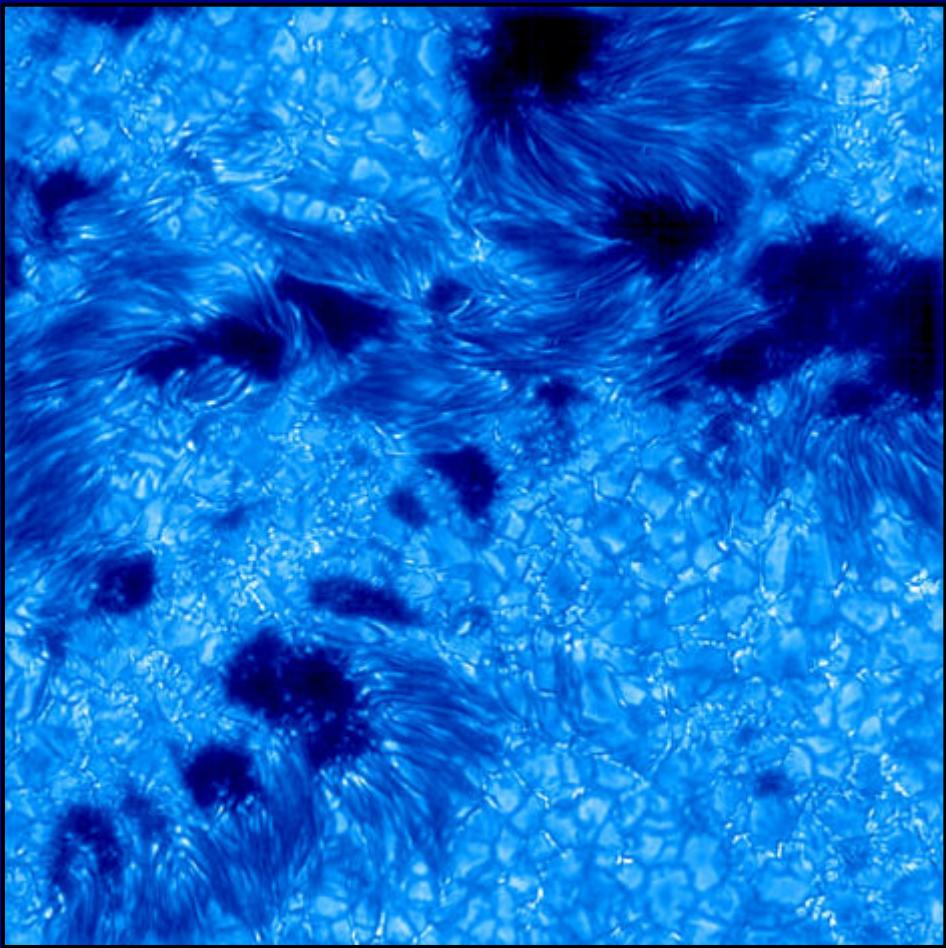
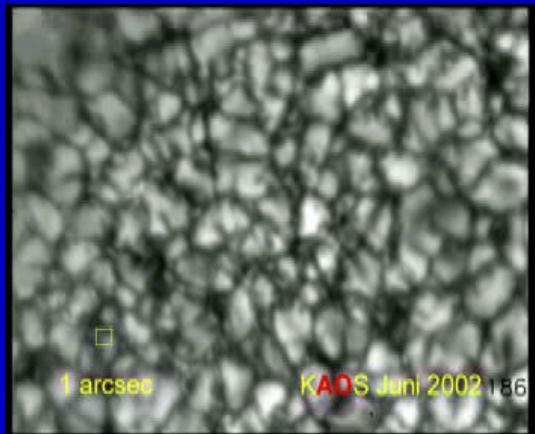
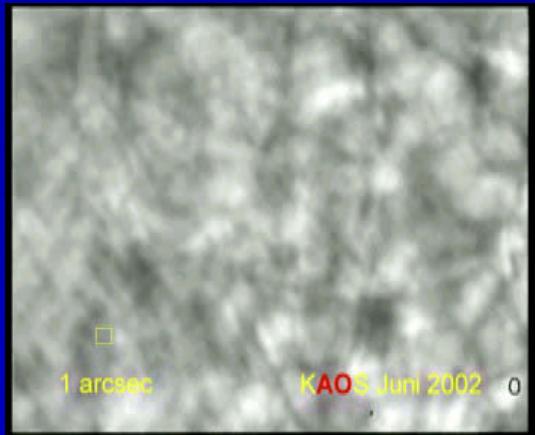


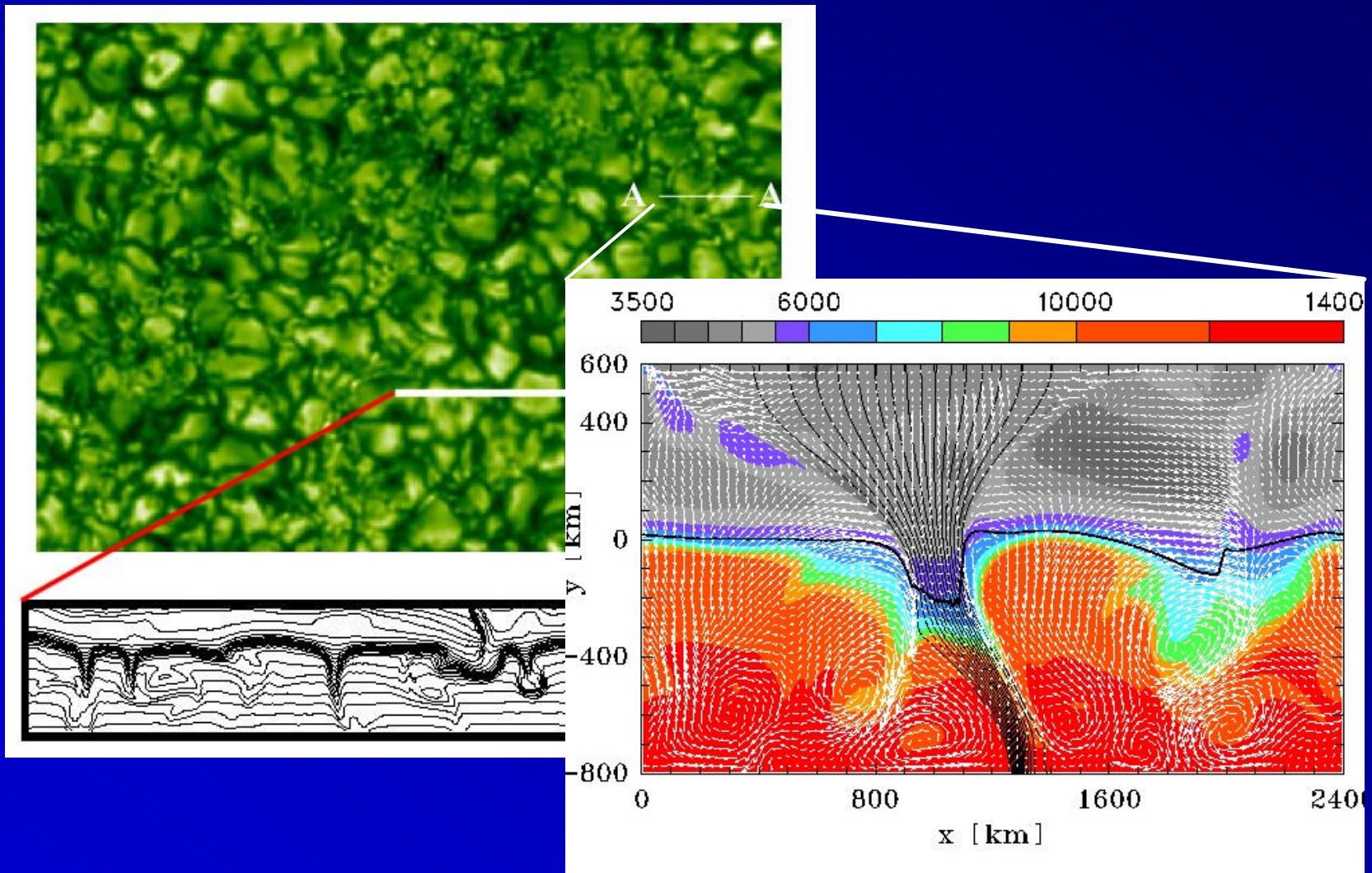
Interferometry of Close Binaries

Technical Considerations

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Kiepenheuer-Institut für Sonnenphysik
Freiburg, Germany





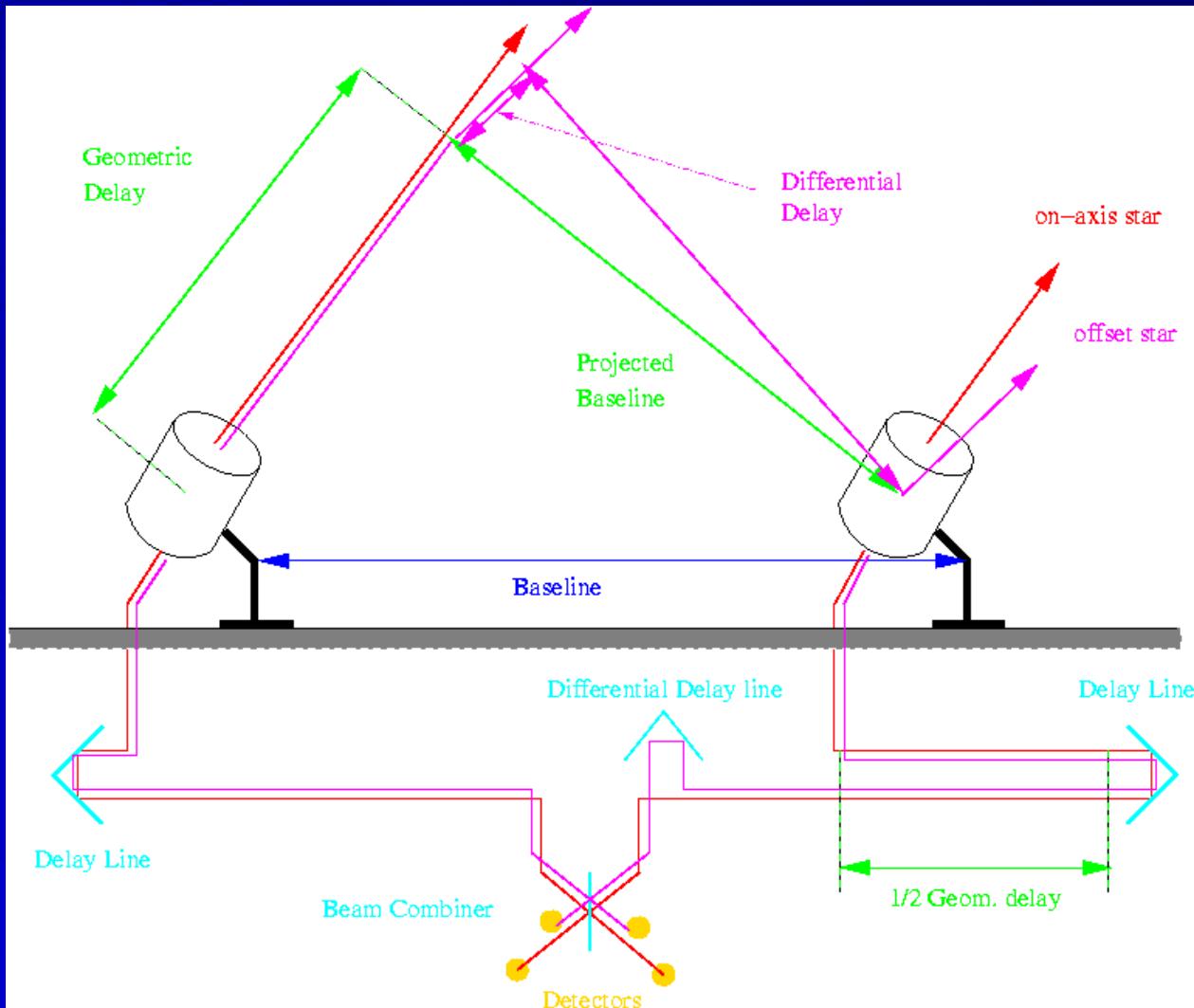


Why Double Stars?

- Simplest source of scientific interest
- Ideal probe to test / demonstrate the characteristics of a two-beam interferometer
- Particular emphasis on extended field issues

Scenario

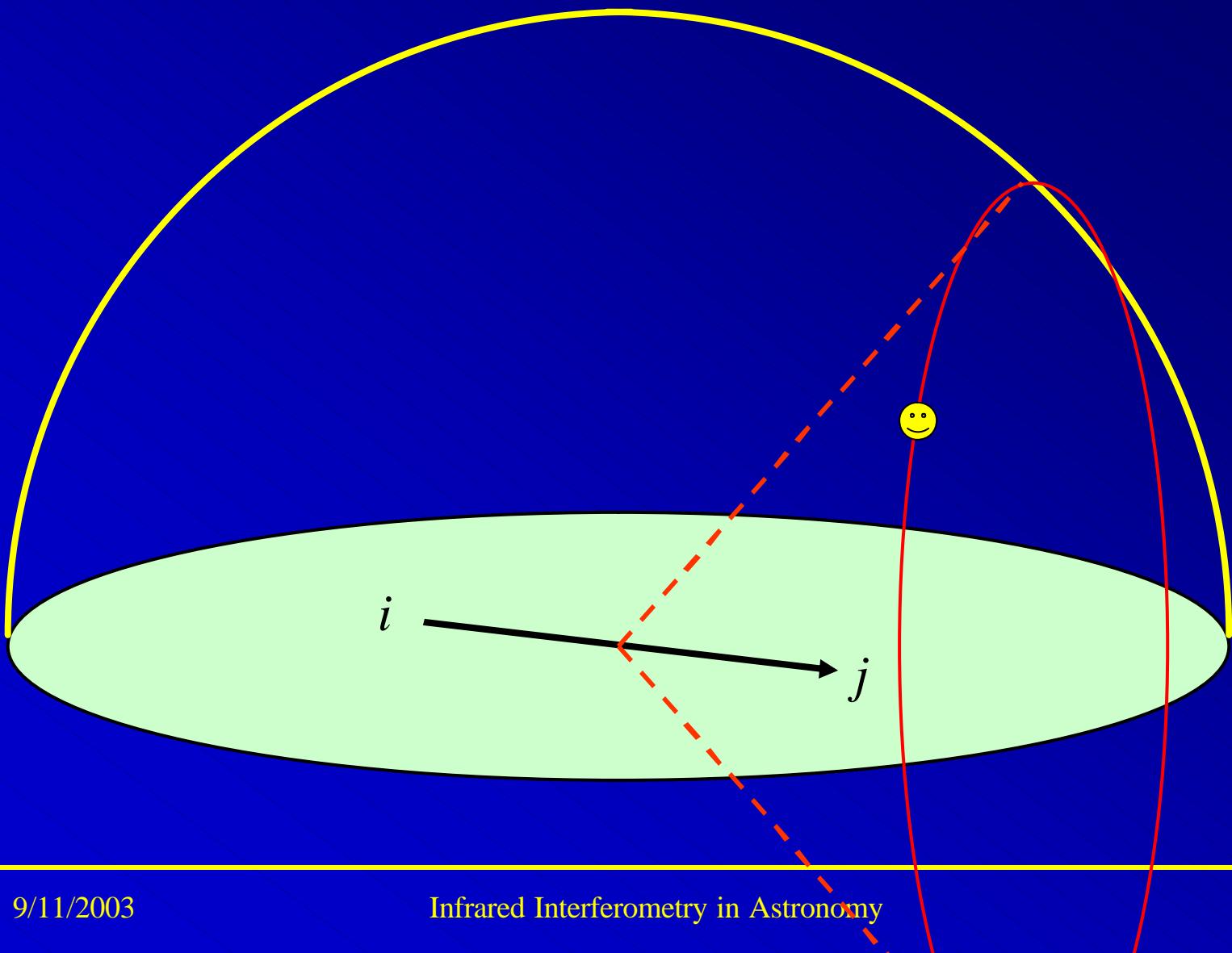
- Two late type main sequence stars somewhere in the FOV of MIDI
- Spectral types K0 ... L0, characterized by T_{eff}
- Spectral regime N band with various settings of the spectral resolution R_{λ}



Interferometer Basics

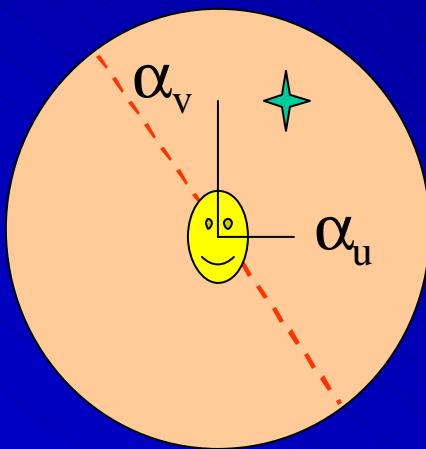
- Projected baseline:
- Cancel geometric delay w_{ij} by delay line for position (δ, h) in sky

$$\bar{\mathbf{B}}_{ij} = \begin{pmatrix} u_{ij} \\ v_{ij} \\ w_{ij} \end{pmatrix}(\mathbf{d}, h)$$



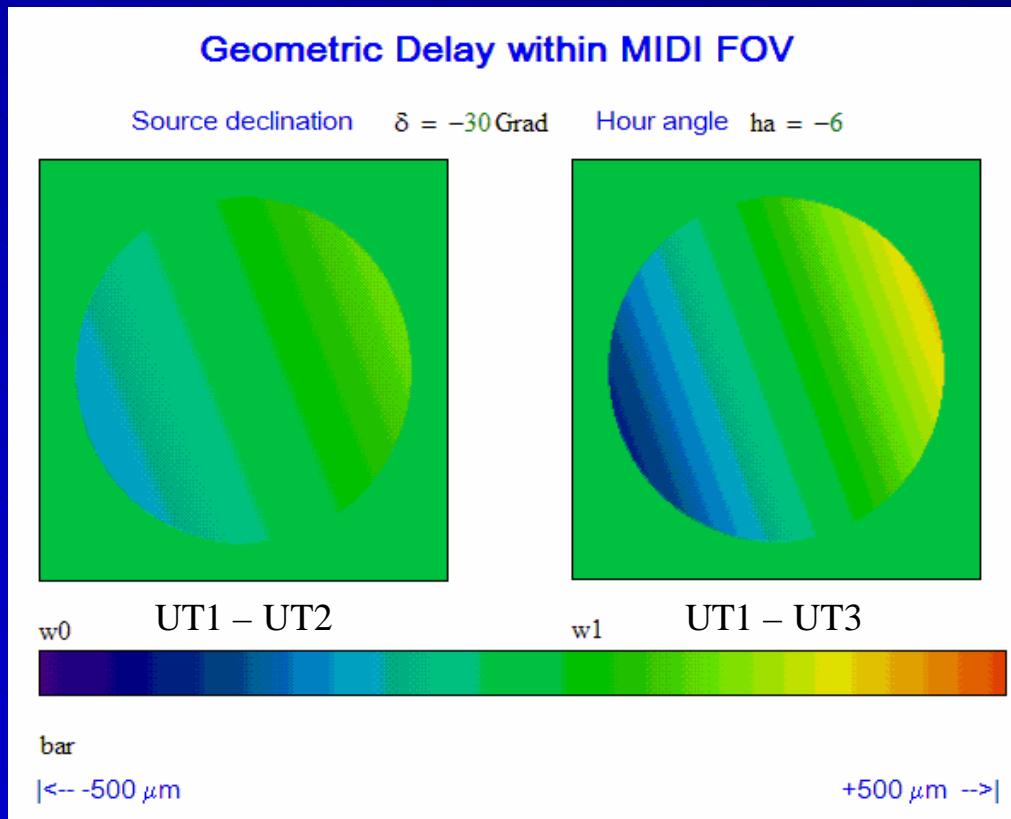
Single Baseline Differential Delay

- Differential delay d_w depends on offset angle a from tracking cone

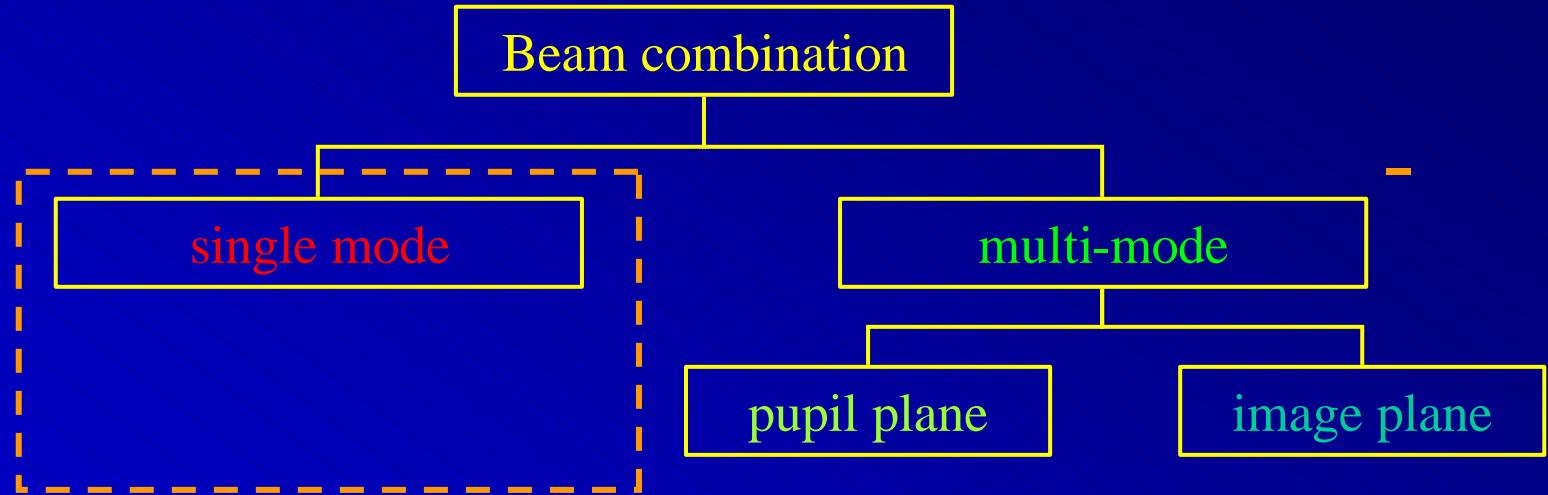


$$\begin{aligned} d_w &= \bar{\mathbf{B}}_{ij} \tilde{\mathbf{a}} \\ \tilde{\mathbf{a}} &= \begin{pmatrix} \mathbf{a}_u \\ \mathbf{a}_v \\ 0 \end{pmatrix} \end{aligned}$$

Differential Delay for MIDI FOV



Methods of beam combination

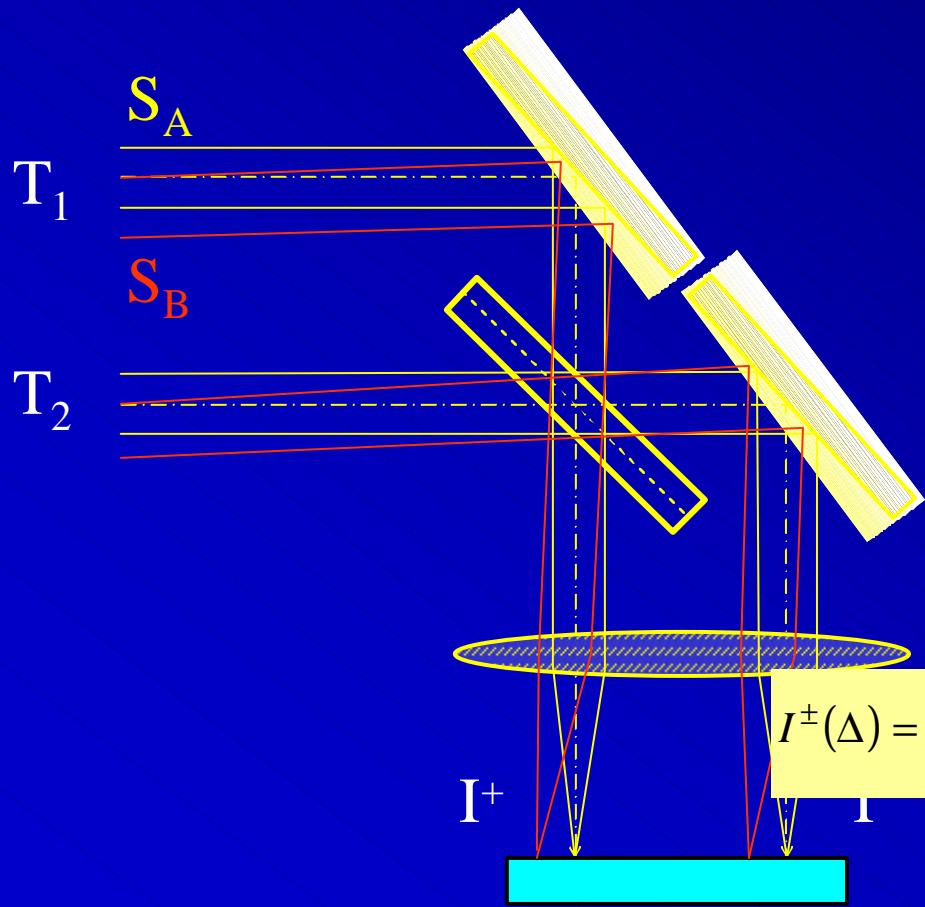


The detected field of view is equivalent to the Airy disk of an array element

The detected field of view exceeds the Airy disk of an array element.

Beam combination takes place in the plane of a transferred pupil or an image.

Multi-Mode Pupil Plane Beam Combination



- Quasi-monochromatic: $\mathbf{d}w < I R_I$
- Detected intensity:

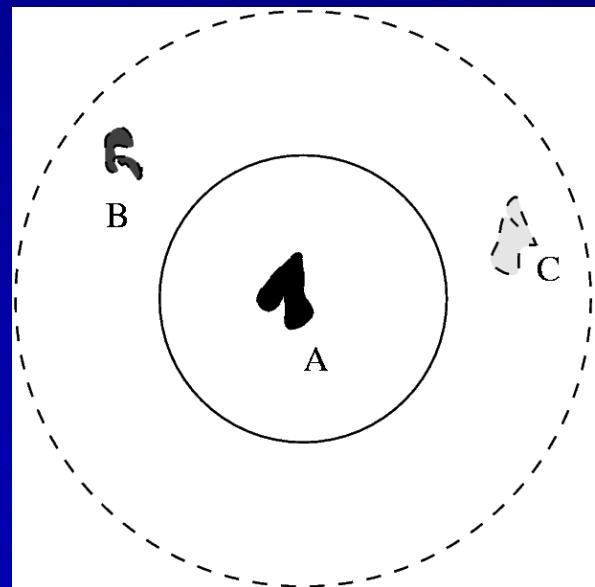
$$I^\pm(\Delta) = F_A \left[T_1^2 + T_2^2 \pm 2T_1T_2 \sin\left(2\pi i \left(\frac{\Delta + \mathbf{d}w_A}{I}\right)\right) \right] \\ + F_B \left[T_1^2 + T_2^2 \pm 2T_1T_2 \sin\left(2\pi i \left(\frac{\Delta + \mathbf{d}w_B}{I}\right)\right) \right]$$

- General intensity distribution:

$$I^\pm(\Delta) = \iint_{\text{Field}} F(\mathbf{a}) \left[T_1^2 + T_2^2 \pm 2T_1T_2 \sin\left(2\pi i \left(\frac{\Delta + \mathbf{d}w_A}{I}\right)\right) \right] d\mathbf{a}$$

Multi-Mode Pupil Plane Beam Combination

- Quasi-monochromatic:
business as usual!
- Fourier relation between measured
fringe visibility and object distribution
is preserved under quasi-
monochromatic conditions, even if
detected with a single pixel detector!
- What counts is the intensity of the
sources which are permitted to
propagate to the detector.
- Use field stops to reject unwanted
sources.



Polychromatic Conditions

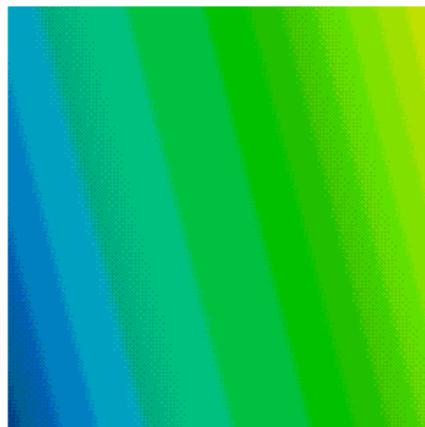
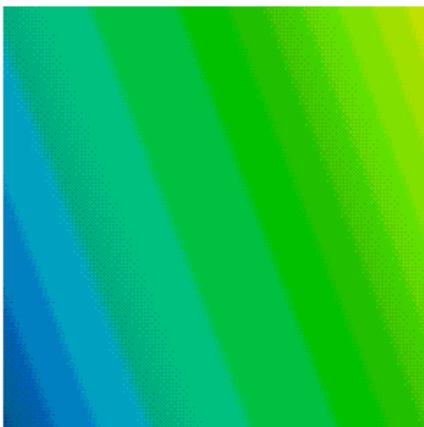
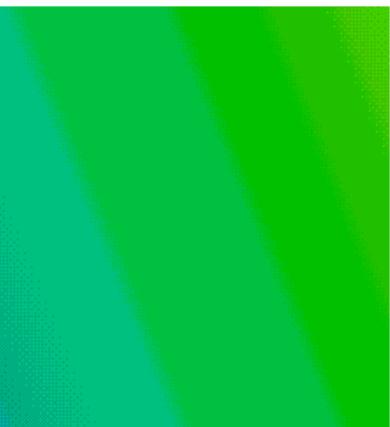
- Spectral distribution F_λ of source
- Spectral sensitivity E_λ of instrument
- Measured intensity is a complicated mixture of spatial and spectral information if differential delay approaches coherence length and sources are not separated!

$$\begin{aligned} I^\pm(\Delta) = & \int E_I F_{I,A} \left[T_1^2 + T_2^2 \pm 2T_1 T_2 \sin\left(2\pi i \left(\frac{\Delta + dw_A}{I}\right)\right) \right] dI \\ & + \int E_I F_{I,B} \left[T_1^2 + T_2^2 \pm 2T_1 T_2 \sin\left(2\pi i \left(\frac{\Delta + dw_B}{I}\right)\right) \right] dI \end{aligned}$$

Phase Difference across MIDI Pixel over Spectral Band

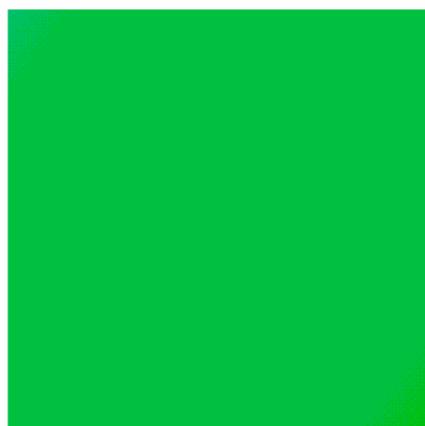
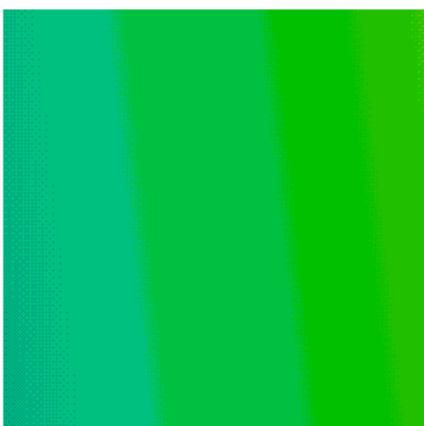
Source declination $\delta = -30$ Grad

Hour angle $ha = -6$



$\Delta\phi 1$

$\Delta\phi 2$



$\Delta\phi 4$

$\Delta\phi 5$



- 1 wave

+1 wave ->

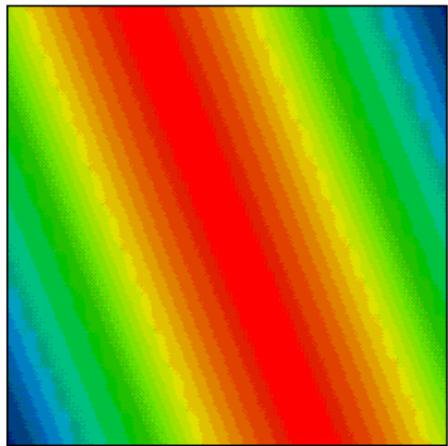
$$R_\lambda = 2.5$$

Fringe Contrast Loss across MIDI Pixel

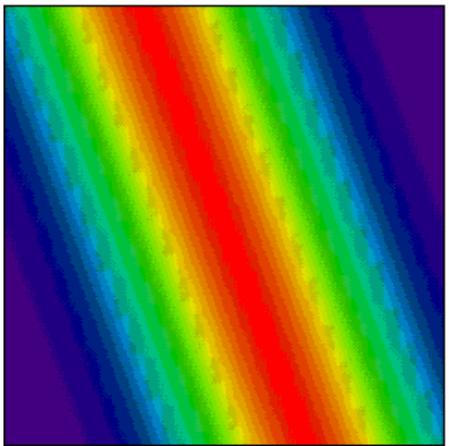
Source declination $\delta = -30$ Grad Hour angle $ha = -6$

IS

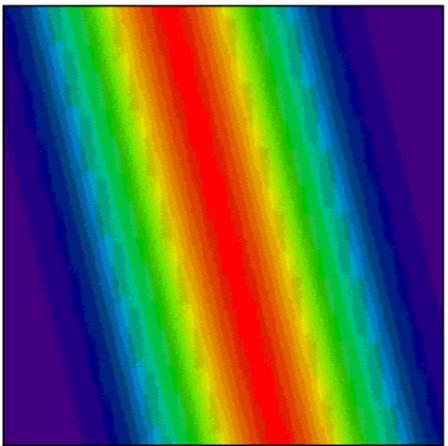
Kie



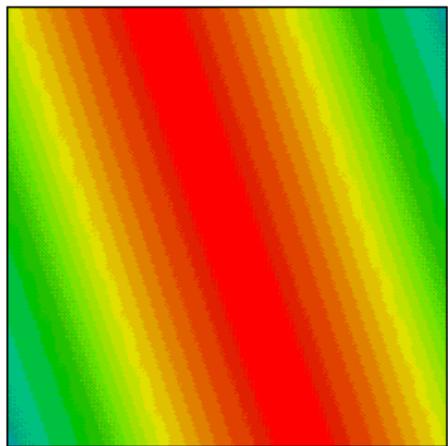
ΔV_0



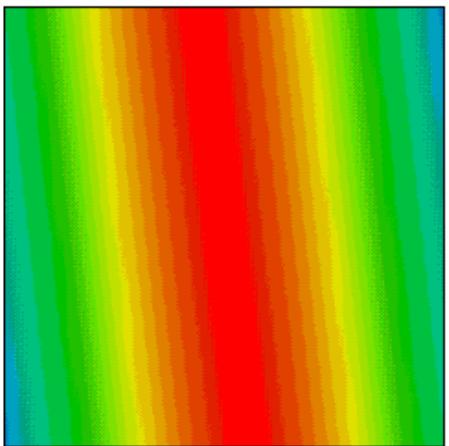
ΔV_1



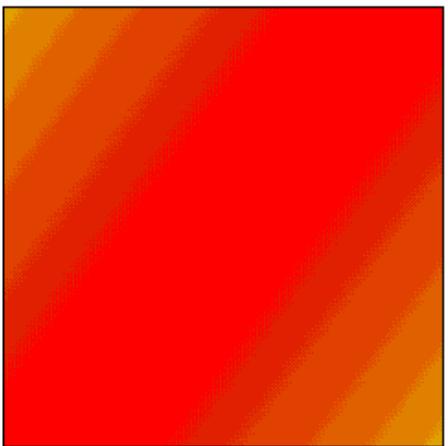
ΔV_2



ΔV_3



ΔV_4



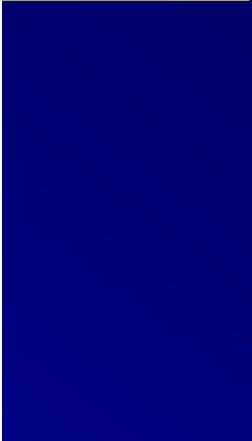
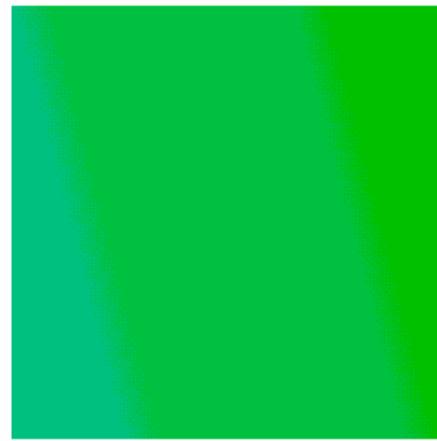
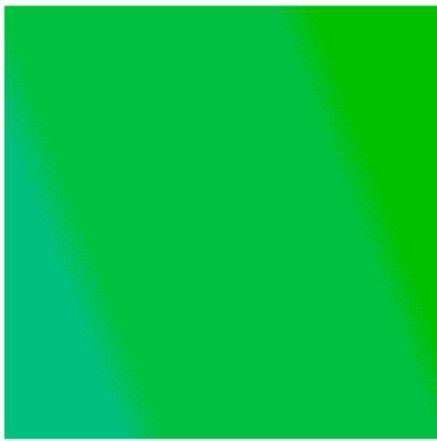
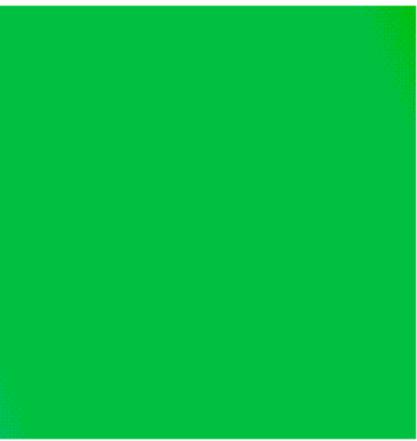
ΔV_5



Phase Difference across MIDI Pixel over Spectral Band



Source declination $\delta = -30$ Grad Hour angle $ha = -6$ Spectral resolution $R_s = 10$



$\phi 0$

$\Delta\phi 1$

$\Delta\phi 2$

$R_\lambda = 10$

$\phi 3$

$\Delta\phi 4$

$\Delta\phi 5$



bar

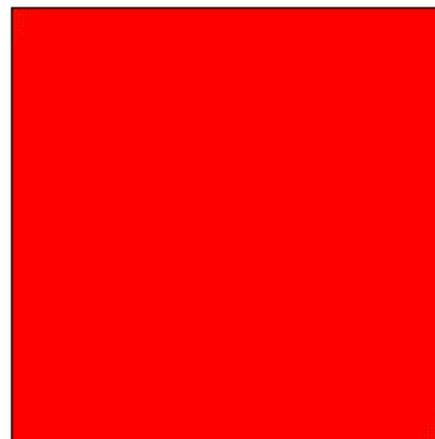
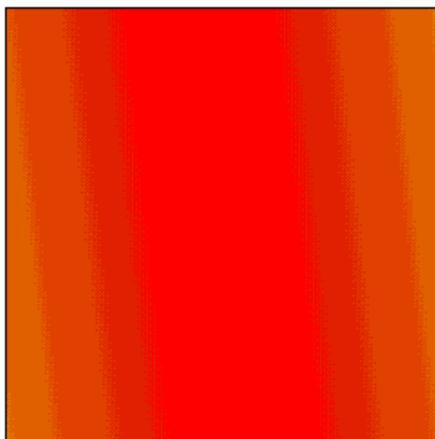
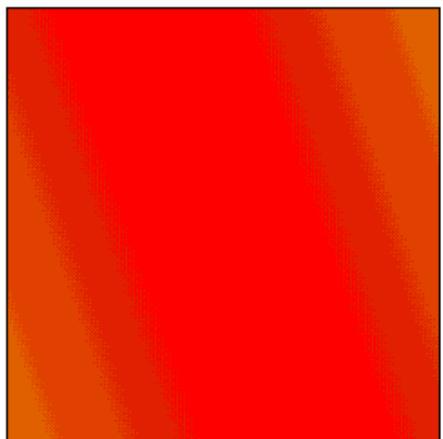
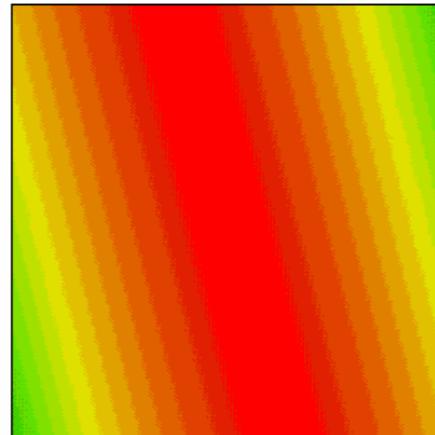
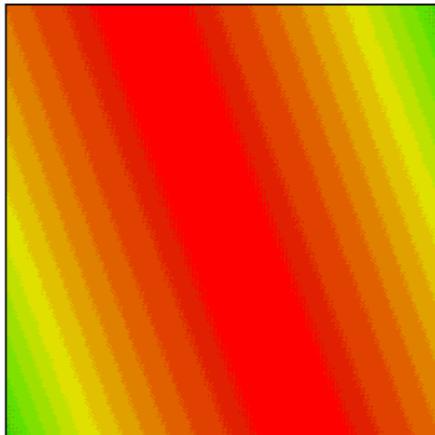
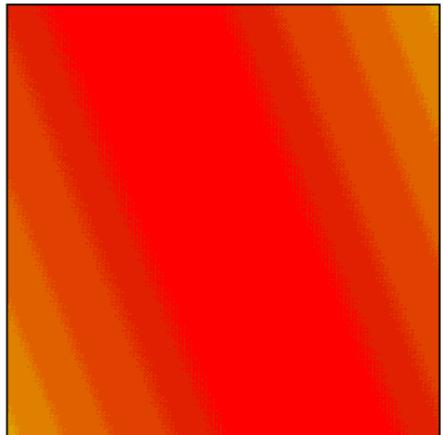
|< -1 wave

+1 wave >|

Fringe Contrast Loss across MIDI Pixel

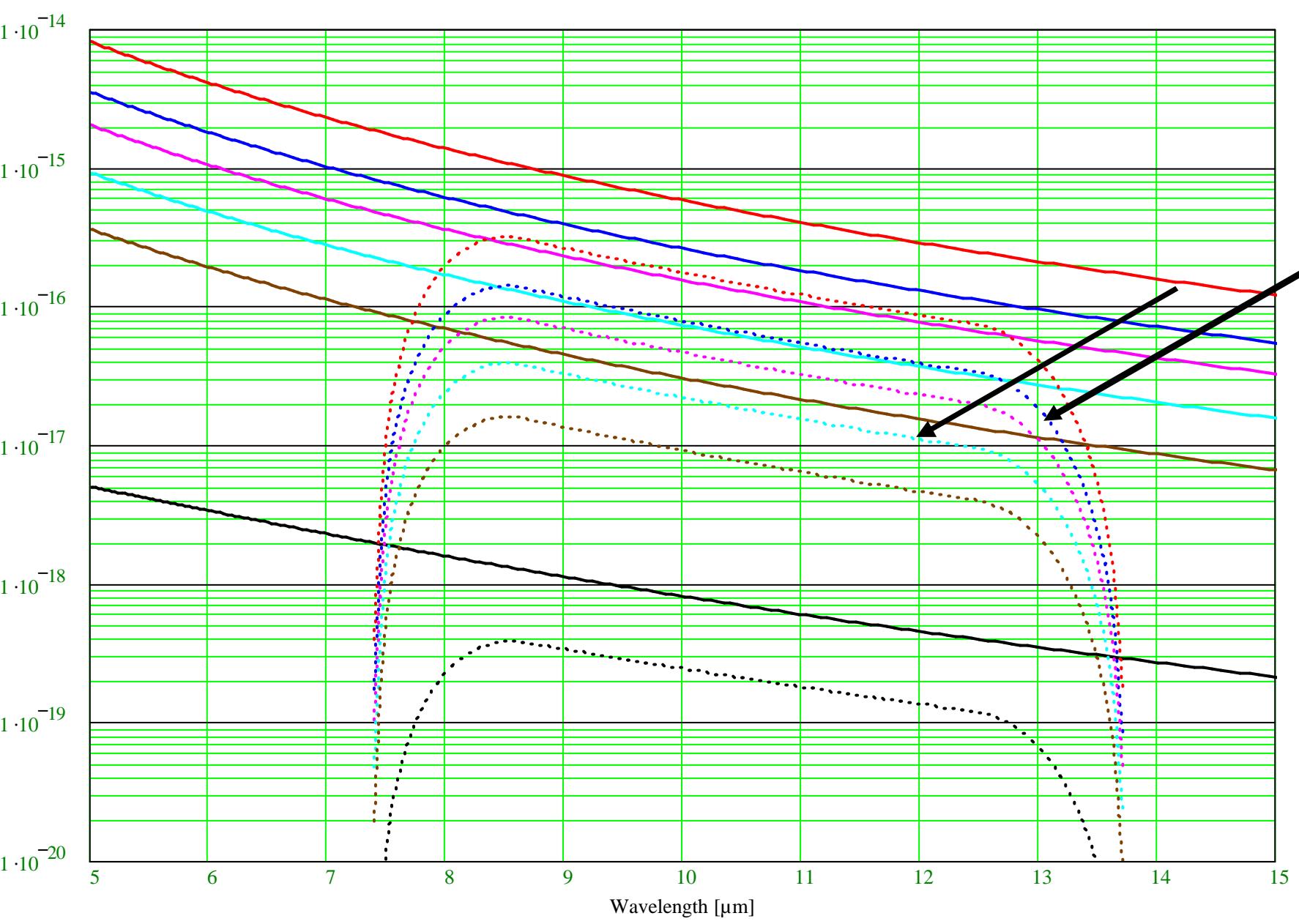
Kiep

Source declination $\delta = -30$ Grad Hour angle $ha = -6$ Spectral resolution $R_s = 10$

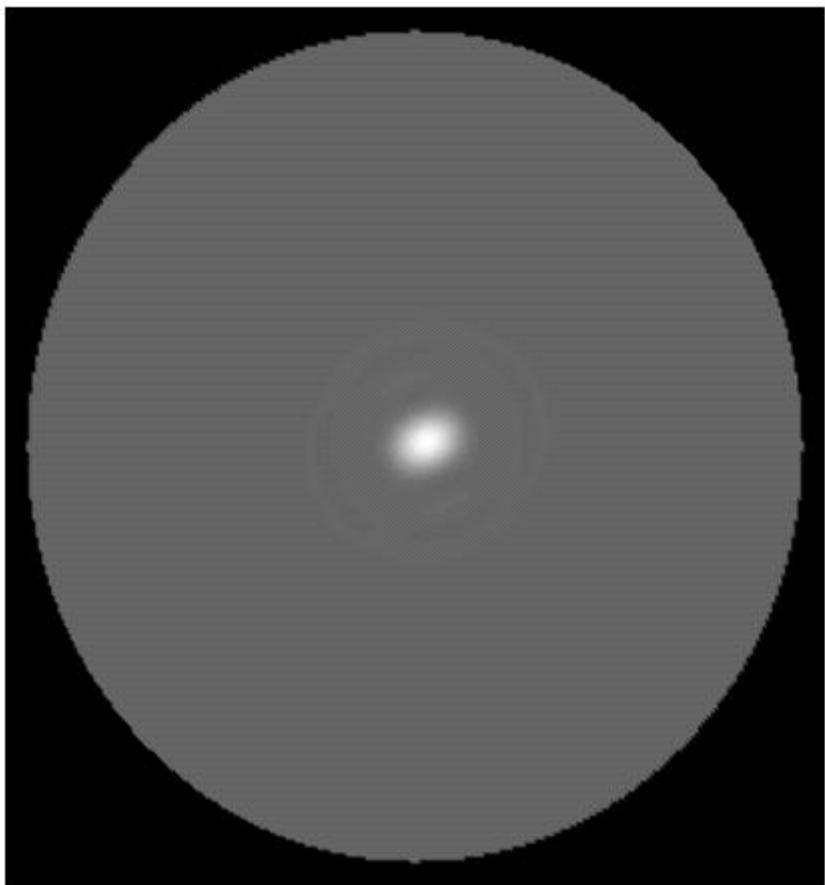


Close Binary Illustrations

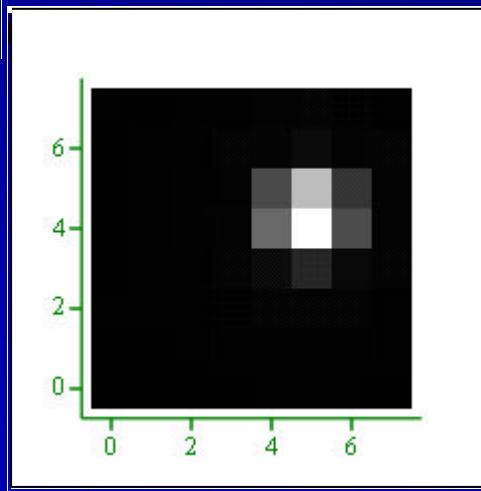
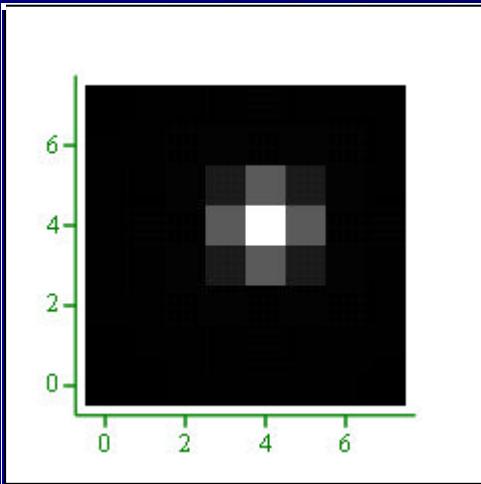
- Two stars at position $\delta = -30^\circ$, $h = 0$
- Distance 50 pc
- Relative positions $(\alpha, \delta)_A = (0,0)$ and $(\alpha, \delta)_B = (0.08, 0.03)$ arcsec from CoF
- Separation 0.085 arcsec (about 1 pixel!)
- Star A: K5V, Star B: M5V
- Rayleigh-Jeans law spectra in N Band
- N Flux ratio 1 / 0.28



Double Star in MIDI field

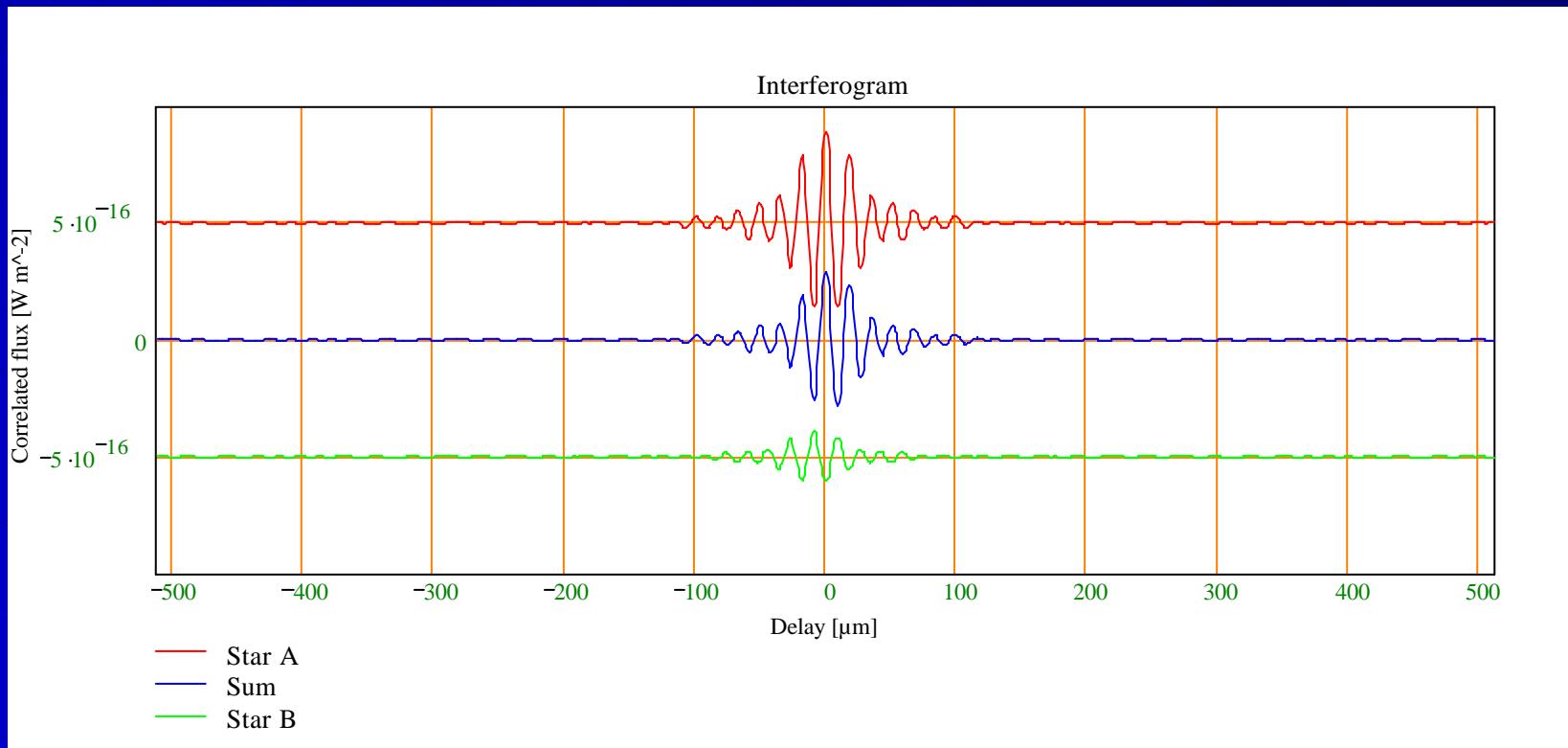


P_{raw}



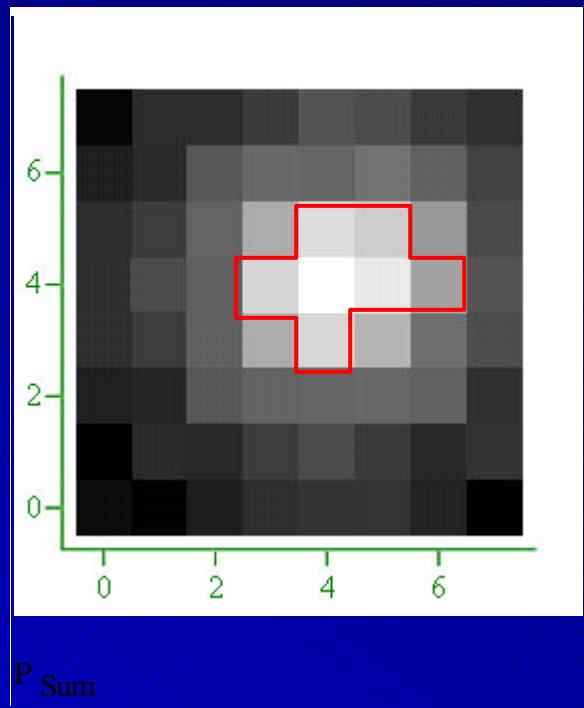
P_{2_B}

Full field interferograms

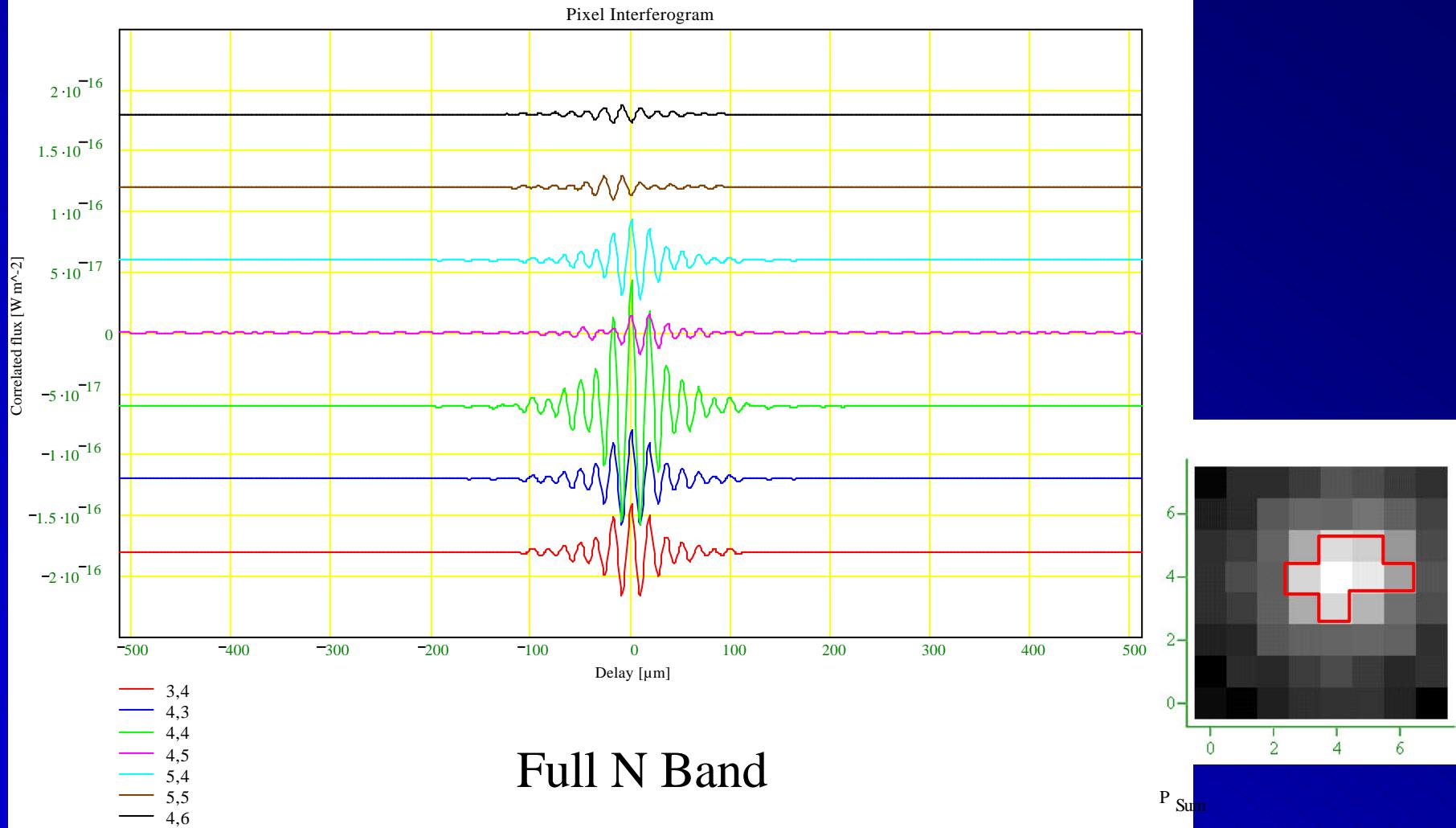


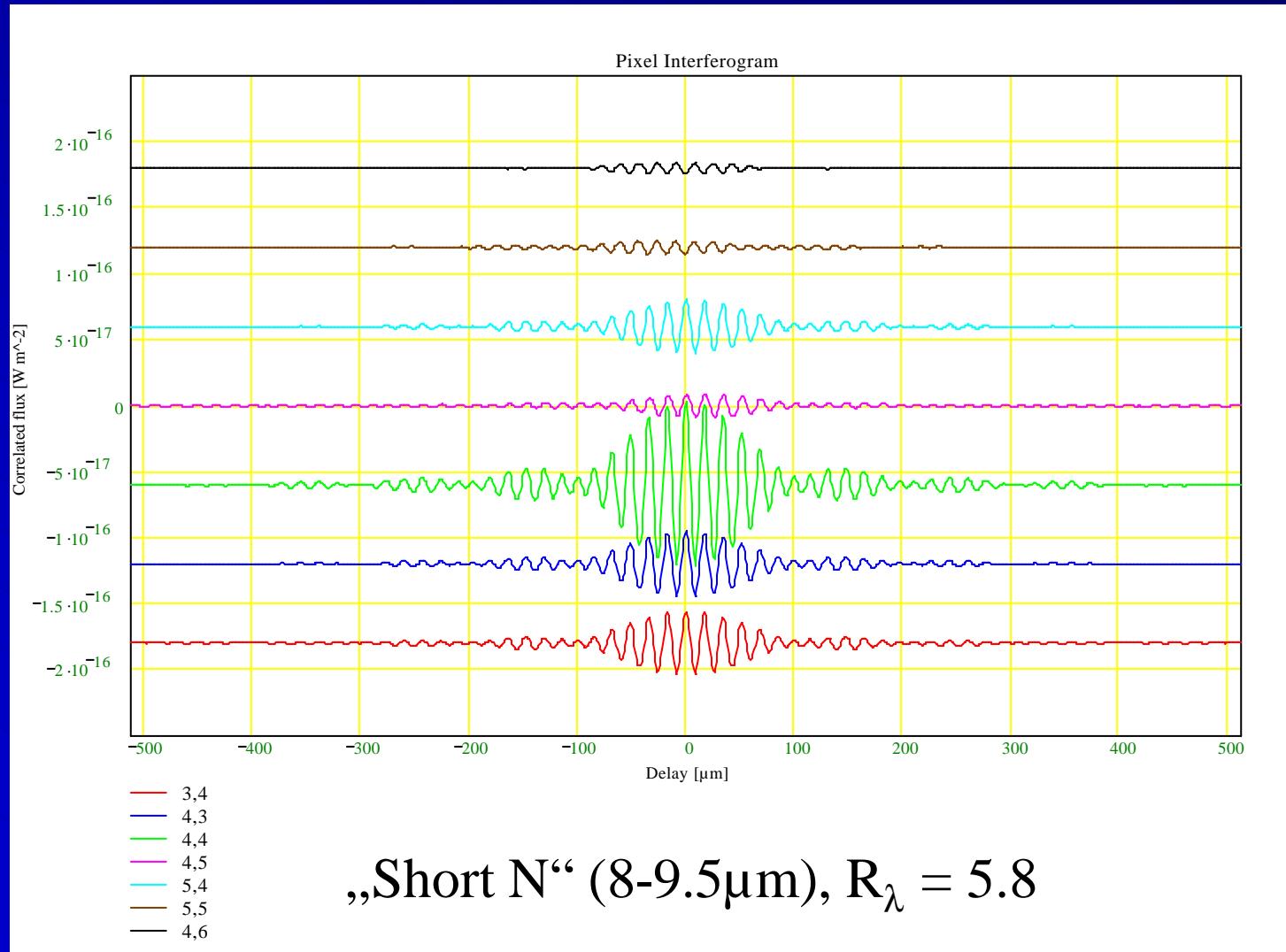
Detected Flux

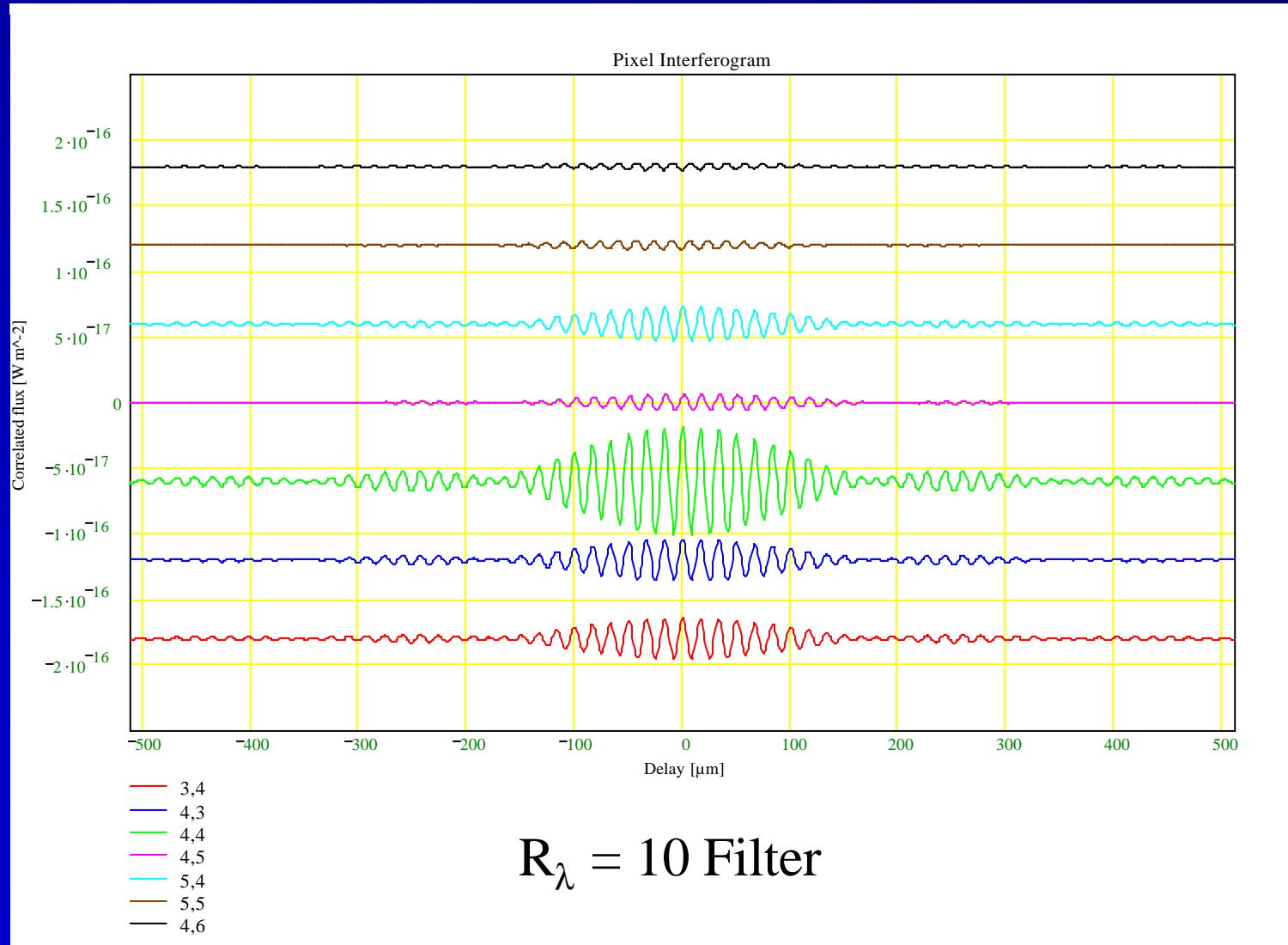
- Log Intensity
- Select seven brightest pixels
- Extract individual interferograms



P_{Sum}







Conclusions and Observations

- Very low R_λ ($<< 10$) measurements of MIDI should be analyzed with careful consideration of bandwidth effects
- There is no need to be concerned about differential delay in the MIDI FoV for higher R_λ
- Long stroke scanning (several 100 μm) enables quasi-simultaneous detection of fringes in an extended field („instantaneous mosaicing“)
- Single mode additions (pinholes, fibers) may just conceal problems