <sub>3</sub> NHCHO	HC <sub>7</sub> NH <sup>+</sup>			c-C <sub>5</sub> H <sub>4</sub> CCH <sub>2</sub>
C2**	H <sub>2</sub> S	HOCO+	H <sub>2</sub> C <sub>2</sub> O	I-HC <sub>4</sub> H*	HOCH <sub>2</sub> CN	CH <sub>3</sub> SiH <sub>3</sub>	HC7O	E-CH <sub>3</sub> CHCHCN			2-C <sub>9</sub> H <sub>7</sub> CN
NO	HNC	H <sub>2</sub> CO	H <sub>2</sub> NCN	I-HC <sub>4</sub> N	HCCCHNH	H <sub>2</sub> NC(0)NH <sub>2</sub>	HCCCHCHCN	Z-CH <sub>3</sub> CHCHCN			C <sub>6</sub> H <sub>5</sub> CCH (2023)
HCI	HNO	H <sub>2</sub> CN	HNC <sub>3</sub>	c-H <sub>2</sub> C <sub>3</sub> O	HC <sub>4</sub> NC	HCCCH <sub>2</sub> CN	H2CCHC3N	CH <sub>3</sub> C(CN)CH <sub>2</sub>			CH <sub>3</sub> OCH <sub>2</sub> CH <sub>2</sub> OH (2024)
NaCl	MgCN	H <sub>2</sub> CS	SiH4*	H <sub>2</sub> CCNH	c-C <sub>3</sub> HCCH	HC <sub>5</sub> NH <sup>+</sup>	H <sub>2</sub> CCCHCCH	CH <sub>2</sub> CHCH <sub>2</sub> CN			
KCI	MgNC	H <sub>3</sub> O <sup>+</sup>	H <sub>2</sub> COH+	C <sub>5</sub> N <sup>-</sup>	I-H <sub>2</sub> C <sub>5</sub>	CH <sub>2</sub> CHCCH	HOCHCHCHO (2024)	HOCH <sub>2</sub> C(0)NH <sub>2</sub> (2023)			
AICI	N <sub>2</sub> H <sup>+</sup>	c-SiC <sub>3</sub>	C <sub>4</sub> H <sup>-</sup>	HNCHCN	MgC <sub>5</sub> N	MgC <sub>6</sub> H	HC <sub>7</sub> N <sup>+</sup> (2024)	CH3CH2CCH (2024)			
AIF	N <sub>2</sub> O	CH3*	HC(O)CN	SiH <sub>3</sub> CN	CH <sub>2</sub> C <sub>3</sub> N	C <sub>2</sub> H <sub>3</sub> NH <sub>2</sub>	CH <sub>2</sub> (CCH) <sub>2</sub> (2024				
PN	NaCN	C <sub>3</sub> N <sup>-</sup>	HNCNH	C <sub>5</sub> S	NC <sub>4</sub> NH <sup>+</sup> (2023)	(CHOH) <sub>2</sub>					
SIC	OCS	PH <sub>3</sub>	CH <sub>3</sub> O	MgC <sub>4</sub> H	MgC <sub>5</sub> N <sup>+</sup> (2023)	HC <sub>2</sub> (H)C <sub>4</sub>					
CP	SO2	HCNO	$NH_4^+$	CH <sub>3</sub> CO <sup>+</sup>	HC <sub>5</sub> N <sup>+</sup> (2024)	C7N <sup>-</sup> (2023)					
NH	c-SiC <sub>2</sub>	HOCN	H <sub>2</sub> NCO <sup>+</sup>	C <sub>3</sub> H <sub>3</sub>	HNC <sub>5</sub> (2024)	CH <sub>3</sub> CHCO (2023)					
SiN	CO2*	HSCN	NCCNH <sup>+</sup>	H <sub>2</sub> C <sub>3</sub> S	CH <sub>2</sub> (CN) <sub>2</sub> (2024	MgC <sub>6</sub> H <sup>+</sup> (2023)					
SO+	NH <sub>2</sub>	H <sub>2</sub> O <sub>2</sub>	CH <sub>3</sub> CI	HCCCHS		Z-(CH) <sub>2</sub> (CN) <sub>2</sub> (2024					
CO+	H3+(")	C <sub>3</sub> H <sup>+</sup>	MgC <sub>3</sub> N	C <sub>5</sub> O							
HF	SICN	HMgNC	NH <sub>2</sub> OH	C <sub>5</sub> H <sup>+</sup>							
SiH?	AINC	HCCO	HC <sub>3</sub> O <sup>+</sup>	HCCNCH <sup>+</sup>							
FeO?	SINC	CNCN	HC <sub>3</sub> S <sup>+</sup>	c-C <sub>3</sub> C <sub>2</sub> H							
O <sub>2</sub>	HCP	HONO	H <sub>2</sub> C <sub>2</sub> S	HC <sub>4</sub> S							
CF <sup>+</sup>	CCP	MgC <sub>2</sub> H	C <sub>4</sub> S	HMgC <sub>3</sub> N (2023)							
PO	AIOH	HCCS	HC(O)SH	MgC <sub>4</sub> H <sup>+</sup> (2023)							
AIO	H <sub>2</sub> O <sup>+</sup>	HNCN	HC(S)CN	H <sub>2</sub> C <sub>3</sub> H <sup>+</sup> (2023)							
OH*	H <sub>2</sub> Cl <sup>+</sup>	H <sub>2</sub> NC	HCCCO	H <sub>2</sub> C <sub>3</sub> N (2023)							
CN <sup>-</sup>	KCN	HCCS+	NaCCCN (2023)	(HO) <sub>2</sub> CO (2023)							
SH*	FeCN	CH <sub>3</sub> <sup>+</sup> (2023)	MgC <sub>3</sub> N <sup>+</sup> (2023)	H <sub>2</sub> CNCN (2024)							
SH	HO <sub>2</sub>	HCNS (2024)	HC <sub>3</sub> N <sup>+</sup> (2024)	NCHCCS (2024)					w.cd		<b>^</b>
HCI <sup>+</sup>	TiO <sub>2</sub>	HOCS <sup>+</sup> (2024)	HC <sub>3</sub> S (2024)					۱۸/۱۸/	W CO		$\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{\mathbf{$
TiO	C <sub>2</sub> N	HNSO (2024)	NC <sub>3</sub> S (2024)					<b>V V V</b>	VVICU		
ArH <sup>+</sup>	Si <sub>2</sub> C										
N <sub>2</sub>	HS <sub>2</sub>										
NO <sup>+</sup>	HCS										
NS <sup>+</sup>	HSC										
HeH*	NCO										
PO <sup>+</sup>	CaNC										
SiP ?	NCS										
FeC (2023)	MgC <sub>2</sub>										
	HSO (2023)										
	CaC <sub>2</sub> (2024)										

More than 320 detected interstellar molecules as of October 2024 (<u>www.cdms.de</u>). 74 molecular detection in extragalactic systems.

## A few important molecules

Mol.	Trans. A	Abund.	Crit. dens. [cm <sup>-3</sup> ]	Comments
H <sub>2</sub>	1-0 S(1)	1	8x10 <sup>7</sup>	Shock tracer
CO	J=1-0	8x10 <sup>-5</sup>	3x10 <sup>3</sup>	Low-density probe
OH	<sup>2</sup> ∏ <sub>3/2</sub> ;J=3/2	3x10 <sup>-7</sup>	1x10 <sup>0</sup>	Magnetic field probe (Zeeman)
$NH_3$	J,K=1,1	2x10 <sup>-8</sup>	2x10 <sup>4</sup>	Temperature probe
CS	J=2-1	1x10 <sup>-8</sup>	4x10 <sup>5</sup>	High-density probe
SiO	J=2-1		6x10 <sup>5</sup>	Outflow shock tracer
H <sub>2</sub> O	6 <sub>16</sub> -5 <sub>23</sub>		1x10 <sup>3</sup>	Maser
$H_2O$	$1_{10} - 1_{11}$	<7x10 <sup>-8</sup>	2x10 <sup>7</sup>	Warm gas probe
CH <sub>3</sub> OH	7-6	1x10 <sup>-7</sup>	1x10 <sup>5</sup>	Dense gas/temperature probe
CH <sub>3</sub> CN	19-18	2x10 <sup>-8</sup>	2x10 <sup>7</sup>	Temperature probe in Hot Cores

Crit. Dens.:  $n_{crit} \sim A/\gamma$ 

## Basics IV

Depletion of molecules on dust grains

In molecule's ref. frame, grains are moving at  $v_{therm}$  relative to molecules

 $E = 1/2 \text{ mv}^2_{\text{therm}} = 3/2 \text{ k}_b \text{T} => \text{v}_{\text{therm}} = (3\text{k}_b \text{T/m})^{1/2}$ 

n grains sweeps out cylindrical volume in time  $\Delta t$  of  $n(\pi a^2)v_{therm}\Delta t$  (a: grain radius)

Probability of molecule in volume V to be struck by grain in time  $\Delta t P(\Delta t) = n(\pi a^2)v_{therm}\Delta t /V$ 

For example CS:  $v_{therm} \sim 5 \times 10^3 cm s^{-1} at 10K$ ,  $n_H \sim 10^4 cm^{-3}$ ,  $\Sigma \sim 10^{-21} cm^2 t_{coll} \sim 6 \times 10^5 yr$ 

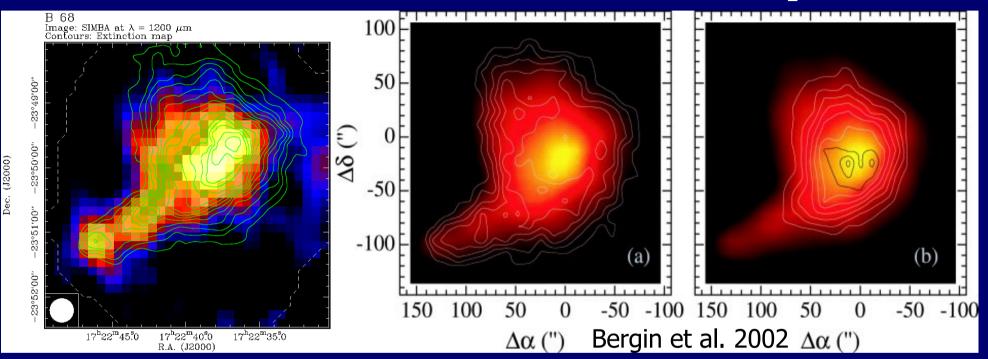
Depletion time-scale very short --> mechanisms for re-injecting molecules from grains important

### Depletion example

 $C^{18}O$ 

 $N_2H^+$ 

#### 1.2 mm Dust Continuum



Possible mechanisms working against depletion:

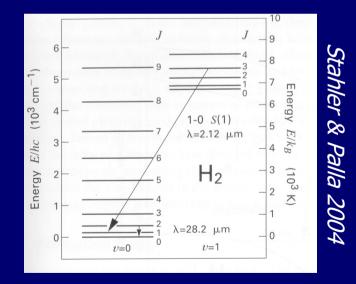
- UV radiation (not working in dense cores)
- In small grain, heat from chemical grain surface reactions could raise temperature
- Kelvin-Helmholtz contraction and energy
- Ignited central protostar
- Shocks

## Molecular Hydrogen (H<sub>2</sub>)

-  $H_2$  consists of 2 identical atoms  $\rightarrow$  no dipole moment

- Rotationally excited H<sub>2</sub> has allowed quadrupole transitions  $\Delta J = 2$  $\rightarrow$  lowest rotational transition J=2-0 has energy change of 510 K

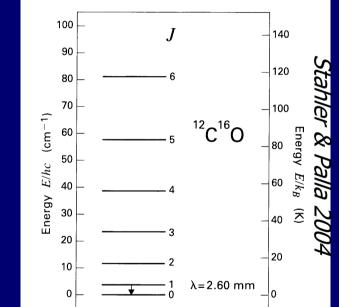
- Rotational energy for H<sub>2</sub>: Classical mechanics: E<sub>rot</sub> = J<sup>2</sup>/2I (J: Angular momentum; I: Moment of inertia)
  - → Small moment of inertia (I=mr<sup>2</sup>)
    → large spread of energy levels



 $\rightarrow$  Cold clouds have to be observed other ways, e.g., CO

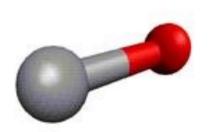
# Carbon monxide (CO)

- Forms through gas phase reactions.
- Strong binding energy of 11.1 eV
  - $\rightarrow$  prevents much further destruction (self-shielding).
- Permanent dipole moment  $\rightarrow$  strong emission at (sub)mm wavelengths.
- Larger moment of inertia than H<sub>2</sub>.
  → more closely spaced rotational ladder, J=1 level at 4.8x10<sup>-4</sup>eV or 5.5K above ground
- In molecular clouds excitation mainly via collisions with H<sub>2</sub>.
- Critical density for thermodynamic equilibrium with H<sub>2</sub> n<sub>crit</sub> = A/γ ~ 3x10<sup>3</sup>cm<sup>-3</sup>. (A: Einstein A coefficient; γ: collision rate with H<sub>2</sub>)



- The level population follows a Boltzmann-law:

 $n_{J+1}/n_J = g_{J+1}/g_J \exp(-\Delta E/k_B T_{ex})$  (for CO, the statistical weights  $g_J = 2J + 1$ ) Excitation temperature  $T_{ex}$  measure for the level populations and equals the kinetic temperature  $T_{kin}$  if densities are >  $n_{crit}$ .



http://www.cdms.de

#### **Topics today**

#### - The ISM, molecules and depletion

- Heating and cooling

- Radiation transfer and column density determination

### Heating processes

UV radiation from stars

Energy injection from supernovae

Energy injection from outflows/jets

 Cosmic rays interact with HI and H<sub>2</sub> (mainly relativistic protons accelerated within magnetized shocks produced by supernova-remnant--molecular cloud interactions)

 $p^+ + H_2 \rightarrow H_2^+ + e^- + p^+$  (dissociation  $\rightarrow$  ion-molecule chemistry)

- Interstellar radiation (diffuse field permeating interstellar space) Mainly dissociates carbon (lower ionization potential than H<sub>2</sub>)

 $C + h_V -> C^+ + e^-$  Electron disperses energy to ISM by collisions.

Photoelectric heating: - Heats grains that re-radiate in infrared regime
 - UV photons eject e<sup>-</sup> from dust
 → e<sup>-</sup> heat surrounding gas via collisions

## Cooling processes

- H & H<sub>2</sub> no dipole moment  $\rightarrow$  no efficient coolant in cold molecular cloud  $\rightarrow$  other coolants needed

--> Hydrogen collides with ambient atoms/molecules/grains  $\rightarrow$  Cooling via these secondary constituents.

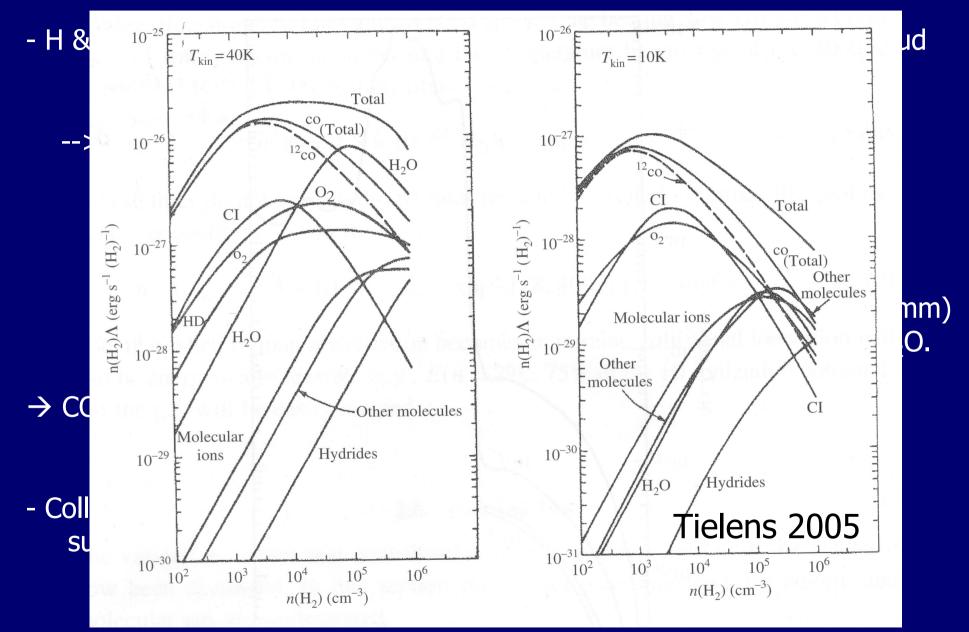
O + H --> O + H + hv collisional excitation (FIR)  $C^{+} + H \longrightarrow C^{+} + H + hv$ fine structure excitation (FIR)  $CO + H_2 \longrightarrow CO + H_2 + hv$ rotational excitation (radio/(sub)mm) At higher densities other molecules come into play, e.g.,  $H_2O$ .

 $\rightarrow$  CO the most effective coolant in molecular clouds.

- Collisions with gas atoms/molecules cause lattice vibrations on grain surfaces, that decay through the emission of infrared photons.

 $\rightarrow$  dust very efficient coolant

## Cooling processes



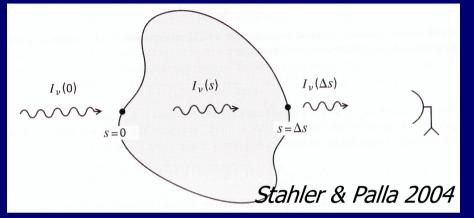
#### **Topics today**

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- Heating and cooling

Radiation transfer and column density determination

### Radiation transfer I



 $dI_{v} = -\kappa_{v}I_{v,0}ds + \varepsilon_{v}ds$ 

with the opacity  $d\tau_v = -\kappa_v ds$ 

κ: absorption coef.ε: emission coef.

and the source function  $S_v = \epsilon_v / \kappa_v$  $\Rightarrow dI_v / d\tau_v = I_{v,0} - S_v$ 

Assuming a spatially constant source function  $\rightarrow$  radiation transfer equation

 $\Rightarrow I_{v} = S_{v} (1 - e^{-\tau(v)}) + I_{v,0} e^{-\tau(v)}$ 

## Radiation transfer II

The excitation temperature  $T_{ex}$  is defined via a Boltzmann distribution as

 $n_{J}/n_{J-1} = g_{J}/g_{J-1} \exp(-h_{V}/kT_{ex})$ 

with n<sub>1</sub> and g<sub>1</sub> the number density and statistical weights.

In case of rotational transitions

 $g_{J} = 2J + 1$ 

J: rot. quantum number

In thermal equilibrium

 $T_{ex} = T_{kin}$ 

In a uniform molecular cloud the source function  $S_v$  equals Planck function

 $S_v = B_v (T_{ex}) = 2hv^3/c^2 (exp(hv/kT_{ex}) - 1)^{-1}$ 

### Radiation transfer III

Then the radiation transfer equation

 $\Rightarrow I_{v} = B_{v} (T_{ex}) (1 - e^{-\tau(v)}) + I_{v,0} e^{-\tau(v)}$ 

In the Rayleigh-Jeans limits ( $h_V < < kT$ ) B equals

 $B = (2kv^2/c^2)T$  (def.  $\rightarrow T = c^2/(2kv^2) I_v$ )

And the radiation transfer equation using now the radiation temperature is

$$T_r = J_v (T_{ex}) (1 - e^{-\tau(v)}) + J_{v,0} (T_{bq}) e^{-\tau(v)}$$

with

 $J_v = hv/k (exp(hv/kT) - 1)^{-1}$ 

#### Molecular column densities I

To derive molecular column densities, 3 quantities are important:

1) Intensity T of the line

2) Optical depth  $\tau$  of the line (observe isotopologues or hyperfine structure)

3) Partition function Q

The optical depth  $\tau$  of a molecular transition can be expressed like

 $\tau = c^2/8\pi v^2 A_{ul}N_u (exp(hv/kT) - 1) \phi$ 

with the Einstein A<sub>ul</sub> coefficient

 $A_{ul} = 64\pi^4 v^3 / (3c^3h) \mu^2 J_u / (2J_u-1)$ 

and the line form function  $\boldsymbol{\phi}$ 

 $\phi = c/v 2 \text{sqrt}(\ln 2)/(\text{sqrt}(\pi)\Delta v)$ 

#### Molecular column densities II

Using furthermore the radiation transfer eq. ignoring the background

 $T = J_v (T_{ex}) \tau (1 - e^{-\tau})/\tau$ 

And solving  $\tau$  -equation for N<sub>u</sub>, one gets

 $N_{u} = \frac{3k}{8\pi^{3}\nu} \frac{1}{\mu^{2}} (2J_{u}-1)/J_{u} \tau / (1 - e^{-\tau}) (T\Delta\nu \operatorname{sqrt}(\pi)/(2\operatorname{sqrt}(\ln 2)))$ 

The last expression equals the integral  $\int T dv$ .

 $\rightarrow N_u \sim \tau / (1 - e^{-\tau}) \int T dv$ 

The column density in the upper level N<sub>u</sub> relates to the total column density N<sub>tot</sub>

 $N_{tot} = N_u/g_u \exp(E_u/kT) Q$ 

For linear molecule like CO, partition function Q approximated: Q = kT/hB. (B: rotational constant)

However, for more complex molecules Q can become very complicated.

#### Conversion from CO to H<sub>2</sub> column densities

Classical way to derive conversion factors from CO to H<sub>2</sub> column densities:

- 1) Derive ratio between colour excess  $E_{B-V}$  and optical extinction  $A_v = 3.1 E_{B-V}$  (Savage and Mathis, 1979)
- 2) The ratio  $N(H_2)/E_{B-V}$ : One can measure the H<sub>2</sub> column density, e.g., directly from UV Absorption lines.
- 3) The ratio N(CO)/A<sub>v</sub>: In regions of molecular gas emission, one can estimate A<sub>v</sub> by star counts in the Infrared regime
- $\Rightarrow$  Combining these three ratios: CO  $\rightarrow$  H<sub>2</sub> column densities.

#### Summary

- Main tools: Spectral line emission and thermal emission and extinction from dust (more on dust next week)

- Molecules interesting for themselves and chemistry
- However, also extremely useful to trace physical processes.
- Molecules deplete on grains at low temperatures
- Discussed main cooling and heating processes
- Discussed basic line radiation transfer and column density determination

#### **Sternentstehung - Star Formation**

Winter term 2024/2025

Henrik Beuther, Thomas Henning & Caroline Gieser

*15.10 Today: Introduction & Overview 22.10 Physical processes I* 29.10 --

#### 05.11 Physcial processes II

12.11 Molecular clouds as birth places of stars 19.11 Molecular clouds (cont.), Jeans Analysis 26.11 Collapse models I 03.12 Collapse models II 10.12 Protostellar evolution 17.12 Pre-main sequence evolution & outflows/jets 07.01 Accretion disks I 14.01 Accretion disks II 21.01 High-mass star formation, clusters and the IMF 28.01 Extragalactic star formation 04.02 Planetarium@HdA, outlook, questions

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11.02 Examination week, no star formation lecture (Beuther, Gieser, Henning) Book: Stahler & Palla: The Formation of Stars, Wileys More Information and the current lecture files: http://www.mpia.de/homes/beuther/lecture\_ws2425.html beuther@mpia.de, henning@mpia.de , gieser@mpia.de Heidelberg Joint Astronomical Colloquium Winter Semester 2024/25 Tuesday October 22nd Main Lecture Theatre, Philosophenweg 12, 16:30 CEST

leftover emission from jet activity

galaxy centre with black hole

jet launched from black hole Leah Morabito (University of Durham):

> The highest resolution at the lowest frequencies: what LOFAR can tell us about active galactic nucleii

https://www.physik.uni-heidelberg.de/hephysto/ Host: Eduardo Banados (banados@mpia.de) Image Credit: L.K. Morabito; LOFAR Legacy Survey

#### Heidelberg Joint Astronomical Colloquium Winter Semester 2024/25

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22 Oct	Leah Morabito (University of Durham)
	The highest resolution at the lowest frequencies: what LOFAR can tell us about AGNs
29 Oct	Joe Callingham (SRON, Leiden)
	Radio stars and exoplanets: Discovering the space weather of other worlds
5 Nov	Jenny Greene (Princeton University)
	To be announced
12 Nov	Elena Pancino (INAF, Florence)
	To be announced
19 Nov	Daisuke Kawata (University College London)
1823	The JASMINE mission
26 Nov	Tadafumi Matsuno (Astronomisches Rechen-Institut, Heidelberg)
	Chemical Enrichments in the Milky Way and it's Accreted Dwarf Galaxies
3 Dec	Daniele Huppenkothen (SRON, Utrecht)
Che Con	To be announced
10 Dec	Barbara Ercolano (Universitäts-Sternwarte München)
	The atmospheres of discs and planets
17 Dec	Aurora Simionescu (Leiden Observatory)
	The beating hearts of galaxies: supermassive black hole feedback probed by X-ray spectroscopy
7 Jan	lise De Looze (University of Ghent)
1 34 5 6	To be announced
14 Jan	Caroline Heneka (Institut für Theoretische Physik, Heidelberg)
X	The Universe in multi-color: Astronomy at the dawn of intensity mapping and Al
21 Jan	Sylvia Ekstroem (University of Geneva)
	To be announced
28 Jan	Martin Pessah (Niels Bohr Institute, Copenhagen)
	To be announced
4 Feb	Amelie Saintonge (UC London / MPI für Radioastronomie, Bonn)
	To be announced
* TR	

https://www.physik.uni-heidelberg.de/hephysto/index.php?s=event@id=1

Caption: JWST-NIRCam image of the SNR Cassiopeia A with filters color coded as F162M: Blue F356W: Green F444W: Red NASA, ESA, CSA, STSCI, Danny Milisavljevic (Purdue University), Ilse De Looze (UGent), Tea Temim (Princeton University)

