## WILKINSON MICROWAVE ANISOTROPY PROBE (WMAP) FIRST YEAR OBSERVATIONS: TE POLARIZATION

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## ABSTRACT

The Wilkinson Microwave Anisotropy Probe (WMAP) has mapped the full sky in Stokes I, Q, and U parameters at frequencies 23, 33, 41, 61, and 94 GHz. We detect correlations between the temperature and polarization maps significant at more than 10 standard deviations. The correlations are inconsistent with instrument noise and are significantly larger than the upper limits established for potential systematic errors. The correlations are present in all WMAP frequency bands with similar amplitude from 23 to 94 GHz, and are consistent with a superposition of a CMB signal with a weak foreground. The fitted CMB component is robust against different data combinations and fitting techniques. On small angular scales ( $\theta < 5^{\circ}$ ), the WMAP data show the temperature-polarization correlation expected from adiabatic perturbations in the temperature power spectrum. The data for  $\ell > 20$  agree well with the signal predicted solely from the temperature power spectra, with no additional free parameters. We detect excess power on large angular scales ( $\theta > 10^{\circ}$ ) compared to predictions based on the temperature power spectra alone. The excess power is well described by reionization at redshift  $11 < z_r < 30$  at 95% confidence, depending on the ionization history. A model-independent fit to reionization optical depth yields results consistent with the best-fit  $\Lambda$ CDM model, with best fit value  $\tau = 0.17 \pm 0.04$  at 68% confidence, including systematic and foreground uncertainties. This value is larger than expected given the detection of a Gunn-Peterson trough in the absorption spectra of distant quasars, and implies that the universe has a complex ionization history: WMAP has detected the signal from an early epoch of reionization.

#### 1. INTRODUCTION

Linear polarization of the cosmic microwave background (CMB) results from anisotropic Thomson scattering of CMB photons by free electrons. By symmetry, an isotropic radiation field can not generate a net polarization. Any net polarization results from the quadrupole moment of the CMB temperature distribution seen by each scatterer. Multiple scattering suppresses polarization by damping the temperature anisotropy; hence, CMB polarization originates primarily from epochs when the opacity was of order unity or less. Standard cosmological models predict two such epochs, corresponding to two characteristic angular scales. The first is the decoupling surface at redshift  $z \approx 1088$ , when the ionization fraction  $x_e$  abruptly falls from near unity to near zero. The acoustic horizon at decoupling subtends an angle  $\theta \approx 1^{\circ}$ ; polarization on these scales reflects conditions in the photon-baryon fluid just prior to recombination. Polarization data from decoupling complement measurements of the temperature anisotropy. Astrophysical sources generate additional polarization as ionizing radiation from the first collapsed objects reionizes the intergalactic medium. For reionization at redshift z < 50 the horizon is on large angular scales,  $\theta > 5^{\circ}$ . Polarization on these scales directly probes the poorlyunderstood process of reionization.

Since CMB polarization originates at modest opacity, the underlying temperature anisotropy is not heavily damped and remains observable today. Precise predictions can be made of the average polarization pattern expected from a given power spectrum of temperature anisotropy (Rees (1968); Kaiser (1983); Bond & Efstathiou (1984); Coulson et al. (1994); Kamionkowski et al. (1997); Zaldarriaga & Seljak (1997); Hu & White (1997); for recent reviews, see Kosowsky (1996); Hu & Dodelson (2002)). The pattern of polarization on the sky is a vector field with both an amplitude and direction at each point, and can

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be separated into two scalar fields, one giving the curl and the other the gradient component (called *B* and *E* modes in analogy with electromagnetic fields). The DASI collaboration has detected CMB polarization on angular scales  $\sim 0.5$  (Kovac et al. 2002). DASI reports an *E* mode signal significant at  $4.9\sigma$  and a TE temperature-polarization correlation significant at  $2\sigma$ . Both signals are consistent with the "concordance" cosmological model (spatially flat model dominated by a cosmological constant and cold dark matter; see, e.g., Hu & Dodelson (2002)) and support an adiabatic origin for the CMB temperature anisotropy.

The Microwave Anisotropy Probe has mapped the full sky in the Stokes I, Q, and U parameters on angular scales  $\theta > 0.2$  in 5 frequency bands centered at 23, 33, 41, 61, and 94 GHz (Bennett et al. 2003a). WMAP was not designed solely as a polarimeter, in the sense that none of its detectors are sensitive only to polarization. Incident radiation in each differencing assembly (DA) is split by an orthomode transducer (OMT) into two orthogonal linear polarizations (Page et al. 2003b; Jarosik et al. 2003). Each OMT is oriented so that the electric field directions accepted in the output rectangular waveguides lie at  $\pm 45^{\circ}$ with respect to the yz symmetry plane of the satellite (see Bennett et al. (2003a) Fig. 2 for the definition of the satellite coordinate system). The two orthogonal polarizations from the OMT are measured by two independent radiometers. Each radiometer differences the signal in the accepted polarization between two positions on the sky (the A and B beams), separated by  $\sim 140^{\circ}$ .

The signal from the sky in each direction  $\hat{n}$  can be decomposed into the Stokes parameters

$$T(\hat{n}) = I(\hat{n}) + Q(\hat{n})\cos 2\gamma + U(\hat{n})\sin 2\gamma, \qquad (1)$$

where we define the angle  $\gamma$  from a meridian through the Galactic poles to the projection on the sky of the E-plane of each output port of the OMT (Fig. 1). In principle, by tracking the orientation of the OMTs on the sky as the satellite scan pattern observes each sky pixel in different orientations, each radiometer could independently produce a map of the Stokes I, Q, and U parameters. In practice, the non-uniform coverage of  $\gamma$  at each pixel would generate significant correlations between the fitted Stokes parameters, allowing leakage of the dominant temperature anisotropy into the much fainter polarization maps. We avoid this problem by differencing the outputs of the two radiometers in each differencing assembly in the timeordered data. Denoting the two radiometers by subscripts 1 and 2, the instantaneous outputs are

and

$$\Delta T_2 = I(\hat{n}_A) - Q(\hat{n}_A)\cos 2\gamma_A - U(\hat{n}_A)\sin 2\gamma_A$$

 $-I(\hat{n}_B) - Q(\hat{n}_B)\cos 2\gamma_B - U(\hat{n}_B)\sin 2\gamma_B$ 

(2)

(3)

$$- \, I(\hat{n}_B) + Q(\hat{n}_B) \cos 2\gamma_B + U(\hat{n}_B) \sin 2\gamma_B.$$
 The sum

 $\Delta T_1 = I(\hat{n}_A) + Q(\hat{n}_A)\cos 2\gamma_A + U(\hat{n}_A)\sin 2\gamma_A$ 

$$\Delta T_I \equiv \frac{1}{2} (\Delta T_1 + \Delta T_2) = I(\hat{n}_A) - I(\hat{n}_B)$$

is thus proportional to the unpolarized intensity, while the difference

$$\Delta T_P \equiv \frac{1}{2} (\Delta T_1 - \Delta T_2)$$
  
=  $Q(\hat{n}_A) \cos 2\gamma_A + U(\hat{n}_A) \sin 2\gamma_A$   
-  $Q(\hat{n}_B) \cos 2\gamma_B - U(\hat{n}_B) \sin 2\gamma_B.$  (4)

is proportional only to the polarization. We produce fullsky maps of the Stokes I, Q, and U parameters from the sum and difference time-ordered data using an iterative mapping algorithm. Since the polarization is faint, the Q and U maps are dominated by instrument noise and converge rapidly (Hinshaw et al. 2003a).

The Stokes Q and U components depend on a specific choice of coordinate system. For each pair of pixels, we define coordinate-independent quantities

$$Q' = Q\cos(2\phi) + U\sin(2\phi)$$
$$U' = U\cos(2\phi) - Q\sin(2\phi), \tag{5}$$

where the angle  $\phi$  rotates the coordinate system about the outward-directed normal vector to put the meridian along the great circle connecting the two positions on the sky (Kamionkowski et al. 1997; Zaldarriaga & Seljak 1997). All of our analyses use these coordinate-independent linear combinations of the Q and U sky maps.

Simulations of the mapping algorithm demonstrate that WMAP can accurately recover the polarization pattern on the sky, even after allowing for residual calibration uncertainty in the individual radiometer channels. However, non-ideal instrumental signals affect the Q and U sky maps to a greater extent than the unpolarized I maps. The spacecraft spin about its z axis sweeps the beams across the sky in a direction 45° from the OMT orientation, preferentially coupling signals not fixed on the sky into the Umap. Residual striping exists to a lesser extent in the Iand Q maps. Systematic errors in the individual Q and U maps are not yet fully assessed; consequently, we defer detailed analysis of the Q or U maps to a later paper. Cross-correlations between maps are largely unaffected by striping or any other channel-specific signal, allowing much simpler analysis of the faint polarization signal than would be possible for the individual Q or U maps. This paper discusses the temperature-polarization (TE) correlation in the WMAP one-year sky maps.

We compute the temperature-polarization crosscorrelation using three different techniques: the two-point correlation function, a quadratic estimator for the power spectrum, and a "template" comparison in pixel space between the polarization maps and the predicted polarization given the observed pattern of temperature anisotropy. All three methods yield similar results despite disparate treatments of the data.

#### 2. CORRELATION FUNCTION

The simplest measure of temperature-polarization crosscorrelation is the two-point angular correlation function

$$C^{IQ}(\theta) = \frac{\sum_{ij} I_i Q'_j w_i w_j}{\sum_{ij} w_i w_j},$$
(6)

where i and j are pixel indices and w are the weights. To avoid residual effects of 1/f noise, we force the temperature map to come from a different frequency band than the polarization maps, and thus use the temperature map at 61 GHz (V band) for all correlations except the V-band polarization maps, which we correlate against the 41 GHz (Q band) temperature map. Since WMAP has a

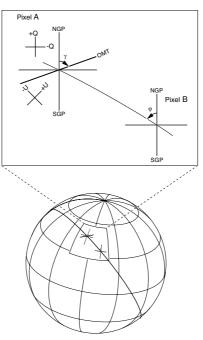


FIG. 1.— Geometry for Stokes Q and U parameters. WMAP measures polarization by differencing two orthogonal polarization channels, then solving for Q and U as the spacecraft compound spin projects the OMT onto the sky at different angles  $\gamma$  relative to the Galactic meridians. All analysis uses coordinate-independent quantities Q' and U' defined with respect to the great circle connecting a pair of pixels (see text).

high signal-to-noise ratio measurement of the CMB temperature anisotropy, we use unit weight  $(w_i = 1)$  for the temperature maps and noise weight  $(w_j = N_j / \sigma_0^2)$  for the polarization maps, where  $N_j$  is the effective number of observations in each pixel j and  $\sigma_0$  is the standard deviation of the white noise in the time-ordered data (Table 1 of Bennett et al. (2003b)). We compare the correlation functions to Monte Carlo simulations of a null model, which simulates the temperature anisotropy using the best-fit  $\Lambda$ CDM model (Spergel et al. 2003) but forces the polarization signal to zero. Each realization generates a CMB sky in Stokes I, Q, and U parameters, convolves this simulated sky with the beam pattern for each differencing assembly, then adds uncorrelated instrument noise to each pixel in each map. We then co-add the simulated skies in each frequency band and compute  $C^{IQ}(\theta)$  using the same software for both the WMAP data and the simulations. All analysis uses only pixels outside the WMAP Kp0 foreground emission mask (Bennett et al. 2003c), approximately 76% of the full sky.

Figure 2 shows  $C^{IQ}(\theta)$  derived by co-adding the individual correlation functions for the frequencies 41, 61, and 94 GHz (Q, V, and W bands) least likely to be affected by Galactic foregrounds. The grey band shows the 68% confidence interval for the null simulations. It is clear that WMAP detects a temperature-polarization signal at high statistical confidence, and that signals exist on both large and small angular scales. We define a goodness-of-fit statistic

$$\chi^2 = \sum_{ab} [C_{\text{MAP}}^{IQ} - \langle C_{\text{sim}}^{IQ} \rangle]_a \ \mathbf{M}_{ab}^{-1} \ [C_{\text{MAP}}^{IQ} - \langle C_{\text{sim}}^{IQ} \rangle]_b, \ (7)$$

where  $C_{\text{MAP}}^{IQ}$  is the co-added correlation function from WMAP data,  $\langle C_{\text{sim}}^{IQ} \rangle$  is the mean from the Monte Carlo simulations, and **M** is the covariance matrix between angular bins *a* and *b* derived from the simulations. We

find  $\chi^2 = 207$  for 78 degrees of freedom when comparing WMAP to the null model: WMAP detects temperaturepolarization correlations significant at more than 10 standard deviations.

## 2.1. Systematic Error Analysis

Having detected a significant signal in the data, we must determine whether this signal has a cosmological origin or results from systematic errors or foreground sources. We test the convergence of the mapping algorithm using end-to-end simulations, comparing maps derived from simulated time-ordered data to the input maps used to generate the simulated time series. The simulations include all major instrumental effects, including beam ellipticity, radiometer performance, and instrument noise (including 1/f component), and are processed using the same map-making software as the WMAP data (Hinshaw et al. 2003a). The Q and U maps converge rapidly, within the 30 iterations required to derive the calibration solution. Correlations in the time-ordered data introduce an anti-correlation in the U map at angles corresponding to the beam separation, with amplitude 0.5% of the noise in the map. This effect is independent for each radiometer and does not affect temperature-polarization crosscorrelations. Similarly, residual 1/f noise in the time series can create faint striping in the maps, but does not affect cross-correlations.

The largest potential systematic error in the temperature-polarization cross-correlation results from bandpass mismatches in the amplification/detection chains. We calibrate the WMAP data in thermodynamic temperature using the Doppler dipole from the satellite's orbit about the Sun as a beam-filling calibration source (Hinshaw et al. 2003a). Astrophysical sources with a

FIG. 2.— Temperature-polarization correlation function for WMAP co-added QVW data. The gray band shows the 68% confidence interval for similar co-added data taken from Monte Carlo simulations without polarization. The inset shows data for  $\theta < 10^{\circ}$ . The data are inconsistent with no temperature-polarization cross-correlations at more than 10 standard deviations. Note that the data are not independent between angular bins.

spectrum other than a 2.7 K blackbody are thus slightly mis-calibrated. The amplitude is dependent on the product of the source spectrum with the unique bandpass of each radiometer. If the bandpasses in each radiometer were identical, the effect would cancel for any frequency spectrum, but differences in the bandpasses between the two radiometers in each DA generate a non-zero residual in the difference signal used to generate polarization maps (Eq. 4). This signal is spatially correlated with the unpolarized foreground intensity but is independent of the orientation of the radiometers on the sky (polarization angle  $\gamma$ ). In the limit of uniform sampling of  $\gamma$  this term drops out of the sky map solution. However, the WMAP scan pattern does not view each pixel in all orientations; unpolarized emission with a non-CMB spectrum can thus be aliased into polarization if the bandpasses of the two radiometers in each DA are not identical. This is a significant problem only at 23 GHz (K band), where the foregrounds are brightest and the bandpass mismatch is largest.

We quantify the effect of bandpass mismatch using endto-end simulations. For each time-ordered sample, we compute the signal in each radiometer using an unpolarized foreground model and the measured pass bands in each output channel (Jarosik et al. 2003). We then generate maps from the simulated data using the WMAP one-

Difference Map<sup>c</sup>

**Probability**<sup>d</sup>

0.26

0.22

0.95

0.95

2

23.6

66.0

10.8

50.4

TABLE 1 NULL TESTS FOR IQ AND IU SUM AND DIFFERENCE DATA<sup>a</sup>

2

62.1

145.1

30.9

66.1

Sum Map<sup>b</sup>

Probability<sup>d</sup>

 $3 \times 10^{-6}$ 

 $2 \times 10^{-9}$ 

0.06

0.22

$^{a}\chi^{2}$ comparison of the WMAP correlation functions $C^{IQ}(\theta)$ and $C^{IU}(\theta)$ to a null hypothesis of CMB temperature anisotropy and instrument
noise, but no polarization. Temperature-polarization signals of cosmic origin should contribute to only $C^{IQ}(\theta)$ in the sum maps. All other
tests are consistent with the null hypothesis.

<sup>b</sup>Polarization sum maps (Q1+Q2)/2, (V1+V2)/2, (W1+W2)/2, and (W3+W4)/2 co-added with noise weights.

DOF

20

58

20

58

Range

 $\theta < 5^{\circ}$ 

 $\theta \geq 5^{\circ}$ 

 $\theta < 5^\circ$ 

 $\theta \ge 5^{\circ}$ 

<sup>c</sup>Polarization difference maps (Q1-Q2)/2, (V1-V2)/2, (W1-W2)/2, and (W3-W4)/2 co-added with noise weights.

<sup>d</sup>Probability to randomly obtain  $\chi^2$  larger than the measured value.

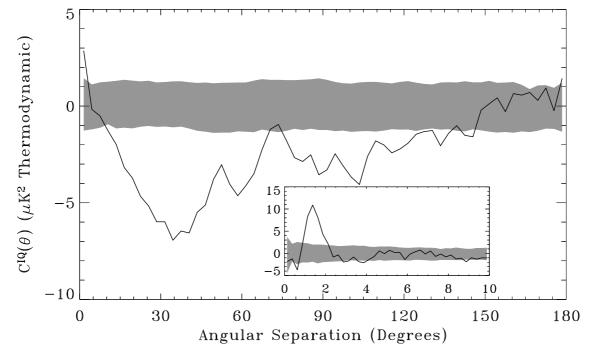
Correlation

IQ

IQ

IŪ

IU



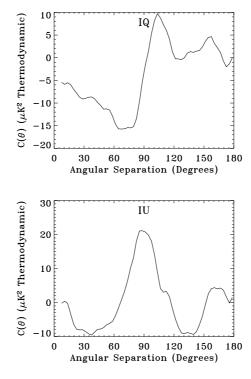


FIG. 3.— Angular templates for potential systematic errors caused by bandpass mismatch between the 2 radiometers in each differencing assembly. We fit this template to the correlation functions from each DA to detect or limit systematic errors related to bandpass mismatch in the main beam. The effect is significant only in K and Ka bands, which have the brightest unpolarized foregrounds.

year sky coverage and compute  $C^{IQ}(\theta)$  using the output I, Q, and U maps from the simulation. Figure 3 shows the predicted signal at K band. We treat this as an angular template and compute the least-squares fit of the WMAP data to this bandpass template to determine the amplitude of the effect in the observed correlation functions. We correct the WMAP correlation functions  $C^{IQ}(\theta)$  and  $C^{IU}(\theta)$  at K and Ka bands by subtracting the best-fit template amplitudes. The fitted signal has peak amplitude of 8  $\mu$ K<sup>2</sup> at 23 GHz and 5  $\mu$ K<sup>2</sup> at 33 GHz. No other channel has a statistically significant detection of this effect.

Sidelobe pickup of polarized emission from the Galactic plane can also produce spurious polarization at high latitudes in the Q and U maps. We estimate this effect using the measured far-sidelobe response for each beam in each polarization (Barnes et al. 2003). The simplest approach would be to estimate the signal in each timeordered sample, convolving the full sky sidelobe response with the Stokes I, Q, and U maps given the instantaneous orientation of the beams for each sample. Such an approach is computationally expensive. We instead approximate the signal in each pixel by convolving the full sky sidelobe response with the one-year Q and U maps. For each pixel, we fix one beam on that pixel while sweeping the other beam through all orientations achieved in flight. The average from the convolution yields the sidelobe contribution for the pixel in question. Details of the sidelobe maps are presented in Barnes et al. (2003). We correlate the sidelobe maps with the temperature anisotropy maps in each channel to estimate the systematic error in the temperature-polarization correlation. Sidelobe pickup of polarized structure in the Galactic plane is less than 1

 $\mu K^2$  in  $C^{IQ}(\theta)$  at 23 GHz and below 0.1  $\mu K^2$  in all other bands. The effect of bandpass mismatch in the far sidelobes (as opposed to the main beam) is similarly weak, with limits 1.3  $\mu K^2$  at 23 GHz and less than 0.05  $\mu K^2$  in all other bands. We do not apply any corrections for these effects, but simply propagate the associated systematic uncertainty throughout our analysis. Note that all of these systematic errors depend on the Galactic foregrounds, and have different frequency dependence than CMB polarization.

Null tests provide an additional check for systematic errors. Thomson scattering of scalar temperature anisotropy produces a curl-free polarization pattern. A non-zero cosmological signal is thus expected only for the IQ (TE) correlation, whereas systematic errors or foreground sources can affect both the IQ and IU (TB) correlations. We also test linear combinations of radiometer maps which cancel the polarization signal but which test for systematic effects. We compute the IQ and IU correlation functions by correlating the Stokes I sum map from the Qor V-band (as noted above) with the polarization difference maps (Q1-Q2)/2, (V1-V2)/2, (W1-W2)/2, and (W3-W4)/2. We then co-add the results with their noise weights, and compare the co-added result for the polarization difference maps to a similar computation for the polarization sum maps. The temperature (Stokes I) map in all cases is a sum map; the test is thus primarily sensitive to systematic errors in the polarization data.

Table 1 shows results of the null tests. We compare  $C^{IQ}(\theta)$  and  $C^{IU}(\theta)$  for the sum and difference maps to a null hypothesis that the data consist of Stokes I and instrument noise, with no polarization in the Stokes Q or U

FIG. 4.— Fitted CMB (left) and foreground (right) components from a multi-frequency decomposition of the measured two-point correlation functions. Top panels show the IQ (TE) correlation, while bottom panels show IU (TB). The CMB component is shown in units of thermodynamic temperature, while the foreground is shown in antenna temperature evaluated at 41 GHz. The best-fit spectral index is  $\beta = -2.7 \pm 0.3$ . The fitted CMB and foreground components are stable as additional low-frequency data are included in the fit.

maps. We break the data into 2 angular regimes to differentiate between signals at decoupling vs reionization. We find a clear signal detection for  $C^{IQ}(\theta)$  in the sum map for both angular scales. All other tests are consistent with instrument noise – there is no evidence for additional systematic errors in the temperature-polarization cross-correlation.

## 2.2. Foregrounds

Galactic emission is not a strong contaminant for CMB temperature anisotropy, but could be significant in polarization. WMAP measurements of unpolarized foreground emission show synchrotron, free-free, and thermal dust emission all sharing significant spatial structure (Bennett et al. 2003c). Of these components, only synchrotron emission is expected to generate significant polarization; other polarized sources such as spinning dust are limited to less than 5% of the total intensity at 33 GHz.

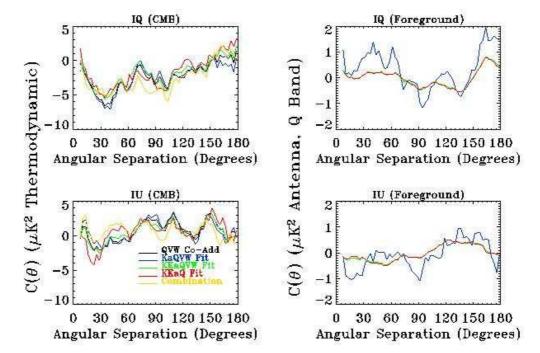
Synchrotron emission from electrons accelerated in the Galactic magnetic field is the dominant unpolarized foreground at frequencies below ~50 GHz. Although it is known to be linearly polarized, previous radio surveys provide little guidance for the high-latitude polarization at mm wavelengths. Extrapolation of radio polarization maps (Brouw & Spoelstra 1976) to millimeter wavelengths indicate a polarization fraction between 10% and 50% depending on Galactic latitude (Lubin & Smoot 1981). The unpolarized component has a steep angular dependence, with power spectrum  $c_{\ell} \propto \ell^{-2}$  (Bennett et al. 2003c). The angular dependence of the *polarized* component is expected to be even steeper (Baccigalupi et al. 2001; Bruscoli et al. 2002; Tucci et al. 2002), suggesting that foreground polarization is most likely to affect results on large angular scales. Radio maps at low Galactic latitude, however, demonstrate that the polarization intensity is not necessarily well correlated with the unpolarized intensity, complicating template analysis for temperature-polarization cross-correlations (Uyanıker et al. 1998, 1999). We thus use the frequency dependence of the measured temperature-polarization crosscorrelation to separate cosmic from foreground signals.

Foreground polarization above 40 GHz is faint: fitting the correlation functions at 41, 61, and 94 GHz (Q, V, and W bands) to a single power-law  $C^{IQ}(\theta, \nu) = C_0^{IQ}(\theta) (\nu/\nu_0)^{2\beta}$  yields spectral index  $\beta = -0.4 \pm 0.4$ , consistent with a CMB signal ( $\beta = 0$ ) and inconsistent with the spectral indices expected for synchrotron ( $\beta \approx -3$ ), spinning dust ( $\beta \approx -2$ ), or thermal dust ( $\beta \approx 2$ ). The measured signal can not be produced solely by foreground emission.

A two-component fit

$$C^{IQ}(\theta,\nu) = C^{IQ}_{\text{CMB}}(\theta) + C^{IQ}_{\text{Gal}}(\theta) \left(\frac{\nu}{\nu_0}\right)^{2\beta}$$
(8)

tests for the superposition of a CMB component with a single foreground component. Figure 4 shows the resulting decomposition for different combinations of WMAP frequency channels. We detect foreground components in both IQ and IU, with best-fit spectral index  $\beta = -2.4 \pm 0.4$ 



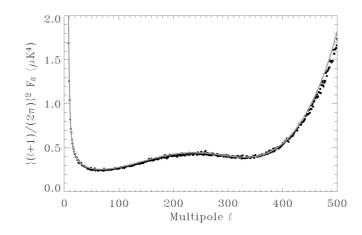


FIG. 5.— Diagonal elements of the covariance matrix for the  $c_l^{TE}$  polarization cross-power spectrum. Points show the diagonal elements computed from 7500 Monte Carlo simulations. The solid line shows the analytical model (Eq. 10). Note we multiply  $\mathbf{M}_{ll}$  by  $[(l+1)/(2\pi)]^2$  to match the units in Figures 7 and 8.

for IQ and  $\beta = -3.0 \pm 0.4$  for IU. It is likely that a single foreground component is responsible for the signal in both IQ and IU; a joint fit yields  $\beta = -2.7 \pm 0.3$  with approximately equal amplitudes (at large angular scales) in curland curl-free modes,  $0.5 \pm 0.1 \ \mu K^2$  at  $\nu_0 = 41$  GHz. The foreground detection does not depend solely on the 23 GHz data; we obtain similar (albeit noisier) results excluding the 23 GHz data from the fit. The fitted index is consistent with an origin from polarized synchrotron emission, and supports a picture in which we correlate polarized synchrotron emission with the total Galactic foreground, since the synchrotron, free-free, and dust morphologies trace each other to a great extent (Bennett et al. 2003c). It is thus not too surprising to find the best-fit foreground index in the temperature-polarization cross-correlation to be somewhat flatter than the spectral index for the synchrotron component alone.

The fitted CMB component is robust against all combinations of frequency channels and fitting techniques. Note the agreement in Fig 4 between nearly independent data sets: the co-added QVW data (uncorrected for foreground emission) and the KKaQ data (corrected for foreground emission). We obtain additional confirmation by correlating I, Q, and U maps derived from a linear combination of the WMAP frequency channels designed to suppress foreground emission. We compute  $C^{IQ}(\theta)$  using the "internal" linear combination I map of Bennett et al. (2003c), and similar minimum-variance linear combinations for the Qand U maps. The result is nearly identical to the CMB component derived from Eq. 8.

## 3. POLARIZATION CROSS-POWER SPECTRA

In a second analysis method, we compute the angular power spectrum of the temperature-polarization correlations using a quadratic estimator (Appendix A). The power spectrum is the Legendre transform of the two-point correlation function, and is more commonly encountered for theoretical predictions. We compute  $c_l^{TE}$  and  $c_l^{TB}$  individually for the each WMAP frequency band, using uniform weight for the temperature map and noise weight for the polarization maps. We then combine the angular power spectra, using noise-weighted QVW data for l > 21where foregrounds are insignificant, and a fit to CMB plus foregrounds using all 5 frequency bands for  $l \leq 21$ . Since foreground contamination is weak, we gain additional sensitivity in this analysis by using the Kp2 sky cut retaining 85% of the sky.

We estimate the uncertainty in each l bin using the covariance matrix **M** for the polarization cross-power spectrum. Based on our analysis of the  $c_l^{TT}$  covariance matrix (Hinshaw et al. 2003b), the  $c_l^{TE}$  covariance matrix has the form along the diagonal of

$$\mathbf{M}_{ll} = \langle c_l^{TE} c_l^{TE} \rangle - \langle c_l^{TE} \rangle^2$$
(9)  
$$\simeq \frac{(c_l^{TT} + n_{TT}/w_l)(c_l^{EE} + n_{EE}/w_l) + (c_l^{TE})^2}{(2l+1)f_{sky}f_{sky}^{\text{eff}}}$$
(10)

where  $n_{TT}$  and  $n_{EE}$  are the TT and EE noise bias terms,  $w_l$  is the effective window function for the combined maps (Page et al. 2003a),  $c_l^{TT}$  and  $c_l^{EE}$  are the temperature and polarization angular power spectra,  $f_{sky} = 0.85$  is the fractional sky coverage for the Kp2 mask, and  $f_{sky}^{\text{eff}} = f_{sky}/1.14$  for noise weighting. Figure 5 compares the analytic expression for the diagonal elements of the covariance matrix to the mean derived from 7500 Monte Carlo simulations. The analytic form (Eq. 10) accurately describes the simulations. We approximate the off-diagonal terms using the geometric mean of the covariance matrix terms for uniform and noise weighting (Hinshaw et al. 2003b),<sup>10</sup>

$$\mathbf{M}_{ll'} \simeq (\mathbf{M}_{ll} \mathbf{M}_{l'l'})^{0.5} r_{\Delta l}.$$
(11)

Figure 6 shows the off-diagonal terms  $r_{\Delta l}$  measured from Monte Carlo simulations. The largest contribution, -2.8%, is at  $\Delta l = 2$  from the symmetry of our sky cut and noise coverage. The total anticorrelation is

<sup>10</sup> Note that Hinshaw et al. (2003b) define off-diagonal elements in terms of the inverse covariance matrix, which differs from  $r_{\Delta l}$  by a sign.

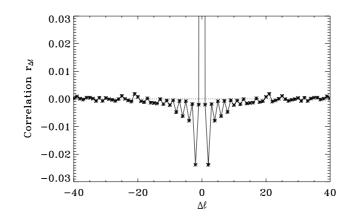


FIG. 6.— Off-diagonal correlations  $r_{\Delta l}$  in the covariance matrix for the  $c_l^{TE}$  polarization cross-power spectrum, computed from simulations. All values are normalized to  $r_{\Delta l} = 1$  at  $\Delta l = 0$ . The dotted line shows  $r_{\Delta l} = 0$  for comparison. The anti-correlation at  $\Delta l = 2$  results from the spatial symmetry of the sky cut and noise coverage.

 $\sum_{\Delta l \neq 0} r_{\Delta l} = -0.124$ . Because of this anti-correlation, the error bars for the binned  $c_l^{TE}$  are slightly smaller than the naive estimate. A second method of estimating the errors relies on end-to-end simulations derived from simulated time-ordered data consisting solely of instrument noise (including the estimated contribution from 1/f fluctuations). We have generated 11 "noise" sky maps each in Stokes I, Q, and U and compute the variance in TE directly from the variance in the simulated signal. These two approaches yield errors that are consistent to better than 5%.

Figure 7 shows the polarization cross-power spectra for the WMAP one-year data. The solid line shows the predicted signal for adiabatic CMB perturbations, based only on a fit to the measured temperature angular power spectrum  $c_l^{TT}$  (Spergel et al. 2003; Hinshaw et al. 2003b). Two features are apparent. The TE data on degree angular scales (l > 20) are in excellent agreement with a priori predictions of adiabatic models (Coulson et al. 1994). Other than the specification of adiabatic perturbations, there are no free parameters – the solid line is not a fit to  $c_l^{TE}$ . The  $\chi^2$  of 24.2 for 23 degrees of freedom indicates that the CMB anisotropy is dominated by adiabatic perturbations. On large angular scales (l < 20) the data show excess power compared to adiabatic models, suggesting significant reionization.

The WMAP detection of the acoustic structure in the TE spectrum confirms several basic elements of the standard paradigm. The amplitudes of the peak and anti-peak are a measure of the thickness of the decoupling surface, while the shape confirms the assumption that the primordial fluctuations are adiabatic. Adiabatic fluctuations predict a temperature/polarization signal anticorrelated on large scales, with TE peaks and anti-peaks located midway between the temperature peaks Hu & Sugiyama (1994). The existence of TE correlations on degree angular scales also provides evidence for super-horizon temperature fluctuations at decoupling, as expected for inflationary models of cosmology (Peiris et al. 2003)

#### 4. TEMPLATE POWER SPECTRA

Figure 7 demonstrates that the power spectrum of temperature-polarization correlations on degree angular scales can be predicted using the power spectrum of the temperature fluctuations alone. We use this for a third derivation of the TE cross-power spectrum, based on template matching in pixel space. On large angular scales, the signal-to-noise ratio for the temperature maps is much larger than one per multipole, while the S/N ratio for the polarization is much less than one. The likelihood function for the polarization measurement then has the simple form

$$\log \mathcal{L} = (\hat{P} - \sum_{l} \alpha_l \hat{P}_{\text{pred}}^l)^T N^{-1} (\hat{P} - \sum_{l} \alpha_l \hat{P}_{\text{pred}}^l), \quad (12)$$

where  $\hat{P}$  is the measured polarization signal (a 2  $N_{\text{pixel}}$  vector),  $\alpha_l = c_l^{TE}/c_l^{TT}$  is the polarization fraction at each l, N is the pixel noise correlation matrix (a  $2N_{\text{pixel}} \times 2N_{\text{pixel}}$  matrix) and

$$Q_{pred}^{l}(\hat{n}) = \sum_{m} a_{lm} ({}_{2}Y_{lm}(\hat{n}) + {}_{-2}Y_{lm}(\hat{n}))$$
$$U_{pred}^{l}(\hat{n}) = i \sum_{m} a_{lm} ({}_{2}Y_{lm}(\hat{n}) - {}_{-2}Y_{lm}(\hat{n})).$$
(13)

Here  $\pm_2 Y_{lm}(\hat{n})$  are the spin harmonics, while  $a_{lm}$  are the measured coefficients for an all-sky map of the CMB temperature. Imposing a cut to mask the Galactic plane introduces additional correlations; we avoid this by using the "internal" linear combination temperature map (Bennett et al. 2003c) without imposing a sky cut.

The maps  $Q_{pred}$  and  $U_{pred}$  represent the predicted polarization pattern based on the observed pattern of temperature anisotropy. We fit these template maps to the observed Q and U polarization maps to derive the polarization fraction  $\alpha_l$  and thus the  $c_l^{TE}$  polarization cross-power spectrum. Minimizing the likelihood function yields the normal equations

$$K_{ll'}\alpha_{l'} = y_l,\tag{14}$$

where

and

$$y_l = \hat{P} N^{-1} \hat{P}_{pred}^l \tag{15}$$

 $K_{ll'} = \hat{P}_{pred}^{l} N^{-1} \hat{P}_{pred}^{l'}.$  (16)

These equations show the advantages of this approach. We compare the data with a template in pixel space, making

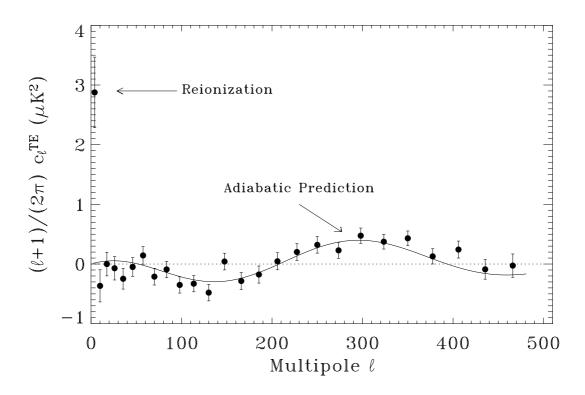


FIG. 7.— Polarization cross-power spectra  $c_{\ell}^{TE}$  for the WMAP one-year data. Note that we plot  $(l+1)/2\pi c_{l}^{TE}$  and not  $l(l+1)/2\pi c_{l}^{TE}$ . This choice emphasizes the oscillatory nature of  $c_{\ell}^{TE}$ . For clarity, the dotted line shows  $c_{l} = 0$ . The solid line is the predicted signal based on the  $c_{\ell}^{TT}$  power spectrum of temperature anisotropy – there are no free parameters. The TE correlation on degree angular scales (l > 20) is in excellent agreement with the signal expected from adiabatic CMB perturbations. The excess power at low l indicates significant reionization at large angular scales.

it straightforward to include a spatially varying noise signal. We directly compare the measured polarization maps to a prediction based on the measured temperature maps, yielding a measurement of the TE polarization cross-power spectrum in the observed sky unaffected by cosmic variance. We can thus more easily compute the errors on the measured polarization fraction. The input temperature map (Stokes I) is already corrected for foreground emission (much simpler in pixel space where the unpolarized foregrounds are more easily measured), greatly reducing the foreground contribution to the cross-power spectra.

We thus compute the temperature-polarization crosscorrelation using three disparate techniques: the two-point angular correlation function, a quadratic estimator for the power spectrum in Fourier space, and a template fit in pixel space. All methods are in good agreement despite their very dissimilar treatment of the data. All methods show a significant excess of power for l < 10.

# 5. REIONIZATION

WMAP detects statistically significant correlations between the CMB temperature and polarization. The signal on degree angular scales (l > 20) agrees with the signal expected in adiabatic models based solely on the temperature power spectrum, without any additional free parameters. We also detect power on large angular scales (l < 10) well in excess of the signal predicted by the temperature power spectrum alone. This signal can not be explained by data processing, systematic errors, or foreground polarization, and has a frequency spectrum consistent with a cosmological origin.

The signal on large angular scales has a natural interpretation as the signature of early reionization.<sup>11</sup> Both the temperature and temperature-polarization power spectra can be related to the power spectrum of the radiation field during scattering (Zaldarriaga 1997). Thomson scattering damps the temperature anisotropy and regenerates a polarized signal on scales comparable to the horizon. The existence of polarization on scales much larger than the acoustic horizon at decoupling implies significant scattering at more recent epochs.

## 5.1. Reionization in a $\Lambda CDM$ Universe

If we assume that the  $\Lambda$ CDM model is the best description of the physics of the early universe, we can fit the observed temperature-polarization cross-power spectrum to derive the optical depth  $\tau$ . We assume a step function for the ionization fraction  $x_e$  and use the CMBFAST code (Seljak & Zaldarriaga 1996) to predict the multipole moments as a function of optical depth. While this assumption is simplistic, our conclusions on optical depth are not very sensitive to details of the reionization history

<sup>11</sup> Although tensor modes can also generate TE correlations at large angular scales, tensor-to-scalar ratios r large enough to fit the WMAP TE data are ruled out by the WMAP TT data (Spergel et al. 2003).

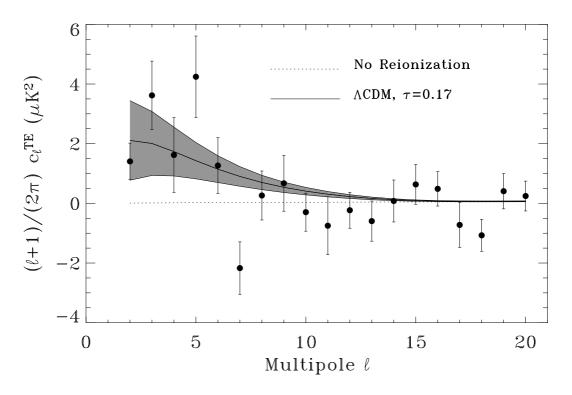


FIG. 8.— WMAP Polarization cross-power spectra  $c_{\ell}^{TE}$  (filled circles) compared to  $\Lambda$ CDM models with and without reionization. The rise in power for l < 10 is consistent with reionization optical depth  $\tau = 0.17 \pm 0.04$ . The error bars on WMAP data reflect measurement errors only; adjacent points are slightly anti-correlated. The grey band shows the 68% confidence interval from cosmic variance. The value at l = 7is particularly sensitive to the foreground correction.

or the background cosmology.

Figure 8 compares the polarization cross-power spectrum  $c_l^{TE}$  derived from the quadratic estimator to  $\Lambda$ CDM models with and without reionization. The rise in power for l < 10 is clearly inconsistent with no reionization. We quantify this using a maximum-likelihood analysis

$$\mathcal{L} \propto \frac{\exp(-\frac{1}{2}\chi^2)}{|\mathbf{M}|^{1/2}}.$$
(17)

Figure 9 shows the relative likelihood  $\mathcal{L}/\text{Max}(\mathcal{L})$  for the optical depth  $\tau$  assuming a  $\Lambda$ CDM cosmology, with all other parameters fixed at the values derived from the temperature power spectrum alone (Spergel et al. 2003). The likelihood for the 5-band data corrected for foreground emission peaks at  $\tau = 0.17 \pm 0.03$  (statistical error only): WMAP detects the signal from reionization at high statistical confidence.

A full error analysis for  $\tau$  must account for systematic errors and foreground uncertainties. We propagate these effects by repeating the maximum likelihood analysis using different combinations of WMAP frequency bands and different systematic error corrections. We correct  $C^{IQ}(\theta)$ in each frequency band not for the best estimate of the systematic error templates, but rather the best estimate plus or minus one standard deviation. We then fit the miscorrected  $C^{IQ}(\theta, \nu)$  for a CMB piece plus a foreground piece (Eq. 8) and use the CMB piece in a maximumlikelihood analysis for  $\tau$ . The change in the best-fit value for  $\tau$  as we vary the systematic error corrections propagates the uncertainties in these corrections. Systematic errors have a negligible effect on the fitted optical depth; altering the systematic error corrections changes the best-fit values of  $\tau$  by less than 0.01.

The largest non-random uncertainty is the foreground separation. We assess the uncertainty in the foreground separation by repeating the entire systematic error analysis (using both standard and altered systematic error corrections) with the foreground spectral index  $\beta = -2.7 \pm 0.3$ shifted one standard deviation up or down from the bestfit value. Table 2 shows the fitted optical depth  $\tau$  and goodness-of-fit statistic  $\chi^2$  for different data combinations and foreground spectral indices derived from the analysis of the two-point correlation function  $C^{IQ}(\theta)$ . The first set of rows shows values derived by simply co-adding the WMAP frequency channels, without any correction for foregrounds. Data at 41, 61, and 94 GHz (Q, V, and W bands) where foregrounds are negligible show similar values for  $\tau$ ; the  $\chi^2 \approx 63$  for 57 degrees of freedom indicates that the data are in excellent agreement with reionized models. Adding additional low-frequency channels reduces the formal statistical uncertainty, but introduces non-zero foreground contamination as shown by the marked increase in  $\chi^2$ . The next three sets of rows show the results when the data are separated into CMB and foreground components (Eq. 8). All data combinations are now in agreement; we obtain nearly identical values for  $\tau$  when fitting either the highest-frequency data set QVW or the lowest-frequency set KKaQ. The fitted optical depth is insensitive to the spectral index: varying the

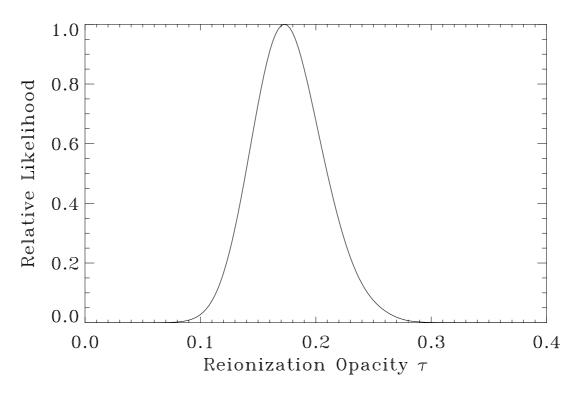


FIG. 9.— Likelihood function for optical depth  $\tau$  for a  $\Lambda$ CDM cosmology, using all 5 WMAP frequency bands fitted to CMB plus foregrounds with foreground spectral index  $\beta = -2.7$ . The best-fit value is  $\tau = 0.17$  with 95% confidence range  $0.09 \le \tau \le 0.28$  after including systematic and foreground uncertainaties.

spectral index from -2.4 to -3.0 changes the fitted values by 0.02 or less. We adopt  $\tau = 0.17 \pm 0.04$  as the best estimate for the optical depth to reionization, where the error bar reflects a 68% confidence level interval including statistical, systematic, and foreground uncertainties.

Spergel et al. (2003) include the TE data in a maximumlikelihood analysis combining WMAP data with other astronomical measurements. The resulting value,  $\tau = 0.17 \pm 0.06$ , is consistent with the value derived from the TE data alone. The larger uncertainty reflects the effect of simultaneously fitting multiple parameters. The TE analysis propagates foreground uncertainties by re-evaluating the likelihood using different foreground spectral index. Since foreground affect only the lowest multipoles, the combined analysis propagates foreground uncertainty by doubling the statistical uncertainty in  $c_l^{TE}$  for  $2 \le l \le 4$ to account for this effect.

# 5.2. Model-Independent Estimate

An alternative approach avoids assuming any cosmological model and uses the measured temperature angular correlation function to determine the radiation power spectrum at recombination. This approach assumes that the best estimate of the three dimensional radiation power spectrum is the *measured* angular power spectrum rather than a model fit to the angular power spectrum. Given the observed temperature power spectrum  $c_l^{TT}$ , we derive the predicted polarization cross-power spectrum  $c_l^{TE}$ (§4), which we then fit to the observed TE spectrum as a function of optical depth  $\tau$ . We obtain  $\tau = 0.16 \pm 0.04$ , in excellent agreement with the value derived assuming a ACDM cosmology. We emphasize that the modelindependent technique makes *no* assumptions about the cosmology. The fact that it agrees well with the bestfit model from the combined temperature and polarization data (Spergel et al. 2003) is an additional indication that the observed temperature-polarization correlations on large angular scales represent the imprint of physical conditions at reionization. The dependence on the underlying cosmology is small.

## 5.3. Early Star Formation

Reionization can also be expressed as a redshift  $z_r$  assuming an ionization history. We consider two simple cases. For instantaneous reionization with ionization fraction  $x_e = 1$  at  $z < z_r$ , the measured optical depth corresponds to redshift  $z_r = 17 \pm 3$ . This conflicts with measurements of the Gunn-Peterson absorption trough in spectra of distant quasars, which show neutral hydrogen present at  $z \approx 6$  (Becker 2001; Djorgovski et al. 2001; Fan 2002). Reionization clearly did not occur through a single rapid phase transition. However, since absorption spectra are sensitive to even small amounts of neutral hydrogen, models with partial ionization  $x_e \lesssim 1$  can have enough neutral column density to produce the Gunn-Peterson trough while still providing free electrons to scatter CMB photons and produce large-scale polarization. Direct Gunn-Peterson observations only imply a neutral hydrogen fraction  $\gtrsim 1\%$  (Fan 2002). Accordingly, we modify the simplest model to add a second transition: a jump from  $x_e = 0$ 

REIONIZATION OPTICAL DEPTH						
Data Set	Method	$\beta$	$ au^{ m b}$	$\chi^2$	$f(>WMAP)^{c}$	
VW	Co-Add		$0.15^{+0.06}_{-0.04}$	63.0	0.249	
QVW	Co-Add		$0.18 \pm 0.03$	63.6	0.233	
KaQVW	Co-Add		$0.17\pm0.03$	91.7	0.002	
KKaQVW	Co-Add		$0.29\pm0.02$	352.1	0.000	
m KKaQ	Co-Add		$0.28\pm0.01$	474.4	0.000	
QVW	$\operatorname{Fit}$	-2.4	$0.14_{-0.04}^{+0.14}$	64.2	0.218	
KaQVW	$\operatorname{Fit}$	-2.4	$\begin{array}{c} 0.14\substack{+0.14\\-0.04}\\ 0.16\substack{+0.09\\-0.03}\end{array}$	67.0	0.162	
KKaQVW	$\operatorname{Fit}$	-2.4	$0.18\pm0.03$	62.3	0.265	
KKaQ	$\operatorname{Fit}$	-2.4	$0.15\pm0.05$	60.6	0.328	
QVW	$\operatorname{Fit}$	-2.7	$0.14^{+0.13}_{-0.04}$	64.5	0.214	
KaQVW	$\operatorname{Fit}$	-2.7	$0.17_{-0.03}^{+0.07}$	66.5	0.169	
KKaQVW	$\operatorname{Fit}$	-2.7	$0.17\pm0.03$	68.1	0.137	
KKaQ	$\operatorname{Fit}$	-2.7	$0.14\pm0.05$	70.0	0.112	
QVW	$\operatorname{Fit}$	-3.0	$0.14_{-0.04}^{+0.13}$	64.5	0.209	
KaQVW	$\operatorname{Fit}$	-3.0	$0.18\pm0.05$	66.1	0.172	
KKaQVW	$\operatorname{Fit}$	-3.0	$0.17\pm0.03$	73.7	0.061	
KKaQ	Fit	-3.0	$0.14\pm0.05$	79.1	0.030	

TABLE 2 REIONIZATION OPTICAL DEPTH<sup>a</sup>

<sup>a</sup>Optical depth  $\tau$  fitted from  $C^{IQ}(\theta)$  for various combinations of data and foreground corrections in a ACDM cosmology. There are 57 degrees of freedom for each fit.

 $^{b}68\%$  confidence statistical uncertainties

<sup>c</sup>Fraction of 1000 simulations of reionized  $\Lambda$ CDM models with  $\chi^2$  larger than WMAP value.

to  $x_e = 0.5$  at redshift  $z_r$ , followed by a second transition from  $x_e = 0.5$  to  $x_e = 1$  at redshift z = 7. Fitting this model to the measured optical depth yields  $z_r \approx 20$ . In reality, reionization is more complicated than simple step transitions. Allowing for model uncertainty, the measured optical depth is consistent with reionization at redshift  $11 < z_r < 30$ , corresponding to times  $100 < t_r < 400$  Myr after the Big Bang (95% confidence).

Extrapolations of the observed ionizing flux to higher redshift lead to predicted CMB optical depth between 0.04 - 0.08 (Miralda-Escude 2002), lower than our best fit values. The measured optical depth thus implies additional sources of ionizing flux at high redshift. An early generation of very massive (Pop III) stars could provide the required additional heating. Tegmark (1997) estimate that  $10^{-3}$  of all baryons should be in collapsed objects by z = 30. If these baryons form massive stars, they would reionize the universe. However, photons below the hydrogen ionization threshold will destroy molecular hydrogen (the principal vehicle for cooling in early stars), driving the effective mass threshold for star formation to  $\sim 10^8$  solar masses and impeding subsequent star formation (Haiman et al. 1997; Gnedin & Ostriker 1997; Tegmark 1997). X-ray heating and ionization (Venkatesan et al. 2001; Oh 2001) may provide a loophole to this argument by enhancing the formation of  $H_2$  molecules (Haiman et al. 2000).

Cen (2003) provides a physically-motivated model of "double reionization" that resembles the two-step model above. A first generation of massive Pop III stars initially ionizes the intergalactic medium. The increased metallicity of the intergalactic medium then produces a transition to smaller Pop II stars, after which the reduced ionizing flux allows regeneration of a neutral hydrogen fraction. The ionization fraction remains at  $x_e \approx 0.6$  until the global star formation rate surpasses the recombination rate at z = 6, restoring  $x_e = 1$ . The predicted value  $\tau = 0.10 \pm 0.03$  should be increased somewhat to reflect the higher WMAP values for the baryon density  $\Omega_b$  and normalization  $\sigma_8$  (Spergel et al. 2003).

#### 6. CONCLUSIONS

WMAP detects statistically significant correlations between the temperature and polarization maps. The correlations are inconsistent with instrument noise and are significantly larger than the upper limits established for potential systematic errors. The correlations are present in all WMAP frequency bands with similar amplitude from 23 to 94 GHz; fitting the data to a single power-law in frequency yields a spectral index  $\beta = -0.4 \pm 0.4$ , consistent with a CMB signal ( $\beta = 0$ ) and inconsistent with the measured spectral indices for Galactic foreground emission. A two-component fit to a superposition of CMB and Galactic foregrounds yields a positive foreground detection in both curl- and curl-free modes, with best-fit spectral index  $\beta = -2.7 \pm 0.3$  consistent with synchrotron emission of amplitude  $0.5 \pm 0.1 \ \mu$ K<sup>2</sup> antenna temperature at 41 GHz.

The fitted CMB component is robust against different data combinations and fitting techniques. On small angular scales ( $\theta < 5^{\circ}$ ), the WMAP data show the temperature-polarization expected from adiabatic perturbations in the temperature power spectrum. The data for  $\ell > 20$  agree well with the signal predicted solely from the temperature power spectra, with no additional free parameters.

The data show excess power on large angular scales  $(\theta > 10^{\circ})$  compared to the predictions based on the temperature power spectrum alone. The excess power is well described by early reionization at redshift  $z_r = 20^{+10}_{-9}$ , corresponding to times  $t_r = 180^{+220}_{-80}$  Myr after the Big Bang (95% confidence). A model-independent fit to reionization optical depth yields results consistent with the  $\Lambda$ CDM model. Our best estimate for the optical depth is  $\tau = 0.17 \pm 0.04$  (68% confidence) where the error terms include statistical, systematic, and foreground uncertainties. This value is larger than expected given the detection of a Gunn-Peterson trough in the absorption spectra of distant quasars, and implies that the universe has a complex ionization history.

The WMAP detection of early reionization opens a new frontier to explore the universe at redshift 6 < z < 30. WMAP's sensitivity to reionization is currently limited by instrument noise, both as direct statistical uncertainty and in the ability to better model and remove faint polarized foregrounds. Instrumental effects do not limit analysis of temperature-polarization correlations. The TE power spectrum and covariance matrix are available at http://lambda.gsfc.nasa.gov. We are currently performing a more complete set of systematic error analyses in the individual Q and U maps. A future data release will include full-sky polarization maps and polarization power spectra.

The WMAP mission is made possible by the support of the Office of Space Sciences at NASA Headquarters and by the hard and capable work of scores of scientists, engineers, technicians, machinists, data analysts, budget analysts, managers, administrative staff, and reviewers.

## APPENDIX

## QUADRATIC ESTIMATOR FOR TEMPERATURE-POLARIZATION POWER SPECTRUM

We estimate the temperature-polarization power spectrum from pixelized sky maps using the following formalism. We begin by expanding the temperature and polarization fluctuations in generalized spherical harmonics

$$T(\hat{n}) = \sum_{lm} a_{lm} Y_{lm}(\hat{n}) \tag{A1}$$

$$Q(\hat{n}) \pm iU(\hat{n}) = \sum_{lm} a_{\pm 2,lm \ \pm 2} Y_{lm}(\hat{n})$$
(A2)

We then decompose the polarization fluctuations into E and B like pieces

$$a_{\pm 2,lm} = E_{lm} \pm iB_{lm}.\tag{A3}$$

We can use the basic properties of the spherical harmonics

$${}_{N}Y_{lm} = (-1)^{(N+m)} {}_{-N}Y_{l-m}^{*}$$
(A4)

$$\int {}_{N}Y_{lm}(\hat{n})_{N}Y_{l'm'}^{*}(\hat{n}) = \delta_{l}^{l'}\delta_{m}^{m'}$$
(A5)

to derive

$$E_{lm} = \frac{1}{2} \int d\hat{n} \qquad \left[ Q(\hat{n}) \left( {}_{\mp 2}Y_{lm}^{*}(\hat{n}) + {}_{-2}Y_{lm}^{*}(\hat{n}) \right) \\ -i U(\hat{n}) \left( {}_{\mp 2}Y_{lm}^{*}(\hat{n}) - {}_{-2}Y_{lm}^{*}(\hat{n}) \right) \right] \\B_{lm} = -\frac{1}{2} \int d\hat{n} \qquad \left[ U(\hat{n}) \left( {}_{\mp 2}Y_{lm}^{*}(\hat{n}) + {}_{-2}Y_{lm}^{*}(\hat{n}) \right) \\ -i Q(\hat{n}) \left( {}_{\mp 2}Y_{lm}^{*}(\hat{n}) - {}_{-2}Y_{lm}^{*}(\hat{n}) \right) \right].$$
(A6)

We can now generalize the approach of Hivon et al. (2002) to estimate the coupling terms. We multiply the temperature and polarization maps by a weighting function

$$\tilde{T}_{lm} = \int d\hat{n} \ w^{T}(\hat{n}) \ I(\hat{n}) Y_{lm}^{*}(\hat{n})$$
(A7)
$$\tilde{E}_{lm} = \frac{1}{2} \int d\hat{n} \ w^{P}(\hat{n}) \ [Q(\hat{n}) (\ _{2}Y_{lm}^{*}(\hat{n}) + \ _{-2}Y_{lm}^{*}(\hat{n})) \\
-iU(\hat{n}) \ (\ _{2}Y_{lm}^{*}(\hat{n}) - \ _{-2}Y_{lm}^{*}(\hat{n}))]$$
(A8)

$$\tilde{B}_{lm} = -\frac{1}{2} \int d\hat{n} \ w^{P}(\hat{n}) \ [U(\hat{n}) \left( \ _{2}Y_{lm}^{*}(\hat{n}) + \ _{-2}Y_{lm}^{*}(\hat{n})\right) \\ -iQ(\hat{n}) \left( \ _{2}Y_{lm}^{*}(\hat{n}) - \ _{-2}Y_{lm}^{*}(\hat{n})\right)].$$
(A9)

We expand the weighting function in spherical harmonics

$$w(\hat{n}) = \sum_{lm} w_{lm} Y_{lm}(\hat{n}), \tag{A10}$$

Kogut et at.

and combine with equations A1 - A3 to yield

$$\begin{split} \tilde{T}_{lm} &= \sum_{l'm'l''m''} w_{l''m''}^T T_{l'm'} \int d\hat{n} \; Y_{l'm'}(\hat{n}) Y_{lm'}(\hat{n}) Y_{lm}^*(\hat{n}) \\ \tilde{E}_{lm} &= \frac{1}{2} \sum_{l'm'l''m''} w_{l''m''}^P \left[ E_{l'm'} \int d\hat{n} \; Y_{l''m''}(\hat{n}) \left( \left. {}_{2}Y_{l'm'}(\hat{n}) \right. {}_{2}Y_{lm}^*(\hat{n}) + \left. {}_{-2}Y_{l'm'}(\hat{n}) \right. {}_{-2}Y_{lm}^*(\hat{n}) \right) \right. \\ &\left. + iB_{lm} \int d\hat{n} \; Y_{l''m''}(\hat{n}) \left( \left. {}_{2}Y_{l'm'}(\hat{n}) \right. {}_{2}Y_{lm}^*(\hat{n}) + \left. {}_{-2}Y_{l'm'}(\hat{n}) \right. {}_{-2}Y_{lm}^*(\hat{n}) \right) \right] \\ \tilde{B}_{lm} &= \frac{1}{2} \sum_{l'm'l''m''} w_{l''m''}^P \left[ B_{l'm'} \int d\hat{n} \; Y_{l''m''}(\hat{n}) \left( \left. {}_{2}Y_{l'm'}(\hat{n}) \right. {}_{2}Y_{lm}^*(\hat{n}) + \left. {}_{-2}Y_{l'm'}(\hat{n}) \right. {}_{-2}Y_{lm}^*(\hat{n}) - {}_{2}Y_{lm}^*(\hat{n}) \right) \right. \\ &\left. - iE_{lm} \int d\hat{n} \; Y_{l''m''}(\hat{n}) \left( \left. {}_{2}Y_{l'm'}(\hat{n}) \right. {}_{2}Y_{lm}^*(\hat{n}) + \left. {}_{-2}Y_{l'm'}(\hat{n}) \right. {}_{-2}Y_{lm}^*(\hat{n}) \right) \right]. \end{split}$$
(A11)

We can then use

$$\int d\hat{n} \,_{N}Y_{lm}^{*}(\hat{n}) \,_{N'}Y_{l'm'}(\hat{n}) \,_{N''}Y_{l''m''}(\hat{n}) = (-1)^{N+m} \left[\frac{(2l+1)(2l'+1)(2l''+1)}{4\pi}\right]^{1/2} \\ \left(\frac{l \, l' \, l''}{-N \, N' \, N''}\right) \left(\frac{l \, l' \, l''}{-m \, m' \, m''}\right)$$
(A12)

to compute

$$\begin{pmatrix} \tilde{c}_l^{TT} \\ \tilde{c}_l^{TE} \\ \tilde{c}_l^{TB} \\ \tilde{c}_l^{EE} \\ \tilde{c}_l^{BB} \end{pmatrix} = \begin{pmatrix} & & & \\ & & M_{ll'}^{ab} \\ & & & \end{pmatrix} \begin{pmatrix} c_{l'}^{TT} \\ c_{l'}^{TE} \\ c_{l'}^{TB} \\ c_{l'}^{EE} \\ c_{l'}^{BB} \\ c_{l'}^{BB} \end{pmatrix}.$$
 (A13)

After some algebra, the coupling terms reduce to

$$M_{ll'}^{TT,TT} = \frac{(2l+1)(2l'+1)}{4\pi} \sum_{l''} W_{l''}^{TT} \begin{pmatrix} l \ l' \ l'' \\ 0 \ 0 \ 0 \end{pmatrix}^2$$

$$M_{ll'}^{TE,TE} = M_{ll'}^{TB,TB}$$

$$= \frac{(2l+1)(2l'+1)}{8\pi} \sum_{l''} W_{l''}^{TP} \begin{pmatrix} l \ l' \ l'' \\ 0 \ 0 \ 0 \end{pmatrix} \left[ \begin{pmatrix} l \ l' \ l'' \\ -2 \ 2 \ 0 \end{pmatrix} + \begin{pmatrix} l \ l' \ l'' \\ -2 \ 2 \ 0 \end{pmatrix} \right]$$
(A14)

$$M_{ll'}^{EE,EE} = M_{ll'}^{BB,BB}$$

$$= \frac{(2l+1)(2l'+1)}{16\pi} \sum_{l''} \mathcal{W}_{l''}^{PP} \left[ \begin{pmatrix} l & l' l'' \\ -2 & 2 & 0 \end{pmatrix} + \begin{pmatrix} l & l' l'' \\ -2 & 2 & 0 \end{pmatrix} \right]$$

$$\times \left[ \begin{pmatrix} l & l' l'' \\ -2 & 2 & 0 \end{pmatrix} + \begin{pmatrix} l & l' l'' \\ -2 & 2 & 0 \end{pmatrix} \right]$$
(A15)

$$M_{ll'}^{EE,BB} = M_{ll'}^{BB,EE}$$

$$= \frac{(2l+1)(2l'+1)}{2} \sum W_{ll'}^{PP} \left[ \begin{pmatrix} l & l' & l'' \\ l' & l'' \end{pmatrix} - \begin{pmatrix} l & l' & l'' \\ l'' & l'' \end{pmatrix} \right]$$
(A16)

$$-\frac{16\pi}{16\pi}\sum_{l''}V_{l''}\left[\left(-2\ 2\ 0\ \right)-\left(-2\ 2\ 0\ \right)\right]$$

$$\times\left[\left(\begin{array}{cccc}l\ l'\ l''\\-2\ 2\ 0\ \end{array}\right)-\left(\begin{array}{cccc}l\ l'\ l''\\-2\ 2\ 0\ \end{array}\right)\right] \tag{A17}$$

where

$$\mathcal{W}_l^{ab} = \sum_m w_{lm}^a w_{lm}^{b*},\tag{A18}$$

with a and b referring to either T or P. All of the other coupling terms are zero. Note that if we use different weighting functions for T, Q and U, we increase the coupling between E and B modes.

# UNIFORM TEMPERATURE WEIGHTING

If we use the full sky to compute the temperature spherical harmonic terms, then the cross-correlation term and its error matrix becomes particularly simple. For this case,  $w_{00}^T = 1/\sqrt{4\pi}$  and all other coupling terms are 0. In this limit, the measured  $c_{l'}^{TE}$  is just a constant times the true  $c_l^{TE}$ 

$$c_l^{TE} = \frac{\tilde{c}_l^{TE}}{f} \tag{B1}$$

where

$$f = \int w_E(\hat{n}) \frac{d\hat{n}}{4\pi} \tag{B2}$$

The covariance matrix for these terms are diagonal.

$$\mathbf{M}_{ll} = \frac{c_l^{TT} \tilde{c}_l^{EE}}{(2l+1)f^2} \tag{B3}$$

#### REFERENCES

- Baccigalupi, C., Burigana, C., Perrotta, F., De Zotti, G., La Porta, L., Maino, D., Maris, M., & Paladini, R. 2001, å, 372, 8
  Barnes, C. et al. 2003, ApJ, submitted
  Becker, R. H. e. a. 2001, AJ, 122, 2850
  Bennett, C. L., Bay, M., Halpern, M., Hinshaw, G., Jackson, C., Jarosik, N., Kogut, A., Limon, M., Meyer, S. S., Page, L., Spergel, D. N., Tucker, G. S., Wilkinson, D. T., Wollack, E., & Wright, E. L. 2003a, ApJ, 583, 1
  Bennett, C. L., Halpern, M., Hinshaw, G., Jarosik, N., Kogut, A., Limon, M., Meyer, S. S., Page, L., Spergel, D. N., Tucker, G. S., Wollack, E., Wright, E. L., Barnes, C., Greason, M., Hill, R., Komatsu, E., Nolta, M., Odegard, N., Peiris, H., Verde, L., & Weiland, J. 2003b, ApJ, submitted
  Bennett, C. L. et al. 2003c, ApJ, submitted
  Bennett, C. L. et al. 2003c, ApJ, submitted
  Bond, J. R. & Efstathiou, G. 1984, ApJ, 285, L45
  Brouw, W. N. & Spoelstra, T. A. T. 1976, Astron. Astrophys. Suppl. Ser., 26, 129
  Bruscoli, M., Tucci, M., Natale, V., Carretti, E., Fabbri, R., Sbarra, On Status, S., Contentino, S., Sharra, C., Status, S., Sharra, C., Superson, M., Status, S., Sharra, C., Superson, S., Sharra, C., Superson, S., Sharra, C., Superson, S., Sharra, S., Sharra, C., Superson, M., Sharra, Status, Status

- Ser., 20, 129
  Bruscoli, M., Tucci, M., Natale, V., Carretti, E., Fabbri, R., Sbarra, C., & Cortiglioni, S. 2002, New Astronomy, 7, 171
  Cen, R. 2003, ApJ, submitted (astro-ph/0210473)
  Coulson, D., Crittenden, R. G., & Turok, N. G. 1994, Phys. Rev. Lett., 73, 2390
  Djorgovski, S. G., Castro, S., Stern, D., & Mahabal, A. A. 2001, ApJ, 560, 156
- Djorgovski, S. G., Castro, S., Stern, D., & Manabal, A. A. 5560, L5
  Fan, X. e. a. 2002, AJ, 123, 1247
  Gnedin, N. Y. & Ostriker, J. P. 1997, ApJ, 486, 581
  Haiman, Z., Abel, T., & Rees, M. J. 2000, ApJ, 534, 11
  Haiman, Z., Rees, M. J., & Loeb, A. 1997, ApJ, 484, 985
  Hinshaw, G. F. et al. 2003a, ApJ, submitted
  2002b, ApJ, cubmitted

- -. 2003b, ApJ, submitted

- Hivon, E., Górski, K. M., Netterfield, C. B., Crill, B. P., Prunet, S., & Hansen, F. 2002, ApJ, 567, 2
  Hu, W. & Dodelson, S. 2002, ARA&A, 40, 171
  Hu, W. & Dodelson, S. 2002, ARA&A, 40, 171
  Hu, W. & Sugiyama, N. 1994, ApJ, 436, 456
  Hu, W. & White, M. 1997, Phys. Rev. D, 56, 596
  Jarosik, N. et al. 2003, ApJS, 145
  Kaiser, N. 1983, MNRAS, 202, 1169
  Kamionkowski, M., Kosowsky, A., & Stebbins, A. 1997, Phys. Rev. D, 55, 7368
  Kosowsky, A. 1996, Annals of Physics, 246, 49
  Kovac, J. et al. 2002, ApJ, astro-ph/0209478
  Lubin, P. M. & Smoot, G. F. 1981, ApJ, 245, 1
  Miralda-Escude, J. 2002, ApJ, submitted (astro-ph/0211071)
  Oh, S. P. 2001, ApJ, 553, 499
  Page, L. et al. 2003, ApJ, submitted
   2003b, ApJ, 585, in press
  Peiris, H. et al. 2003, ApJ, submitted
  Rees, M. J. 1968, ApJ, 153, L1
  Seljak, U. & Zaldarriaga, M. 1996, ApJ, 469, 437
  Spergel, D. N. et al. 2003, ApJ, submitted
  Tegmark, M., e. a. 1997, ApJ, 474, 1
  Tucci, M., Carretti, E., Cecchini, S., Nicastro, L., Fabbri, R., Gaensler, B. M., Dickey, J. M., & McClure-Griffiths, N. M. 2002, ApJ, 579, 607
  Uvanker, B., Fuerst, E., Beich, W., Beich, P., & Wielebinski, B.
- ApJ, 579, 607 Jyan, Ker, B., Fuerst, E., Reich, W., Reich, P., & Wielebinski, R. 1998, Astron. Astrophys. Suppl. Ser., 132, 401
  —. 1999, Astron. Astrophys. Suppl. Ser., 138, 31
  Venkatesan, A., Giroux, M. L., & Shull, J. M. 2001, ApJ, 563, 1
  Zaldarriaga, M. 1997, Phys. Rev. D, 55, 1822
  Zaldarriaga, M. Saliot, L. 1007, Phys. Rev. D, 55, 1820

- Zaldarriaga, M. & Seljak, U. 1997, Phys. Rev. D, 55, 1830